

## A generally covariant *generalization* of the Dirac equation that does not require gauges (Newpde)

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This fundamental Newpde(3) is derivable, if  $\kappa_{ij}$  is known, from the part between brackets in:  
 $(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 - \kappa_{tt} dt^2 = ds^2$ . Dirac's 1928 guess of flat space  $\kappa_{xx} = \kappa_{yy} = \kappa_{zz} = \kappa_{tt} = 1$  (in his equation(1)) was *not* fundamental since in general space is not flat\*, is curved so generally covariant. A *truly* fundamental  $\kappa_{ij}$  must instead be derived from

the *ultimate* Occam's razor postulate 1 (+C). In fact the (simplest) algebraic definition of 1 is  $z=zz$  (Thus  $z=1,0$ ) and *merely adding constant C* (so  $\delta C=0$ ) most simply in:  $z'=z'z'+C$  (eq.1) does indeed derive that Newpde. To show this note these are unknown Cs except for that single  $C=0$  since  $z=zz+0$  was postulated and so  $z=1,0 \in \{z'\}$ . So you plug 1,0 back into eq.1 for  $z'$ :

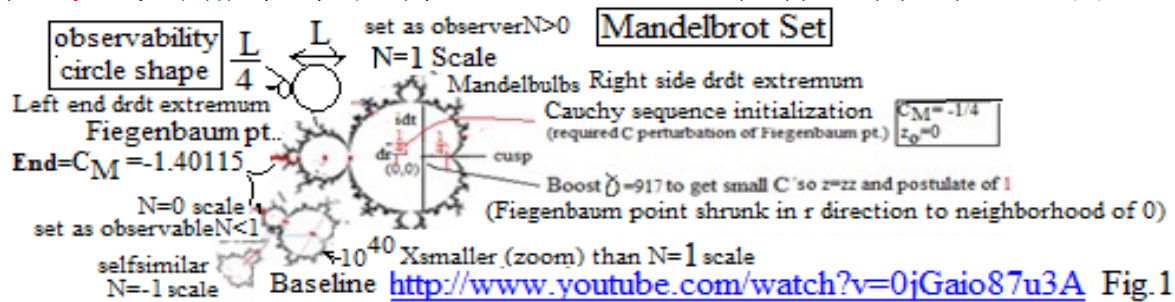
$z=0 = z_0 = z'$  in the iteration of eq.1 using  $\delta C=0$  *generates* the (2D)Mandelbrot set  $C=C_M$  (fig1)  
 (Need iteration to get all the Cs because of the  $\delta C=0$  (appendix). Note  $10^{40N} C_M$  fractal scales)

$z=1$ ,  $z'=1+\delta z$  substitution into eq.1 using  $\delta C=0$  ( $N>0$  observer) gets eq5 so 2D Dirac eq.(e,v)

(Eq.5 gives the Minkowski (flat space) metric, Clifford algebra  $\gamma^i$  and eq.11 *in one step.*)

These two  $z=1$  and  $z=0$  steps together (appendix) get the curved space  $2D+2D=4D$  Newpde (3) and thus the 4D universe, no more and no less. ( $\kappa_{ij}$  (4) from eqs.13,14,15) So just **postulate 1 !!!**

(Newpde:  $\gamma^\mu \sqrt{(\kappa_{\mu\mu})} \partial \psi / \partial x_\mu = (\omega/c) \psi$ ,  $\kappa_{00}=1-r_H/r=1/\kappa_{rr}$ ,  $r_H=(2e^2)(10^{40N})/(mc^2)$ .  $N=-1,0,1,..$ fractal)



That  $\kappa_{ij}$  (in the Newpde) also unifies theoretical physics

Note that this new Newpde  $\kappa_{ij}$  contains a Mandelbrot set(6)  $e^2 10^{40N}$  Nth fractal scale source(fig1) term(4) that also just happens to successfully **unify** the **Standard electroweak Model** (eg.,the 4 Bosons, eq.12,appendix A) and **Quantum Mechanics** (i.e, Newpde, appendix C) with **General Relativity** (eg.,Schwarzschild metric  $g_{ij}$ ,  $N=-1$ ) which no one has done before. For example:

For  $N=-1$  (i.e., $e^2 X 10^{-40} \equiv G m_e^2$ )  $\kappa_{ij}$  is then by inspection(4) the Schwarzschild metric  $g_{ij}$ ; so we just derived General Relativity and the gravity constant G from Quantum Mechanics in one lineWow for  $N=0$  the higher order Taylor expansion(terms) of  $\sqrt{\kappa_{ij}}$  gives the anomalous gyromagnetic ratio and Lamb shift *without* the renormalization and infinities (appendix D3): This is very important\*

So  $\kappa_{uv}$  provides the general covariance of the Newpde. Eq. 4 even provides us space-time r,t.

For  $N=1$  (so  $r < r_c$ ) Newpde zitterbewegung expansion stage explains the universe expansion (For  $r > r_c$  it's not observed, per Schrodinger's 1932 paper.).

For  $N=1$  zitterbewegung harmonic coordinates and Minkowski metric submanifold (after long time expansion) gets the De Sitter ambient metric we observe (D16, 6.2).

For  $N=0$  Newpde  $r=r_H$   $2P_{3/2}$  state composite 3e is the baryons (sect.2, partII) and Newpde  $r=r_H$  composite e,v is the 4 Standard electroweak Model Bosons (4 eq.12 rotations→appendixA)

So we got all physics here by *mere inspection* of this (curved space) Newpde with no gauges!

## References

- (1)  $\gamma^\mu \partial \psi / \partial x_\mu = (\omega/c) \psi$
- (2) Spherical symmetry:  $(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 - \kappa_{tt} dt^2 = ds^2$   
 $\kappa_{xx} = \kappa_{yy} = \kappa_{zz} = \kappa_{tt} = 1$  is flat space, Minkowski, as in his Dirac equation(1).
- (3) Newpde:  $\gamma^\mu \sqrt{(\kappa_{\mu\mu})} \partial \psi / \partial x_\mu = (\omega/c) \psi$  for e,v. So we didn't just drop the  $\kappa_{\mu\nu}$  (as is done in ref.1)
- (4) Here  $\kappa_{oo} = 1 - r_H/r = 1/\kappa_{rr}$ ,  $r_H = (2e^2)(10^{40N})/(mc^2)$ . The  $N = \dots -1, 0, 1, \dots$  fractal scales (eqs.13,14,15)
- (5) Penrose in a utube video implied that the Mandelbrot set might contain physics. Here we merely showed how to find it. For example the (fractal Mandelbulb neighborhood area  $|drdt| > 0$  of the) Fiegenbaum point is a subset (containing that  $10^{40N}$  Xselfsimiilar scale jump: Fig1)

\* I found that there is a problem with the 1928 Dirac equation(1). In (spherical symmetry):  
 $(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 - \kappa_{tt} dt^2 = ds^2$  (1)  
 Dirac set  $\kappa_{xx} = \kappa_{yy} = \kappa_{zz} = \kappa_{tt} = 1$  so flat space(2) in his equation(1) when we know in general space is not flat, there are forces. So over the past 100 years (since 1928, ref.1) people have had to try to make up for that(flat space) mistake by adding ad hoc convoluted gauge force after gauge force until fundamental theoretical physics became a mass of confusion, a train wreck, a junk pile. So all they can do for ever and ever is to rearrange that junk pile Dirac noticed this too and even, toward the end of his life, tried his hand at *fixing*  $\kappa_{ij}$ . See Chapter 15 of the Memorial Volume "Paul Adrian Maurice Dirac: R,eminiscences about a Great Physicist", edited by Behram N. Kursunoglu and Eugene Paul Wigner. There Dirac mentions "a different kind of Hamiltonian" which indeed would change  $\kappa_{ij}$ . Richard Feynman too felt very uncomfortable with "these rules of subtracting infinities" (renormalization, yet another unfortunate consequence of setting  $\kappa_{ii} = 1$ ) and called it a "shell game" and "hocus pocus, "Renormalization", Oct 2009). Even more recently, Lewis H. Ryder in his text "Quantum Field Theory" (edition 1996, page 390) lamented "there ought to be a more satisfactory way of doing things".

Well, we found it here: The  $N=0$  higher order Taylor expansion terms(4) in  $\sqrt{\kappa_{ij}}$  gives the anomalous gyromagnetic ratio and Lamb shift *without* the renormalization and infinities (appendix D3). It is of tremendous value to QM to not require renormalization anymore anywhere and yet still get those well known high precision (qed) quantitative results from a mere Taylor expansion(D4). This result, and that ultimate Occam's razor single postulate, creates a new paradigm that sets us back on course of seeking fundamental theoretical physics again (i.e., **postulate 1**).

**Occam's Razor Implies Postulate 1:** Postulate 1 is the simplest idea imaginable. 1 (in  $1=1X1$ ) is thereby the *ultimate* application of Occam's razor since 0 (also in  $z=zz$ ) postulates literally *nothing*. Also  $z=zz$  is 'simpler' than  $z=zzzz$  and  $z'=z'z'+C$  is simpler than  $(z'+C)=(z'+C)z'+C$ .

## I Newpde from **Postulate 1 (observable)**

You would think just postulating 1 is nonsense. That can't lead anywhere, right? But it does! The (simplest) algebraic definition of 1 is  $z=zz$  (Thus  $z=1,0$ ) and *merely adding constant C* (so  $\delta C=0$ ) most simply in  $z'=z'z'+C$  (eq.1) derives the Newpde and so physics. To show this note these are unknown Cs except for that single  $C=0$  since  $z=zz+0$  was postulated and so  $z=1,0 \in \{z'\}$ . So we plug  $z=1,0$  back into eq.1 for  $z'$ :

$z=0 = z_0 = z'$  in the iteration of eq.1 using  $\delta C=0$  *generates* the (2D)Mandelbrot set  $C=C_M=\text{end}^{**}$  (Need iteration to get all the Cs because of the  $\delta C=0$  (appendix),  $\text{end}=10^{40N}X$  fractal scales)

$z=1$ ,  $z'=1+\delta z$  substitution into eq.1 using  $\delta C=0$  ( $N>0$  observer) gets eq5 so 2D Dirac eq.(e,v)

(Eq.5 gives the Minkowski (flat space) metric, Clifford algebra  $\gamma^i$  and eq.11 *in one step.*)

These two  $z=1$  and  $z=0$  steps together (appendix) get the curved space  $2D+2D=4D$  **Newpde** (3) and thus the 4D universe, no more and no less .

So just **postulate 1 !!!**

## Summary

All I did here is to postulate 1 and **prove it's observable**: Eq.11:  $p_x\psi = -i\hbar\partial\psi/\partial x$  is the well known *observables* (p) definition,  $\psi$  is from **Newpde**(3). C is merely some *required observer*! Note also eq.11 *real number* eigenvalue observability (eg., dr noise) derived from our right side  $-1/4$  initiated Cauchy sequence(7), Ch.2, =reals: our Mandelbrot set iteration sequence there!

Therefore  $N=0$  **postulate 1** can also be used in a list-define math to get the *real number* algebra (without all those many Rel#math axioms). Eg.,  $1 \cup 1 \equiv 1+1$  (B2, Ch.2). So we get both the physics (See ref.5) AND (rel#)mathematics from ONE postulate1, everything! We finally figured it out!

## Compare and contrast

The core of mainstream physics is the Standard electroweak Model (SM) that gives us important results like Maxwell's equations and weak interaction theory that explain electricity and magnetism and some radioactive decays respectively. Add to that QCD that explains the nuclear force (NF) and baryons. General Relativity (GR) gives us gravity and mechanics. But they are not fundamental since they contain *many assumptions* (Lagrangian densities, free parameters, many dimensions, gauge symmetries,..etc.,) of unknown origin.

### In contrast

what if you found instead a mathematical theory with only one *simple assumption* (eg., '1', defined from  $z=zz$  since  $1=1X1$ ) using a *single simple math step* (eg., just add C to 1) top down that got a *generally covariant generalization of the Dirac equation that does not require gauges* (**Newpde**, next page) that in turn gave these same results (i.e., **SM particles**, **NF**, **GR, QM** in ref.5 & **real#**)? You will then have a truly *fundamental* theory.

Review:

Algebraic definition of 1 is  $z=zz$  so  $(z=\mathbf{1},0)$ , add constant C (so  $\delta C=0$ ) to get  $z'=z'z'+C$  (eq.1)

$z=zz$  postulated so  $z=\mathbf{1},0 \in \{z'\}$

## Appendix Details of those two $z=0$ , $z=\mathbf{1}$ steps (in above proof of observability)

But first solve equation 1 by itself (to at least see that  $z'$  can be complex)

Thus plug  $z'=\mathbf{1}+\delta z$  into eq.1 and get  $\delta z+\delta z\delta z=C$  (3)

For real  $C<-1/4$   $\delta z = (-1 \pm \sqrt{1+4C})/2 = dr+idt$  (4)

is complex. Fiegenbaum point  $C_M=C$  eq.3  $\delta z$  in fig.6

1<sup>st</sup> step:

$\mathbf{z}=\mathbf{0}=z_0=z'$  To find all C substitute  $z'$  on left (eq.1) into right  $z'z'$  repeatedly and get iteration  $z_{N+1}=z_N z_N - C$ . Constraint  $\delta C=0$  requires us to reject the Cs for which  $-\delta C=\delta(z_{N+1}-z_N z_N)=\delta(\infty-\infty) \neq 0$  which gets the **Mandelbrot set**  $C_M=\text{end}^{**}=\text{Fiegenbaum pt.}$  from  $\delta C_r=0$ .  $drdt \neq 0$ , eq.7 Also in distance units of 1 on the  $N=0$  fractal scale, for observer  $N=1$  scale lengths  $\text{Rel}\delta z >> 1$ .

2<sup>nd</sup> step:

$\mathbf{z}=\mathbf{1}$  in  $z'=\mathbf{1}+\delta z$  in eq.1 get eq.3 ( $\text{rel}\delta z \gg 1$ ):  $\delta(\delta z+\delta z\delta z)=\delta\delta z(1)+\delta\delta z(\delta z)+(\delta z)\delta\delta z \approx \delta(\delta z\delta z)=0=(\text{plug in eq.4})=\delta[(dr+idt)(dr+idt)]=\delta[(dr^2-dt^2)+i(dr dt+dt dr)]=0$  (5)  
 $= (\text{Minkowski metric}(9))+i(\text{Clifford algebra})$

Factor eq.5  $\delta(dr^2-dt^2)=\delta[(dr+dt)(dr-dt)]=0=[\delta(dr+dt)](dr-dt)+[(dr+dt)]\delta(dr-dt)=0$  (6)  
 so  $(\rightarrow \pm e) dr+dt=ds, dr-dt=ds \equiv ds_1$ , for  $(-dr-dt)^2=ds^2 \rightarrow$  Ist and IVth quadrant in fig3 (7)  
 Also note the positive scalar  $drdt$  of eq.7 (so not eq.10 vacuum) implies the eq.5 *non* infinite extremum  $\text{imaginary} \equiv drdt+dt dr=0=\gamma^i dr^j dt+\gamma^j dt \gamma^i dr=(\gamma^i \gamma^j+\gamma^j \gamma^i) drdt$  so Clifford algebra

$$(\gamma^i \gamma^j+\gamma^j \gamma^i)=0, i \neq j. \quad (7a)$$

$$(\rightarrow \text{light cone } v) dr+dt=ds, dr=-dt, \quad \text{for } (-dr-dt)^2=ds^2 \rightarrow \text{III quadrant} \quad (8)$$

$$“ “ dr-dt=ds, dr=dt, \quad \text{for } (-dr-dt)^2=ds^2 \rightarrow \text{II quadrant} \quad (9)$$

$$(\rightarrow \text{vacuum}, z=1) dr=dt, dr=-dt \quad \text{so } dt=0=dr \quad (\text{So eigenvalues of } dt, dr=0 \text{ in eq.11}) \quad (10)$$

We square eqs.7,8,9  $ds_1^2=(dr+dt)(dr+dt)=(-dr-dt)(-dr-dt)=[dr^2+dt^2]+(drdt+dt dr) \equiv ds^2+ds_3=ds_1^2$ . Since  $ds_3$  (is max or min) and  $ds_1^2$  (from eq.7,8,9) are invariant then so is **Circle**  $ds^2=dr^2+dt^2=ds_1^2-ds_3$ , also implying the rest of the Clifford algebra  $\gamma^i \gamma^i=1$  in eq.7a, no sum on 'i' and also the lemniscate formulation(fig.7). Note this separate  $ds$  is a minimum at  $45^\circ$  given the eq.7 constraints and so Circle  $\equiv \delta z=dse^{i0}=dse^{i(\Delta\theta+\theta_0)}=dse^{i((\cos\theta dr+\sin\theta dt)/(ds)+\theta_0)}$ ,  $\theta_0=45^\circ$ . ( $\delta z$  in fig.6). We define  $k \equiv dr/ds$ ,  $\omega \equiv dt/ds$ ,  $\sin\theta \equiv r$ ,  $\cos\theta \equiv t$ .  $dse^{i45^\circ} \equiv ds'$ . Take ordinary derivative  $dr$  (since flat

$$\text{space) of 'Circle' } \frac{\partial \left( dse^{i \left( \frac{r dr}{ds} + \frac{t dt}{ds} \right)} \right)}{\partial r} = i \frac{dr}{ds} \delta z \text{ so } \frac{\partial (dse^{i(rk+wt)})}{\partial r} = ik \delta z, k \delta z = -i \frac{\partial \delta z}{\partial r} \quad (11).$$

$\langle F \rangle^* = \int (F\psi)^* \psi d\tau = \int \psi^* F \psi d\tau = \langle F \rangle$  Hermitian) from right side real number Cauchy seq.starting at  $-1/4$  iteration case of the Mandelbrot set iteration(7), Ch.2,sect.2, with small C limit making *real eigenvalues* (eg.,noise) likely. The observables  $dr \rightarrow k \rightarrow p_r$  condition gotten from eq.11 **operator formalism**(10) thereby converting eq.7-9 into Dirac eq. pdes( 4XCircle solution in left side fig.1 also implies observability). Cancel that  $e^{i45^\circ}$  coefficient ( $45^\circ=\pi/4$ ) then multiply both sides of eq.11 by  $\hbar$  and define  $\delta z \equiv \psi$ ,  $p \equiv \hbar k$ . Eq.11 becomes the familiar

$$p_r \psi = -i\hbar \frac{\partial \psi}{\partial r} \quad (11)$$

Repeat eq.3 for  $\tau, \mu$  respective  $\delta z$  lobes in fig.6 so they each have their own neutrino  $\nu$ .

**\*\*end**  $\delta C = \left(\frac{\partial C}{\partial r}\right)_t dr + \left(\frac{\partial C}{\partial t}\right)_r dt = 0$ . For those 4X circles (so eq.11 *observables*) in fig1 N=0: eq.3 gives  $C \approx \delta z' = ds e^{i\theta}$ . Furthermore if  $\theta=0$ ,  $ds e^{i\theta} = ds = dC (=dr)$  we additionally have the required *Real* eigenvalues for  $dr/ds$  observable in eq.11a. making  $\left(\frac{\partial C}{\partial r}\right)_t dr = 0$  only at the Fiegenbaum point  $=F^x=(-1.40115, i0)=C_M=end$  since there  $\partial r \approx dr \approx 0$  and  $\partial C/\partial r = \text{constant}$  (for these 4X circles). Note if a circle (or many circles) is rotated (U), translated (D), shrunk (S) equally in both dimensions (i.e.,  $(\partial x^j/\partial x'^k) f^j = f'^k \equiv \begin{bmatrix} f_{1N} \\ f_{2N} \end{bmatrix} = S_N \begin{bmatrix} U_{11} & U_{12} \\ U_{21} & U_{22} \end{bmatrix} \begin{bmatrix} f \\ 0 \end{bmatrix} + \begin{bmatrix} D_{1N} \\ D_{2N} \end{bmatrix}$ ) it is still a circle, eq.11 still holds, so it's still an observable as seen in the N fractal scale zoom. Thus you can pick out from that zoom these fig.1 Mandelbrot set 4Xdiameter circles as the only **observables** geometry in all that clutter so we get for that 'end' point:  $S_N C_M = 10^{40N} C_M$  in the eq.13.

### **z=1, z=0 steps together** (on Circle with small C boost)

**Postulate1** also implies a small C in eq.1 which thereby implies a (Minkowski metric Lorentz contraction(9))  $1/\gamma$  boosted frame of reference in the eq.3  $C=C_M/\gamma \equiv C_M/\xi_1 = \delta z' = \Delta$  for next small smaller fractal scale  $N_{ob} < 0$  so  $\delta z' \ll 1$  (composite 3e: sect.2 and PartII). Also recall  $\delta ds^2 = 0$  in eq.5. For  $N=0$  eq.5 (which is true only for  $N>0$ ) and so eq.7 is not quite true (and  $\delta z$  in eq.11 perturbed). But  $\delta C = \delta ds = 0$  (since imaginary extremum  $=0$ ) is still true so we must have an angle perturbation of big  $N=1$   $dr, dt$  for  $\theta_0 = 45^\circ$  on above **ds Circle** and so a slightly modified eq.7

$$(dr - \delta z') + (dt + \delta z') = dr' + dt' = ds \quad (12)$$

### **N=1, N=0 extremum rotations**

Since (eq.12)  $dr, dt$  is the (eq.11) observer  $N_{\text{observer}} > 0$  scale then  $\delta z'$  defines the  $N_{ob} = 0$  object. Also the  $r, t$  axis' are the max extremum for  $ds^2$ , and the  $ds^2$  at  $45^\circ$  is the min extremum  $ds^2$  so  $\Delta\theta = \theta \text{ modulo } 45^\circ$  is pinned to an axis' so extreme  $\Delta\theta \approx \pm 45^\circ = \delta z'$ . So in eq.12 the 4 rotations  $45^\circ + 45^\circ = 90^\circ$  define 4 Bosons (appendix A), and  $45^\circ - 45^\circ = 0$  eq.7-9 defines leptons. Again, for  $N_{ob} < 0$ , you also have other (smaller) fractal scale extreme  $\delta z'$  (eg., tiny Fiegenbaum pts so  $N=1$   $dr=r$ , for  $N=0$ ) so metric coefficient  $\kappa_{rr} \equiv (dr/dr')^2 = (dr/(dr - (C_M/\xi_1)))^2 = 1/(1 - r_H/r)^2 = A_1/(1 - r_H/r) + A_2/(1 - r_H/r)^2$ . The partial fractions  $A_i$  can be split off from RN and so  $\kappa_{rr} \approx 1/[1 - ((C_M/\xi_1)r)]$  (13) ( $C_M$  defined to be  $e^2$  charge,  $\gamma \equiv \xi_1$  mass). So:  $ds^2 = \kappa_{rr} dr'^2 + \kappa_{oo} dt'^2$  (14)

$$\text{From eq.7a } dr' dt' = \sqrt{\kappa_{rr}} dr' \sqrt{\kappa_{oo}} dt' = dr dt \text{ so } \kappa_{rr} = 1/\kappa_{oo} \quad (15)$$

We can then do a rotational dyadic coordinate transformation of  $\kappa_{\mu\nu}$  to get the Kerr metric which is all we need for our GR applications(9). So from eqs.4,5,14,15 we found the relation between  $x_i, x_j$  pairs:  $(\sum_{i=1}^2 \gamma^i \sqrt{\kappa_{ii}} dx_i)^2 = \sum_{i=1}^2 \kappa_{ii} d^2 x_i$  (14a). So given this added 2D  $\Delta$  perturbation we get curved space  $2D \otimes 2D = 4D$  independent  $x_1, x_2 \rightarrow x_1, x_2, x_3, x_4$ . Also assuming orthogonality  $dr^2 \equiv dx_1^2 + dx_2^2 + dx_3^2$  (as  $r \rightarrow \infty$  in eq.13,15) the right side of eq.14a therefore has the 2 in the sum replaced by a 4 implying the left side then has to be in eq.14a for the 2D form to be a special case (of any 2  $x_i x_j$ ) in B2: Imposing orthogonality thereby creates 6 pairs of eqs.4&5. So eq.14a becomes:  $(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 + \kappa_{tt} dt^2 = ds^2$ . Multiplying the bracketed term by  $1/ds$  & unknown  $\delta z \equiv \psi$  so eq 11 implies 4D **Newpde**:

$$\gamma^\mu (\sqrt{\kappa_{\mu\mu}}) \partial \psi / \partial x_\mu = (\omega/c) \psi \text{ for } e, \nu, \kappa_{oo} = 1 - r_H/r = 1/\kappa_{rr} \quad r_H = e^2 X 10^{40N}/m \quad N(= -1, 0, 1, \dots) \quad (16)$$

$= C_M/\gamma$  (from sect.2)  $C_M = \text{Fiegenbaum point}$ . So: **postulate1**  $\rightarrow$  **Newpde**. syllogism

\*Need small C boost for  $z=zz$  so postulate1 It is created by Newpde  $r=r_H$   $2P_{3/2}$  stable state P, sect2

The 4 eq.12 Newpde  $e, \nu$  rotations at  $r=r_H$  are the 4  $W^+, \gamma, W^-, Z_0$  SM Bosons (appendix A)

So Penrose's intuition(6) was right on! There is physics in the Mandelbrot set, all of it.



**2 N=0 Small C boost circle observables.** Note that **real** component of eq.5 is Minkowski metric implying possible Lorentz transformation Fitzgerald contraction  $C/\gamma$  boosted C frames of reference. From eq.3 for  $N=0: C \approx \delta z$  and  $C \rightarrow C/\gamma = C_M/\gamma \equiv C_M/\xi$ . So from eq.3 for  $N=0$  in eq.12  $C_M/\xi = \delta z$  (eq.17)

( $C_M/\xi = \delta z$  for  $N=1$ ) . So  $\delta C_M = 0 = \delta \delta z \xi + \delta \xi \delta z = 0$  ( $N=0$ ). If  $z=0$  then  $\delta z' = -1$  is big for  $N=0$ . In  $\delta C_M = 0 = \delta \delta z \xi + \delta \xi \delta z = 0$  for  $\xi$  small then  $\delta \xi$  has to be small and so  $\xi$  is stable, electron  $\xi_0 = \Delta \epsilon = \epsilon$ . for  $z=1$  then  $\delta z$  is small on  $N=0$  thus  $\delta \xi$  and  $\xi$  are both big so unstable and large mass For  $N=0$  observable  $\xi = 10^{40} N \xi$ ; the subatomic observable cosmos. The Laplace Beltrami method (D4) ,  $N>1$  applies to observation of the huge  $r_H$  cosmological objects. ( $N=1$  is what it is).

**N=1 small C boost so postulate observable 1 (e)** Recall the Mandelbrot set in small C boost  $C_M = \xi C$  sect.2. From eq.3  $\delta z + \delta z \delta z = C$  or observer  $N=1$   $\delta z \delta z = C$ . The  $68.7^\circ$  is from eq3 quadratic equation at the Feigenbaum point.  $45^\circ$  from minimum  $ds^2$ .  $\mu$  then is not a constant in time because of eq.12 angle New pde zitterbewegung contribution to the  $\delta z$  chord perturbation of the  $45^\circ$ . The observer limaçon is the electron e, the  $45^\circ$  intersection chord with that Mandelbulb is  $\mu$  ( fig6 below.). The  $68.74^\circ$  tiny Mandelbulb is the tauon. But what if we constructed instead from the limaçon 'e' composite  $3e$   $2P_{3/2}$  state at  $r=r_H$  requiring a mass constraint of  $2m_p \geq$  mass of the respective Hund rule free particle  $2S_{1/2}$  ( $\equiv$  the tauon  $\tau$ ) plus  $1S_{1/2}$  ( $\equiv$  muon  $\mu$ ) states? The reduced mass is then the proton that then also generates the  $\gamma$  boost on the  $m_e$  s that gives us that small C and the **postulate 1** (observable e).

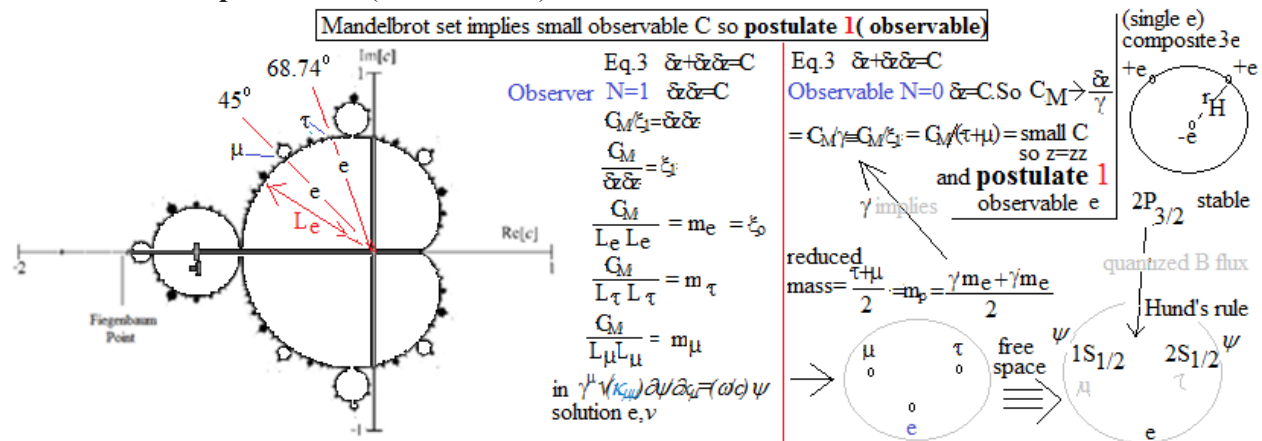


Fig.6

### Conclusion

So we really did just **postulate 1 (observable e)** fig6, right side, and **prove observability** (eq.11,16).

**3e Stability:** We can actually calculate  $m_p$  from the quantization of the magnetic flux  $h/2e = \Phi_0 = BA$ . Using the Mandelbrot set  $2m_p = \tau + \mu + e = \xi_1$  (which just sets  $h$ ) and the Mercuron equation D15 for  $\mu$  and also use the location of object B to find the actual magnitude of  $m_e$  (eqD9). So *stability* is implied by  $(dt')^2 = (1 - r_H/r) dt^2$  since clocks stop at  $r=r_H$ . That 3<sup>rd</sup> mass also reverses the pair annihilation with virtual pair creation inside the  $r_H$  volume given  $\sigma = \pi r_H^2 \approx (1/20)$  barns. which is the reason why only composite  $3e$  gives stability and not other larger composites (except multiples of  $3e$  itself). Note here we also derived baryon physics ( $m_p$ ).

The ground state  $m_e$  (from the  $67.8^\circ$  line on the Mandelbrot set) as a fraction of the tauon mass  $m_e = \xi_0 = \Delta\varepsilon = .0005799$ . (18)

Inertial frame dragging suppression (D9) from nearby object B gives this large value of  $m_\tau + m_e$ .

## 2.1 $C = -1/4$ (right)min-max *Right end Big limaçon at $z = -1/4$ , Real eigenvalues(2)*

On the right end minimum of the  $\|C\|$  maxima extremum of the Mandelbrot set we get the Mandelbrot set iteration formula starting from extremum  $z_0 = 0$ ,  $C_M = -1/4$  that is *also* uniquely a Cauchy sequence(2) of rational numbers (since the sequence started with a rational number  $-1/4$ ) then  $-1/4 = 0 \times 0 - 1/4$ ;  $-3/16 = (-1/4)(-1/4) - 1/4$ , etc., with limit 0 that implies that 0 in our (later) small  $C'$  uncertainty neighborhood limit application region has a nonzero probability of being a real number  $dr$  so we have **real eigenvalues** (in  $dr$  and so  $k$  in eq.11) for our later small  $C$  limit neighborhood (sect.3.1). Also since right side extremum  $-1/4 \geq C$  (in  $rel\delta z' = rel \frac{\delta z}{\gamma} = \frac{C_M}{\gamma} =$

$rel \frac{-1 \pm \sqrt{1+4C}}{2} = \frac{dr}{\gamma}$ ) and  $\gamma dt = dt' \neq 0$  so the Hamiltonian (operator) exists and so  $N=0$  observability

(8)Tensor Analysis, Sokolnikoff, John Wiley

(9)The Principle of Relativity, A Einstein, Dover

(10)Quantum Mechanics, Merzbacher, John Wiley

(11) lemniscate circle sequence (Wolfram, Weisstein, Eric)

## Part I FOREWORD (Referencing eq.16 and composite 3e)

Maker's New Pde Implies The Strong Interaction Without A Host of Assumptions

I am writing in support of David Maker's new generalization of the Dirac equation.(New pde)

For example at his  $r=r_H$  Maker's new pde  $2P_{3/2}$  state fills first, creating a 3 lobed shape for  $\psi^*\psi$ .

At  $r=r_H$  the time component of his metric is zero, so clocks slow down, *explaining the stability of the proton*. The 3 lobed structure means the electron (solution to that new pde) spends 1/3 of its time in each lobe, *explaining the multiples of  $1/3e$  fractional charge*. The lobes are locked into the center of mass, can't leave, *giving asymptotic freedom*. Also there are 6  $2P$  states *explaining the 6 quark flavors*.  $P$  wave scattering *gives the jets*. Plus the  $S$  matrix of this new pde gives the  $W$  and  $Z$  as resonances (*weak interaction*) and the Lamb shift but this time without requiring renormalization and higher order diagrams. Solve this new pde with the Frobenius solution at  $r=r_H$  and get the hyperon masses. Note we mathematically *solved* the new pde in each of these cases, *we did not add any more assumptions*. In contrast there are many assumptions of QCD (i.e., masses  $SU(3)$ , couplings, charges, etc.,) versus the one simple postulate of Maker's idea and resulting pde.

Many assumptions are in reality a mere list of properties. One assumption means you actually understand the phenomena.

Dr. Jack Archer  
PhD Physicist

## Concerns the e,v composite Standard electroweak Model and 3e composite

Physics Theories Interconnected In Maker Theory

A cosmologist has probably asked: What is dark energy? What is the source of the dipole moment in CMBR? Why is gravity only attractive? A particle physicist has probably wondered: Why is the core of the SM a left handed Dirac doublet? What is the source of the nuclear force? Is gauge invariance needed? David Maker has derived a generalized Dirac equation that answers

all of these questions. Furthermore, his theory shows that all of these questions are intimately connected.

Dr. Jorge O'Farril PhD  
In Particle Physics Theory

### Physics Implications of the Maker Theory (**Referencing eq.16**)

“People work with a Hamiltonian which, used in a direct way, would give the wrong results, and then they supplement it with these rules of subtracting infinities. I feel that, under those conditions, you do not really have a correct mathematical theory at all. You have a set of working rules. So the quantum mechanics that most physicists are using nowadays is just a set of working rules, and not a complete dynamical theory at all. In spite of that, people have developed it in great detail. “

This sharp criticism of modern quantum field theory is quoted from a talk by Paul Dirac that was published in 1987, three years after his death: see Chapter 15 of the Memorial Volume “Paul Adrian Maurice Dirac: Reminiscences about a Great Physicist”, edited by Behram N.

Kursunoglu and Eugene Paul Wigner (paperback edition 1990). Richard Feynman too felt very uncomfortable with “these rules of subtracting infinities” (renormalization) and called it "shell game" and "hocus pocus" (wikipedia.org “Renormalization”, Oct 2009). Even more recently, Lewis H. Ryder in his text “Quantum Field Theory” (edition 1996, page 390) lamented “there ought to be a more satisfactory way of doing things”.

[The third term in the Taylor expansion of the square root in equation 9  $\gamma^r \sqrt{(\kappa_r)} \partial \psi / \partial r = (\omega/c) \psi$  gives the equation 6.12.10 and so the Lamb shift and equation 8.4 gives anomalous gyromagnetic ratio so we do obtain the QED precision but without the higher order diagrams and infinite charges and masses]

In his highly critical talk Dirac went on to say:

“I want to emphasize that many of these modern quantum field theories are not reliable at all, even though many people are working on them and their work sometimes gets detailed results.” He stressed the fundamental requirement to find a Hamiltonian that satisfies the Heisenberg equation of motion for the dynamic variables of the considered system in order to obtain the correct quantum theory. After all, it was this kind of approach, not invoking the correspondence principle to classical mechanics, that led him to discover the relativistic spinor wave equation of the electron that carries his name! The underlying question here is, of course, how to modify the Hamiltonian of that original Dirac equation to incorporate a dynamical system with electromagnetic fields. As wikipedia.org, under the entry “Dirac Equation”, put it (Oct 2009): “Dirac's theory is flawed by its neglect of the possibility of creating and destroying particles, one of the basic consequences of relativity. This difficulty is resolved by reformulating it as a quantum field theory. Adding a quantized electromagnetic field to this theory leads to the theory of quantum electrodynamics (QED).” But it is just this simple additive modification of the Hamiltonian based on the correspondence principle that violates the Heisenberg equation of motion and, therefore, had been rejected by Dirac.

Dirac concluded his talk with these words:

“I did think of a different kind of Hamiltonian which is in conformity with the Heisenberg equations, but ... it has not led to anything of practical importance up to the present. Still, I like



to mention it as an example of the lines on which one should seek to make advance. ... I shall continue to work on it, and other people, I hope, will follow along such lines. “

Unfortunately, nobody seemed to have listened, instead everybody continued to believe that renormalizing away those awkward infinities is the only available answer and blindly followed in the steps of QED in formulating other quantum field theories, such as those for the weak and the strong forces. This has led to a hodgepodge of complex mathematical acrobatics including the proliferation of string theories for quantum gravity and the attempts to construct a comprehensive matrix string theory (M-theory, supposedly a “theory of everything”), theories that require an unreasonable number of dimensions. Dirac would despair!

But eventually, an outsider has been looking back and took Dirac seriously. Joel David Maker, over the past two decades, has been formulating a new theory totally based on the fundamental principles laid out by Dirac. He was able to derive a new Hamiltonian for the Dirac equation to incorporate the electromagnetic (EM) field. In order to achieve this task, he basically had to create a new general relativity (GR) for the EM force by postulating that there is only one truly fundamental elementary particle, the electron - all other particles are derived from it. Maker expresses this postulate mathematically by a basic EM point source that is an observable quantum mechanical object. He then argues that the equivalence principle for an EM force from such a point source does, in fact, hold, since one has to deal with only one value of charge, namely, the electron charge. Hence, he is able to apply Einstein’s GR formalism to this simple EM point source. A new ambient metric results in which the Dirac equation needs to be imbedded, leading to a modification of the Hamiltonian that is by no means additive but is GR covariant and satisfies the requirement of the Heisenberg’s equation of motion.

Note: [the 3<sup>rd</sup> term in the Taylor expansion of the square root (see 6.12.1(Lamb shift), eq.8.4 (anomalous gyromagnetic ratio) in eq.2 pde  $\gamma^r \sqrt{(\kappa_{rr})} \partial \psi / \partial r = (\omega/c)$  (1.11) contains the high precision QED results otherwise only obtainable by gauges, higher order diagrams and renormalization.]

An important ingredient of this new ambient metric is the existence of an EM Schwarzschild radius for the postulated single point source generating an electron event horizon that is directly related to the classical electron radius. It also leads to the revolutionary concept of fractal event horizons that envelope each other with deep implications for the self-similarity of the physics at different scales. Our observable physics is, however, limited to the region between the electron (more generally, Dirac particle) horizon and the next larger scale horizon, the cosmological horizon. Perturbations from higher-order scales can, however influence observations in our observable region.

Maker’s fundamentally new approach, by including the concept of observability, naturally unifies general relativity with quantum mechanics and makes GR complete (i.e. ungauged), a result, Einstein had been striving for, but was unable to achieve. In addition it provides the precision answers of QED (such as a accurate value of the Lamb shift) and other quantum field theories in a direct way without higher-order Feynman diagrams and/or renormalization. Solutions of the new GR covariant Dirac equation for the region outside the electron event horizon produce the needed physics for EM forces, QED corrections, and weak forces. Solutions for a composite Dirac particle evaluated near its event horizon (which, in a composite system,

needs to be a “fuzzy” horizon and, hence, some inside observation becomes possible) provide an understanding of leptons and hadrons (baryons and mesons) as electronic S,  $2P_{3/2}$  states of the multi-body Dirac particle: For example, S-states are interpreted as leptons, hybrid SP2 states as baryons. Quarks are not separate particles but are related to the three-fold lobe structure of  $2P_{3/2}$  at  $r=r_H$  states in this model, providing an explanation of the strong forces. Gravity is derived, as a first-higher-order effect, from the modification of the ambient EM metric by the self-similar radial expansion dynamics at the cosmological scale. This first-higher-order effect, also provides an understanding of the lepton mass differences; by including the perturbation from the next self-similar larger-scale dynamics (those of a “super cosmos”) the finiteness of neutrino masses are explained as tiny contributions from such a second-higher-order effect. Amazingly, Maker was able to deduce all these results from a basic simple postulate, namely, the existence of a single observable EM point source, which - within the formalism of Einstein’s general relativity - defines a new ambient metric.

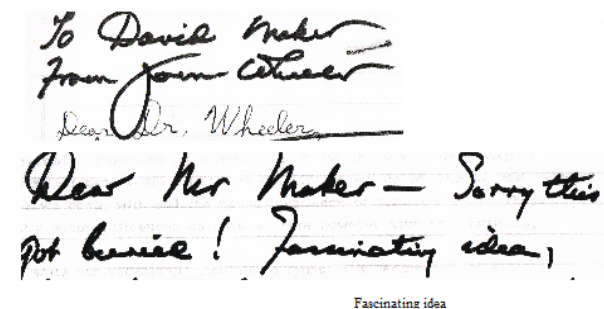
Thus, with his radically new thinking, Maker has proven the correctness of Dirac’s lines of approach to the Hamiltonian problem. Dirac believed in the power of mathematical beauty in the search for a correct description of our observable physical world: “God used beautiful mathematics in creating the world” (thinkexist.com, Oct 2009). Beautiful mathematics it is indeed!

Reinhart Engelmann, Oct 2009

Maker, *Quantum Physics and Fractal Space Time*, volume 19, Number 1, Jan 1999, CSF,  
**Concerns the fractal cosmological implications**

The above reference is a publication in a refereed journal of an article on the universe as a particle in a fractal space time. Here these (fractal) objects are the result of circle mappings onto Z plane Riemann surfaces, separated by nontrivial branch cuts (see preface below). The  $dr+dt$  extrema diagonals on this Z plane translate to pde’s for leptons in the  $ds$  extrema case and for bosons in the  $ds^2 (=dr^2+dt^2)$  extrema case each with its own “wave function”  $\psi$ .

I attended the U.Texas for a while and as a teaching assistant I shared the mailbox rack with people like Weinberg and Archibald Wheeler. So one day on looking over at Wheeler’s a few mailboxes over on an impulse I plopped in a physics paper on this subject. Wheeler responded later in a hand written note that what I had done was a ‘fascinating idea’.



To David Maker  
 From John Wheeler  
 Dear Dr. Wheeler  
 Dear Mr Maker - Sorry this  
 got buried! Fascinating idea,  
 Fascinating idea

He apparently took this fractal idea seriously because 8 years later he organized a seminar at Tufts U. (1990) on a closely related concept: “the wave function of the universe” (the universe in his case as a Wheeler De Witt equation boson wavefunction). Allen Guth and Stephan Hawking also attended.

## Derivation of the New Pde From the Postulate Of 1

Algebraic definition of 1 is  $z=zz$ . Add small constant C

## Table of Contents

**Part I 1U1 Postulate 1**  $\rightarrow z=zz$  (eq.2),  $z'=z'z'+C$ ,  $\delta C=0$  (1),  $z \in \{z'\}$

**Ch.1** Given  $z=zz$  eq.2  $z=1,0$ , initialize iteration of eq.1 with  $z=0=z_0$ , substitute  $z'=1+\delta z$  into eq.1

**Ch.2** 1U1 List-define Math, and eq.1 iteration Mandelbrot set Fractalness

**Ch.3** Quantum mechanics Comes From the  $z'=1+\delta z$  substitution and resulting Lemniscates.

**Ch.4** Equation 16 (Newpde) written in different coordinate systems

**Ch.5** Nearby (fractal) selfsimilar object B, and object C, components of the proton we are inside

**Ch.6** Particle mass from object B and A separation.  $U=e^{iHt}$  used to derive metric quantization

**Ch.7** Comoving coordinate transformation with object A: Cosmological observables, G

**Part II Small C** (is the stable  $2P_{3/2}$  state of Newpde at  $r=r_H$  and is composite 3e) 1U1U1

**Ch.8** Separation Of Variables Of Eq.16 (Newpde): So stable  $2P_{3/2}$  Composite 3e state at  $r=r_H$ .

Paschen Back excited states,  $\Phi=h/2e$ , giving high mass hyperon multiplets

**Ch.9** Frobenius Solution To New PDE perturbs Paschen Back levels, Getting Hyperons

**Part III Outside  $N=-1$  object Mixed State Operators**

**Ch.10** Metric Quantization from  $g_{00}=\kappa_{00}$ , in halos replacing need for dark matter

**A generally covariant *generalization* of the Dirac equation that does not require gauges (Newpde)**

David Maker

This fundamental **Newpde**(3) is derivable, if  $\kappa_{ij}$  is known, from the part between brackets in:  $(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 - \kappa_{tt} dt^2 = ds^2$ . Dirac's 1928 guess of flat space  $\kappa_{xx}=\kappa_{yy}=\kappa_{zz}=\kappa_{tt}=1$  (in his equation(1)) was *not* fundamental since in general space is not flat\*, is curved so generally covariant. A *truly* fundamental  $\kappa_{ij}$  must instead be derived from

the *ultimate* Occam's razor postulate 1 (+C). In fact the (simplest) algebraic definition of 1 is  $z=zz$  (Thus  $z=1,0$ ) and *merely adding constant C* (so  $\delta C=0$ ) most simply in:  $z'=z'z'+C$  (eq.1) does indeed derive that Newpde. To show this note these are unknown Cs except for that single  $C=0$  since  $z=zz+0$  was postulated and so  $z=1,0 \in \{z'\}$ . So you plug **1,0** back into eq.1 for  $z'$ :

$z=0=z_0=z'$  in the iteration of eq.1 using  $\delta C=0$  *generates* the (2D)Mandelbrot set  $C=C_M$  (fig1)

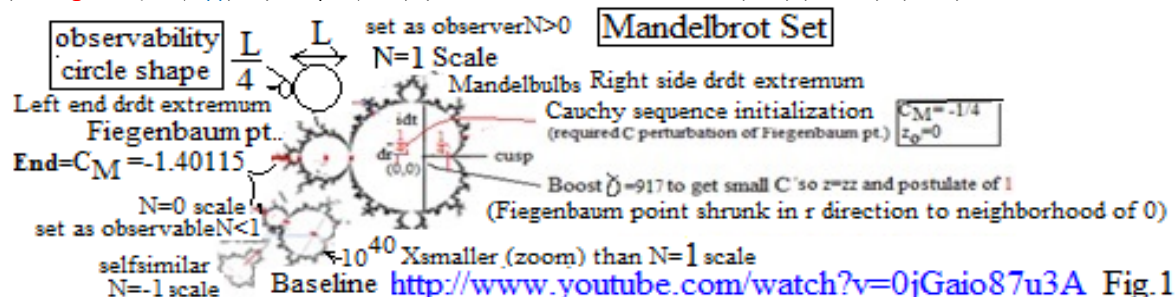
(Need iteration to get all the Cs because of the  $\delta C=0$  (appendix). Note  $10^{40N} C_M$  fractal scales)

$z=1$ ,  $z'=1+\delta z$  substitution into eq.1 using  $\delta C=0$  ( $N>0$  observer) gets eq5 so 2D Dirac eq.(e,v)

(Eq.5 gives the Minkowski (flat space) metric, Clifford algebra  $\gamma^i$  and eq.11 *in one step.*)

These two  $z=1$  and  $z=0$  steps together (appendix) get the curved space  $2D+2D=4D$  **Newpde** (3) and thus the 4D universe, no more and no less. ( $\kappa_{ij}$  (4) from eqs.13,14,15) So just **postulate 1 !!!**

(**Newpde**:  $\gamma^\mu \sqrt{(\kappa_{\mu\mu})} \partial \psi / \partial x_\mu = (\omega/c) \psi$ ,  $\kappa_{00}=1-r_H/r=1/\kappa_{rr}$ ,  $r_H=(2e^2)(10^{40N})/(mc^2)$ .  $N=-1,0,1,..$ fractal)



That  $\kappa_{ij}$  (in the Newpde) also unifies theoretical physics

Note that this new **Newpde**  $\kappa_{ij}$  contains a Mandelbrot set(6)  $e^2 10^{40N}$  Nth fractal scale source(fig1) term(4) that also just happens to successfully **unify** the **Standard electroweak Model** (eg.,the 4 Bosons, eq.12,appendix A) and **Quantum Mechanics** (i.e, Newpde, appendix C) with **General Relativity** (eg.,Schwarzschild metric  $g_{ij}$ ,  $N=-1$ ) which no one has done before. For example:

For  $N=-1$  (i.e., $e^2 X 10^{-40} \equiv G m_e^2$ )  $\kappa_{ij}$  is then by inspection(4) the Schwarzschild metric  $g_{ij}$ ; so we just derived General Relativity and the gravity constant  $G$  from Quantum Mechanics in one lineWow for  $N=0$  the higher order Taylor expansion(terms) of  $\sqrt{\kappa_{ij}}$  gives the anomalous gyromagnetic ratio and Lamb shift *without* the renormalization and infinities (appendix D3): This is very important\* So  $\kappa_{uv}$  provides the general covariance of the Newpde. Eq. 4 even provides us space-time  $r,t$ .

For  $N=1$  (so  $r < r_c$ ) Newpde zitterbewegung expansion stage explains the universe expansion (For  $r > r_c$  it's not observed, per Schrodinger's 1932 paper.).

For  $N=1$  zitterbewegung harmonic coordinates and Minkowski metric submanifold (after long time expansion) gets the De Sitter ambient metric we observe (D16, 6.2).

For  $N=0$  Newpde  $r=r_H$   $2P_{3/2}$  state composite **3e** is the baryons (sect.2, partII) and Newpde  $r=r_H$  composite **e,v** is the 4 Standard electroweak Model Bosons (4 eq.12 rotations→appendixA)

So we got all physics here by *mere inspection* of this (curved space) Newpde with no gauges!

## References

(1)  $\gamma^\mu \partial \psi / \partial x_\mu = (\omega/c) \psi$

(2)Spherical symmetry:  $(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 - \kappa_{tt} dt^2 = ds^2$   
 $\kappa_{xx} = \kappa_{yy} = \kappa_{zz} = \kappa_{tt} = 1$  is flat space, Minkowski, as in his Dirac equation(1).

(3) Newpde:  $\gamma^\mu \sqrt{(\kappa_{\mu\mu})} \partial \psi / \partial x_\mu = (\omega/c) \psi$  for **e,v**. So we didn't just drop the  $\kappa_{\mu\nu}$  (as is done in ref.1)

(4) Here  $\kappa_{oo} = 1 - r_H/r = 1/\kappa_{rr}$ ,  $r_H = (2e^2)(10^{40N})/(mc^2)$ . The  $N = \dots -1, 0, 1, \dots$  fractal scales (eqs.13,14,15)

(5) Penrose in a utube video implied that the Mandelbrot set might contain physics. Here we merely showed how to find it. For example the (fractal Mandelbulb neighborhood area  $|drdt| > 0$  of the) Feigenbaum point is a subset (containing that  $10^{40N}$  Xselfsimiilar scale jump: Fig1)

\* I found that there is a problem with the 1928 Dirac equation(1). In (spherical symmetry):

$(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 - \kappa_{tt} dt^2 = ds^2$  (1)

Dirac set  $\kappa_{xx} = \kappa_{yy} = \kappa_{zz} = \kappa_{tt} = 1$  so flat space(2) in his equation(1) when we know in general space is not flat, there are forces. So over the past 100 years (since 1928, ref.1) people have had to try to make up for that(flat space) mistake by adding ad hoc convoluted gauge force after gauge force until fundamental theoretical physics became a mass of confusion, a train wreck, a junk pile. So all they can do for ever and ever is to rearrange that junk pile Dirac noticed this too and even, toward the end of his life, tried his hand at *fixing*  $\kappa_{ij}$ . See Chapter 15 of the Memorial Volume “Paul Adrian Maurice Dirac: Reminiscences about a Great Physicist”, edited by Behram N. Kursunoglu and Eugene Paul Wigner. There Dirac mentions ”a different kind of Hamiltonian” which indeed would change  $\kappa_{ij}$ . Richard Feynman too felt very uncomfortable with “these rules of subtracting infinities” (renormalization, yet another unfortunate consequence of setting  $\kappa_{ii} = 1$ ) and called it a "shell game" and "hocus pocus, “Renormalization”, Oct 2009). Even more recently, Lewis H. Ryder in his text “Quantum Field Theory” (edition 1996, page 390) lamented “there ought to be a more satisfactory way of doing things”.

Well, we found it here: The  $N=0$  higher order Taylor expansion terms(4) in  $\sqrt{\kappa_{ij}}$  gives the anomalous gyromagnetic ratio and Lamb shift *without* the renormalization and infinities (appendix D3). It is of tremendous value to QM to not require renormalization anymore anywhere and yet still get those well known high precision (qed) quantitative results from a mere Taylor expansion(D4). This result, and that ultimate Occam's razor single postulate, creates

a new paradigm that sets us back on course of seeking fundamental theoretical physics again (i.e., **postulate 1**).

**Occam's Razor Implies Postulate 1:** Postulate 1 is the simplest idea imaginable. 1 (in  $1=1X1$ ) is thereby the *ultimate* application of Occam's razor since 0 (also in  $z=zz$ ) postulates literally *nothing*. Also  $z=zz$  is 'simpler' than  $z=zzzz$  and  $z'=z'z'+C$  is simpler than  $(z'+C)=(z'+C)z'+C$ .

### I Newpde from **Postulate 1 (observable) and prove observability**

You would think just postulating 1 is nonsense. That can't lead anywhere, right? But it does! The (simplest) algebraic definition of 1 is  $z=zz$  (Thus  $z=1,0$ ) and *merely adding constant C* (so  $\delta C=0$ ) most simply in  $z'=z'z'+C$  (**eq.1**) derives the Newpde and so physics. To show this note these are unknown Cs except for that single  $C=0$  since  $z=zz+0$  was postulated and so  $z=1,0 \in \{z'\}$  so that:

$z=0 = z_0 = z'$  in the iteration of **eq.1** using  $\delta C=0$  *generates* the (2D)Mandelbrot set  $C=C_M=\text{end}^{**}$

(Need iteration to get all the Cs because of the  $\delta C=0$  (appendix),  $\text{end}=10^{40N}X$  fractal scales)

$z=1$ ,  $z'=1+\delta z$  substitution into **eq.1** using  $\delta C=0$  ( $N>0$  observer) gets eq5 so 2D Dirac eq.(e,v)

(Eq.5 gives the Minkowski (flat space) metric, Clifford algebra  $\gamma^i$  and eq.11 *in one step*.)

These two  $z=1$  and  $z=0$  steps together (appendix) get the curved space  $2D+2D=4D$  **Newpde** (3) and thus the 4D universe, no more and no less .

So just **postulate 1 !!!**

### Summary

All I did here is to (postulate 1 and) **prove observability**: Eq.11:  $p_x \psi = -i\hbar \partial \psi / \partial x$  is the well known *observables* (p) definition,  $\psi$  is from **Newpde**(3). C is merely the *required observer*! Note also eq.11 *real number* eigenvalue observability (eg., dr noise) derived from our right side  $-1/4$  initiated Cauchy sequence(7), Ch.2, =reals: our Mandelbrot set iteration sequence there!

Therefore  $N=0$  **postulate 1** can also be used in a list-define math to get the *real number* algebra (without all those many Rel#math axioms). Eg.,  $1 \cup 1 \equiv 1+1$  (B2, Ch.2). So we get both the physics (See ref.5) AND (rel#)mathematics from ONE postulate1, everything! We finally figured it out!

### Compare and contrast

The core of mainstream physics is the Standard electroweak Model (SM) that gives us important results like Maxwell's equations and weak interaction theory that explain electricity and magnetism and some radioactive decays respectively. Add to that QCD that explains the nuclear

We square eqs.7,8,9  $ds_1^2=(dr+dt)(dr+dt)=(-dr-dt)(-dr-dt)=[dr^2+dt^2] +(\textcolor{blue}{drdt}+\textcolor{blue}{dtdr})$   
 $\equiv ds^2+ds_3=ds_1^2$ . Since  $ds_3$  (is max or min) and  $ds_1^2$  (from eq.7,8,9) are invariant then so is **Circle**



$ds^2=dr^2+dt^2=ds_1^2-ds_3$ , also implying the rest of the Clifford algebra  $\gamma^i\gamma^i=1$  in eq.7a, no sum on 'i' and also the lemniscate formulation(fig.7). Note this separate ds is a minimum at  $45^\circ$  given the eq.7 constraints and so Circle $\equiv\delta z=dse^{i\theta}=dse^{i(\Delta\theta+\theta_0)}=dse^{i((\cos\theta dr+\sin\theta dt)/(ds)+\theta_0)}$ ,  $\theta_0=45^\circ$ . ( $\delta z$  in fig.6). We define  $k\equiv dr/ds$ ,  $\omega\equiv dt/ds$ ,  $\sin\theta\equiv r$ ,  $\cos\theta\equiv t$ .  $dse^{i45^\circ}\equiv ds$ . Take ordinary derivative dr (since flat

space) of 'Circle'  $\frac{\partial(dse^{i(\frac{rdr}{ds}+\frac{tdt}{ds})})}{\partial r} = i \frac{dr}{ds} \delta z$  so  $\frac{\partial(dse^{i(rk+wt)})}{\partial r} = ik\delta z$ ,  $k\delta z = -i \frac{\partial\delta z}{\partial r}$  (11).

( $\langle F \rangle^* = \int (F\psi)^* \psi d\tau = \int \psi^* F\psi d\tau = \langle F \rangle$  Hermitian) from right side real number Cauchy seq.starting at  $-1/4$  iteration case of the Mandelbrot set iteration(7), Ch.2,sect.2, with small C limit making real eigenvalues (eg.,noise) likely. The observables  $dr \rightarrow k \rightarrow p_r$  condition gotten from eq.11 **operator formalism**(10) thereby converting eq.7-9 into Dirac eq. pdes (Circle solution also implies lemniscates, fig.7, so fig.1 observability). Cancel that  $e^{i45^\circ}$  coefficient ( $45^\circ=\pi/4$ ) then multiply both sides of eq.11 by  $\hbar$  and define  $\delta z \equiv \psi$ ,  $p \equiv \hbar k$ . Eq.11 becomes the familiar

$$p_r \psi = -i\hbar \frac{\partial\psi}{\partial r} \quad (11)$$

Repeat eq.3 for  $\tau$ ,  $\mu$  respective  $\delta z$  lobes in fig.6 so they each have their own neutrino  $\nu$ .

**\*\*end**  $\delta C = \left(\frac{\partial C}{\partial r}\right)_t dr + \left(\frac{\partial C}{\partial t}\right)_r idt = 0$ . For those 4X circles (so eq.11 observables) in fig1

$N=0$ , eq.3,  $C \approx \delta z' = dse^{i\theta}$ . Furthermore if  $\theta=0$ ,  $dse^{i\theta} \equiv ds = dC (=dr)$  we additionally have the required *Real* eigenvalues for  $dr/ds$  observable in eq.11a. making  $\left(\frac{\partial C}{\partial r}\right)_t dr = 0$  only at the

Fiegenbaum point= $F^x=(-1.40115, i0)=C_M \equiv \text{end}$  since there  $\partial r \approx dr \approx 0$  and  $\partial C/\partial r = \text{constant}$  for these 4X circles. Note if a circle (or many circles) is rotated (U), translated (D), shrunk (S) equally in both dimensions (i.e.,  $(\partial x^j/\partial x^k) f^j = f^k \equiv \begin{bmatrix} f_{1N} \\ f_{2N} \end{bmatrix} = S_N \begin{bmatrix} U_{11} & U_{12} \\ U_{21} & U_{22} \end{bmatrix} \begin{bmatrix} f \\ 0 \end{bmatrix} + \begin{bmatrix} D_{1N} \\ D_{2N} \end{bmatrix}$ ) it is still a circle, eq.11 still holds, so *it's still an observable* as seen in the N fractal scale zoom. Thus you can pick out from that zoom these fig.1 Mandelbrot set 4Xdiameter circles as the only **observables** geometry in all that clutter so we get for that 'end' point:  $S_N C_M = 10^{40N} C_M$  in the eq.13.

## **z=1,z=0 steps together** (on Circle with small C boost)

**Postulate1** also implies a small C in eq.1 which thereby implies a (Minkowski metric Lorentz contraction(9))  $1/\gamma$  boosted frame of reference in the eq.3  $C=C_M/\gamma \equiv C_M/\xi_1 = \delta z' = \Delta$  for next small smaller fractal scale  $N_{ob}<0$  so  $\delta z' \ll 1$  (composite 3e: sect.2 and PartII). Also recall  $\delta ds^2=0$  in eq.5. For  $N=0$  eq.5 (which is true only for  $N>0$ ) and so eq.7 is not quite true (and  $\delta z$  in eq.11 perturbed). But  $\delta C = \delta ds = 0$  (since imaginary extremum  $=0$ ) is still true so we must have an angle perturbation of big  $N=1$   $dr, dt$  for  $\theta_0=45^\circ$  on above **ds Circle** and so a slightly modified eq.7

$$(dr-\delta z')+(dt+\delta z') \equiv dr'+dt'=ds \quad (12)$$

## **N=1,N=0 extremum rotations**

Since (eq.12)  $dr, dt$  is the (eq.11) observer  $N_{\text{observer}}>0$  scale then  $\delta z'$  defines the  $N_{ob}=0$  object. Also the  $r, t$  axis' are the max extremum for  $ds^2$ , and the  $ds^2$  at  $45^\circ$  is the min extremum  $ds^2$  so  $\Delta\theta=\theta \text{ modulo } 45^\circ$  is pinned to an axis' so extreme  $\Delta\theta \approx \pm 45^\circ = \delta z'$ . So in eq.12 the 4 rotations  $45^\circ+45^\circ=90^\circ$  define 4 Bosons (appendix A), and  $45^\circ-45^\circ=0$  eq.7-9 defines leptons. Again, for  $N_{ob}<0$ , you also have other (smaller) fractal scale extreme  $\delta z'$  (eg.,tiny Fiegenbaum pts so  $N=1$   $dr=r$ , for  $N=0$ ) so metric coefficient  $\kappa_r \equiv (dr/dr')^2 = (dr/(dr-(C_M/\xi_1)))^2 = 1/(1-r_H/r)^2 = A_1/(1-r_H/r) + A_2/(1-r_H/r)^2$ . The partial fractions  $A_i$  can be split off from RN and so  $\kappa_r \approx 1/[1-((C_M/\xi_1)r)]$  (13) ( $C_M$  defined to be  $e^2$  charge,  $\gamma \equiv \xi_1$  mass). So:  $ds^2 = \kappa_r dr'^2 + \kappa_{oo} dt'^2$  (14)

$$\text{From eq.7a } dr'dt'=\sqrt{\kappa_{rr}}dr'\sqrt{\kappa_{00}}dt'=drdt \text{ so } \kappa_{rr}=1/\kappa_{00} \quad (15)$$

We can then do a rotational dyadic coordinate transformation of  $\kappa_{\mu\nu}$  to get the Kerr metric which is all we need for our GR applications(9). So from eqs.4,5,14,15 we found the relation between  $x_i, x_j$  pairs:  $(\sum_{i=1}^2 \gamma^i \sqrt{\kappa_{ii}} dx_i)^2 = \sum_{i=1}^2 \kappa_{ii} d^2 x_i$  (14a). So given this added 2D  $\Delta$  perturbation we get curved space  $2D \otimes 2D = 4D$  independent  $x_1, x_2 \rightarrow x_1, x_2, x_3, x_4$ . Also assuming orthogonality  $dr^2 = dx_1^2 + dx_2^2 + dx_3^2$  (as  $r \rightarrow \infty$  in eq.13,15) the right side of eq.14a therefore has the 2 in the sum replaced by a 4 implying the left side then has to be in eq.14a for the 2D form to be a special case (of any 2  $x_i x_j$ ) in B2: Imposing orthogonality thereby creates 6 pairs of eqs.4&5. So eq.14a becomes:  $(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 - \kappa_{tt} dt^2 = ds^2$ . Multiplying the bracketed term by  $1/ds$  & unknown  $\delta z \equiv \psi$  so eq 11 implies 4D Newpde:

$$\gamma^\mu (\sqrt{\kappa_{\mu\mu}}) \partial \psi / \partial x_\mu = (\omega/c) \psi \text{ for } e, \nu, \kappa_{00} = 1 - r_H/r = 1/\kappa_{rr} \quad r_H = e^2 X 10^{40N}/m \quad N(= -1, 0, 1), \quad (16)$$

$= C_M/\gamma$  (from sect.2)  $C_M = \text{Fiegebaum point}$ . So: **postulate 1**  $\rightarrow$  Newpde. syllogism

\*Need small C boost for  $z=zz$  so postulate1 It is created by Newpde  $r=r_H$   $2P_{3/2}$  stable state P, sect2 The 4 eq.12 Newpde  $e, \nu$  rotations at  $r=r_H$  are the 4  $W^+, \gamma, W^-, Z_0$  SM Bosons (appendixA

So Penrose's intuition(6) was right on! There *is* physics in the Mandelbrot set, all of it.

**2 N=0 Small C boost circle observables.** Note that **real** component of eq.5 is Minkowski metric implying possible Lorentz transformation Fitzgerald contraction  $C/\gamma$  boosted C frames of reference. From eq.3 for  $N=0: C \approx \delta z$  and  $C \rightarrow C/\gamma = C_M/\gamma \equiv C_M/\xi$ . So from eq.3 for  $N=0$  in eq.12  $C_M/\xi = \delta z$  (eq.17)

$(C_M/\xi = \delta z \delta z \text{ for } N=1)$ . So  $\delta C_M = 0 = \delta \delta z \xi + \delta \xi \delta z = 0$  ( $N=0$ ). If  $\mathbf{z}=0$  then  $\delta z' = -1$  is big for  $N=0$ . In  $\delta C_M = 0 = \delta \delta z \xi + \delta \xi \delta z = 0$  for  $\xi$  small then  $\delta \xi$  has to be small and so  $\xi$  is stable, electron  $\xi_0 = \Delta \epsilon = \epsilon$ . for  $\mathbf{z}=1$  then  $\delta z$  is small on  $N=0$  thus  $\delta \xi$  and  $\xi$  are both big so unstable and large mass For  $N=0$  observable  $\xi = 10^{40N} \xi$ : the subatomic observable cosmos. The Laplace Beltrami method (D4),  $N>1$  applies to observation of the huge  $r_H$  cosmological objects. ( $N=1$  is what it is).

**N=1 small C boost so postulate observable 1 (e)** Recall the Mandelbrot set in small C boost  $C_M = \xi C$  sect.2. From eq.3  $\delta z + \delta z \delta z = C$  or observer  $N=1$   $\delta z \delta z = C$ . The  $68.7^\circ$  is from eq3 quadratic equation at the Fiegebaum point.  $45^\circ$  from minimum  $ds^2$ .  $\mu$  then is not a constant in time because of eq.12 angle New pde zitterbewegung contribution to the  $\delta z$  chord perturbation of the  $45^\circ$ . The observer limaçon is the electron  $e$ , the  $45^\circ$  intersection chord with that Mandelbulb is  $\mu$  ( fig6 below.). The  $68.74^\circ$  tiny Mandelbulb is the tauon. But what if we constructed instead from the limaçon 'e' composite  $3e$   $2P_{3/2}$  state at  $r=r_H$  requiring a mass constraint of  $2m_p \geq \text{mass}$  of the respective Hund rule free particle  $2S_{1/2}$  ( $\equiv$  the tauon  $\tau$ ) plus  $1S_{1/2}$  ( $\equiv$  muon  $\mu$ ) states? The reduced mass is then the proton that then also generates the  $\gamma$  boost on the  $m_e$  s that gives us that small C and the **postulate 1** (observable e).



$1.4011/\gamma$  shrinks a lot but time  $\times 10^{-40}\gamma$  doesn't get much bigger since it was so small to begin with at the Feigenbaum point. Eq.1 then means we have Occam's razor optimized **postulated 1**. Given the New pde  $r_H$  we only see the  $r_H = e^2 10^{40N}/m$  sources from our  $N=0$  observer baseline. We never see the  $r < r_H$  <http://www.youtube.com/watch?v=0jGaio87u3A> which explores the Mandelbrot set interior near the Feigenbaum point. The splits are in 3 directions from the orbs. There appear to be about 2.5 splits going by each second (given my PC baud rate) and the next Mandelbrot set comes up in about 62 seconds. So  $3^{2.7 \times 62} = 10^N$  so  $172 \log 3 = N = 82$ . So there are  $10^{82}$  splits. So there are about  $10^{82}$  splits per initial split. But each of these Mandelbrot set Feigenbaum points is a  $C_M/\xi \equiv r_H$  in electron (eq.13 above). So for each larger electron there are  **$10^{82}$  constituent electrons**. Also the scale difference between Mandelbrot sets as seen in the zoom is about  **$10^{40}$ , the scale change** between the classical electron radius and  $10^{11} ly$  giving us our fractal universe.

Recall again we got from eq.3  $\delta z + \delta z \delta z = C$  with quadratic equation result:

$\delta z = \frac{-1 \pm \sqrt{1-4C}}{2}$ . is real for noise  $C < 1/4$  creating our noise on the  $N=1$  th fractal scale. So  $1/4 = (3/2)kT/(m_p c^2)$ . So  $T$  is 20MK. So here we have *derived the average temperature of the universe* (stellar average). That  $z' = 1 + \delta z$  substitution also introduces Lorentz transformation rotational and translation noise that does not effect the number of splits, analogous to how a homeomorphism does not change the number of holes (which is a Topological invariant). So the excess  $C$  noise (due to that small  $C'$  boost) causes the Feigenbaum point neighborhood internal structure to become randomized (as our present universe is) but the number of electrons ( $10^{82}$ ) remains invariant. See appendix D mixed state case2 for further organizational effects.  $N = r^D$ . So the **fractal dimension**  $= D = \log N / \log r = \log(\text{splits}) / \log(\#r_H \text{ in scale jump}) = \log 10^{80} / \log 10^{40} = \log(10^{40})^2 / \log(10^{40}) = 2$ . (See appendix E for Hausdorff dimension & measure) which is the same as the 2D of eq.4 and the Mandelbrot set. The next smaller (subatomic) fractal scale  $r_1 = r_H = 2e^2/m_e c^2$ ,  $N=0$ th,  $r_2 = r_H = 2GM/c^2$  is defined as the  $N=1$ th where  $M = 10^{82} m_e$  with  $r_2 = 10^{40} r_1$  So the Feigenbaum pt. gave us a lot of physics: eg. **#of electrons in the universe; the universe size, temp.**

**2.3 Results:** What makes this all work is (**Postulate 1**  $\rightarrow$  Newpde). Postulate **1** is the simplest idea imaginable: a Occam's razor *optimized* theory. We *also* get the *actual* physics with the Newpde (Therefore the usual postulating of hundreds of Lagrange densities, free parameters, dimensions ,etc., is senseless.).

For example (appendixC) Newpde **composite 3e**  $2P_{3/2}$  at  $r=r_H$  is the proton: That B flux quantization(C3) implies a big proton mass implying high speed  $\gamma=917$  positrons and so the Fitzgerald **contracted E field lines are the strong force**: we finally understand the strong force! So these two positrons then have big mass *two body* motion(partII) so **ortho(s,c,b) and para(t) excited (multiplet) states** understood. Eq.12 implies **Composite e,v** at  $r=r_H$  is **the electroweak SM** (appendixA) **Special relativity** is that Minkowski result. **With the Eqs.16  $\psi$**  (sect.B3) **we finally understand Quantum Mechanics** for the first time and eq.4 **gave us a first principles derivation of r,t space-time** for the first time. That Newpde  $\kappa_{\mu\nu}$  metric (In eq.14), on the  $N=-1$  next smaller fractal scale(1) so  $r_H = 10^{-40} 2e^2/m_e c^2 \equiv 2Gm_e/c^2$ , is the Schwarzschild metric since  $\kappa_{00} = 1 - r_H/r = 1/\kappa_{rr}$  (15): we **just derived General Relativity(gravity) from quantum mechanics in one line**. The Newpde zitterbewegung expansion component ( $r < r_C$ ) on the next larger fractal scale is the universe expansion: **we just derived the expansion of the universe in one line**. The Newpde appendix C derivation of those precision QED values (eg.,Lamb shift sect.C1) allow us

## Real# Mathematics from Postulate 1

The postulate 1 also gives the *list-define* math (B2) *list* cases  $1 \cup 1 \equiv 1 + 1 \equiv 2$ , *define*  $a = b + c$  (So no other math axioms but 1.) and Cauchy sequence proof (2) of real number eigenvalues (sect.2.1) from the Mandelbrot set iteration formula. That means the **mathematics and the physics** come from (**postulate 1**  $\rightarrow$  **Newpde**): *everything*. Recall from eq.7 that  $dr + dt = ds$ . So combining in quadrature eqs 7 & 11  $SNR \delta z ((dr/ds + dt/ds) \delta z = ((dr + dt)/ds) \delta z = (1) \delta z$  (11a, appendF) and so having come *full circle* back to postulate 1 as a real eigenvalue ( $1 \equiv$  Newpde electron). So we really do have a binary physics signal. So, having come *full circle* then:

### Mathematical Notion (of postulate 1 $\Leftrightarrow$ Newpde)





## Intuitive Notion (of postulate 1 $\leftrightarrow$ Newpde)

The Mandelbrot set introduces that  $r_H = C_M/\xi_1$  horizon in  $\kappa_{00}=1-r_H/r$  in the Newpde, where  $C_M$  is fractal by  $10^{40}$ Xscale change(fig.2) So we have found ([davidmaker.com](http://davidmaker.com)) that: Given that fractal selfsimilarity astronomers are observing from the inside of what particle physicists are studying from the outside, that **ONE** New pde e electron  $r_H$ , **one** thing (fig.1). *Everything* we observe big (cosmological) and small (subatomic) is then that (New pde)  $r_H$ , even baryons are composite 3e. So we understand, *everything*. This is the only Occam's razor optimized first principles theory **Summary**: So instead of doing the usual powers of 10 simulation we do a single power of  $10^{40}$  simulation and we are immediately back to where we started! Think about that as you gaze up into a star filled sky some evening! We really then understand how there could ONE object (that we postulated).

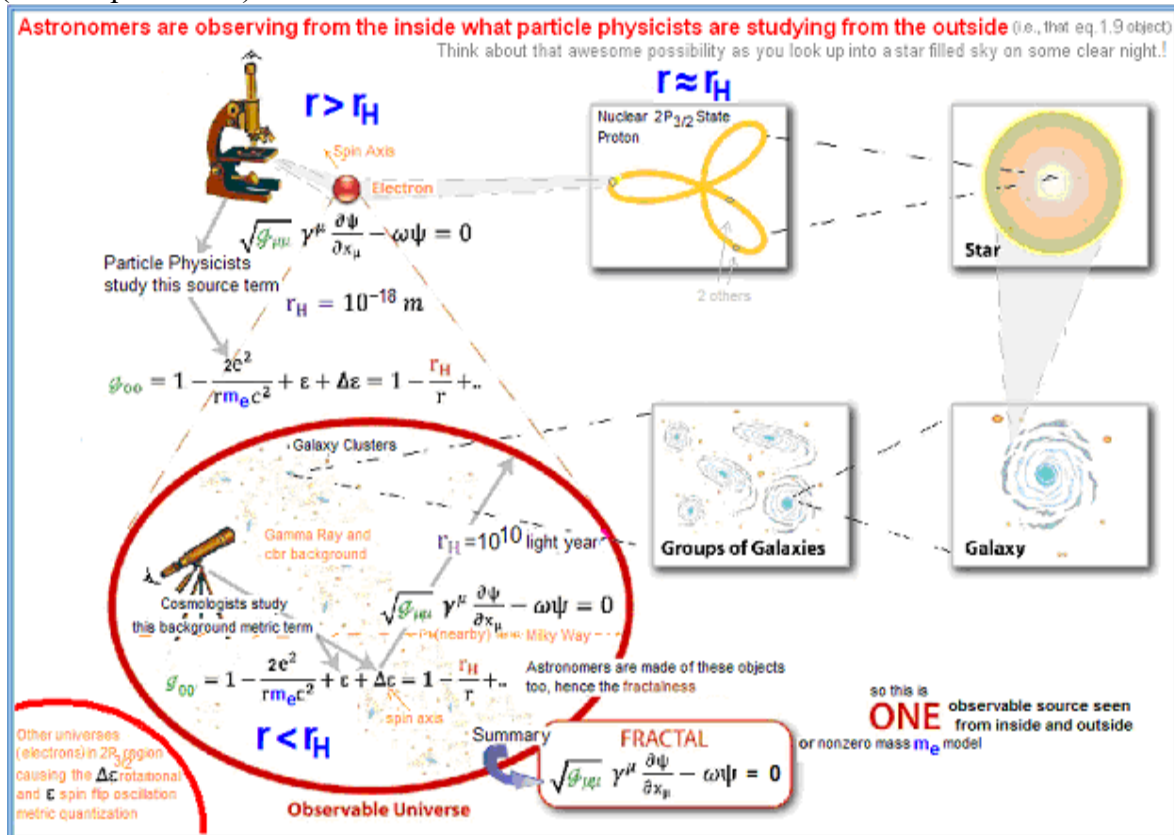


fig2

(↑lowest left corner) Object B caused perturbation structure jumps: void→galaxy→globular,,etc.

## References

- (6) Penrose in a utube video implied that the Mandelbrot set might contain physics. Here we merely showed how to find it. For example the (fractal Mandelbulb neighborhood area  $|drdt|>0$  of the) Fiegenbaum point is a subset (containing that  $10^{40}$ Xselfsimiilar scale jump: Fig1)
- (7) Cantor: Ueber die Ausdehnung eines Satzes aus der Theorie der trigonometrischen Reihen, "Ueber eine elementare Frage der Mannigfaltigkeitslehre" Jahresbericht der Deutschen Mathematiker-Vereinigung." Mandelbrot set iteration sequence  $z_n$   $C_M=-1/4$ ,  $z_0=0$  same as Cauchy seq. since it begins with rational number  $-1/4$ , allowing the ( $C'$  uncertainty)  $dr$  neighborhood of 0 to have a nonzero probability of being a real number and thereby giving real eigenvalues to the equation 11 operator formalism after the small  $C'$  boost to get observability around  $dr=0$ .Sect.3.1.



## Appendix A: $z=0$ , $N=0$ (composite $e, \nu$ at $r=r_H$ from eq.12)

The New pde also has an associated field theory coming out of eq.12 implications with  $z=0$  so large  $\delta z'$  angle ( $++45^\circ$  extremum, sect.1) $=\theta$ . Since observer  $N>0$ , so arbitrarily large  $\theta \propto \delta z \gg 1$  so  $\Delta\theta = \theta \text{ Modulo } 45^\circ$ . Here all four  $\Delta\theta \pm 45^\circ \times 2$  rotations of **Composite  $e, \nu$**  implied by eq.12.

### A1 I $\rightarrow$ II, II $\rightarrow$ III, III $\rightarrow$ IV, IV $\rightarrow$ I rotations in eq.7-9 plane Give SM Bosons

For  $z=0$   $\delta z'$  is big in  $z=1+\delta z$  and so we have again  $\pm 45^\circ$  min ds and so two possible  $45^\circ$  rotations so through a total of two quadrants for  $\pm \delta z'$  in eq.12. Note in fig.3  $dr, dt$  is also a rotation and so has eq.11 rotation operator  $\theta$  observable. Thus from equation 11 for  $(\theta)$  angle rotations  $\theta \delta z = (dr/ds) \delta z = -i \partial(\delta z) / \partial r$  for the first  $45^\circ$  rotation. So we got through one Newpde derivative for each  $45^\circ$  rotation. For the next  $45^\circ$  rotation in fig.4 it is then a second derivative  $\theta \theta \delta z' = e^{i\theta} e^{i\theta} \delta z = e^{i(\theta+\theta)} \delta z = (dr/ds)((dr/ds)dr) = -i \partial(-i \partial(dr)) / \partial r \partial r = -\partial^2(dr) / \partial r^2$  large angle rotation in figure 3. For  $z=1$ ,  $\delta z'$  small so  $45^\circ$ - $45^\circ$  small angle rotation in figure 3. Do the same with the time  $t$  and get for  $z=0$  rotation of  $45^\circ+45^\circ$  t (fig.4) then  $\theta \theta \delta z' = (d^2/dr^2)z' + (d^2/dt^2)z'$  (A1)

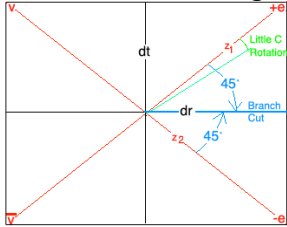


fig.3. for  $45^\circ$ - $45^\circ$  eq.16 case: leptons

So  $\Delta S = 1/2 + 1/2 = 1$  or  $1/2 - 1/2 = 0$ . So  $\Delta S = 1/2 + 1/2 = 1$  making 2 body (at  $r=r_H$ )  $S=1$  Bosons. Note we also get these Laplacians characteristic of the Boson field equations by those  $45^\circ+45^\circ$  rotations so eq.16 implies Bosons accompany our leptons (given the  $\delta z'$ ), so these leptons exhibit “force”.

### A3 Newpde $r=r_H$ , $z=0$ , $45^\circ+45^\circ$ rotation of composites $e, \nu$ implied by Equation 12

So  $z=0$  allows a large  $C$   $z$  rotation application from the 4 different axis' max extremum (of eq.16) branch cuts gives the 4 results:  $Z, +, -W$ , photon bosons of the Standard Model. So we have derived the Standard Model of particle physics in this very elegant way (from the four axis'). You are physically at  $r=r_H$  if you rotate through the electron quadrants (I, IV). of eq.7-9.. So we have large  $C_M$  dichotomic  $90^\circ$  rotation to the next Reimann surface of eq.12, eq.A1  $(dr^2+dt^2)z''$  from some initial extremum angle(s)  $\theta$ . Eq.12 solutions imply complex 2D plane Stern Gerlach dichotomic rotations using eq.A1 thereby using Pauli matrices  $\sigma_i$  algebra, which maps one-to-one to the quaternionA algebra. Using eq.12 we start at some initial angle  $\theta$  and rotate by  $90^\circ$  the noise rotations are:  $C=z'' = [e_L, \nu_L]^T \equiv z'(\uparrow) + z'(\downarrow) \equiv \psi(\uparrow) + \psi(\downarrow)$  has a eq.12 infinitesimal unitary generator  $z'' \equiv U = 1 - (i/2)\epsilon n \cdot \sigma$ ,  $n \equiv \theta/\epsilon$  in  $ds^2 = U^\dagger U$ . But in the limit  $n \rightarrow \infty$  we find, using elementary calculus, the result  $\exp(-(i/2)\theta \cdot \sigma) = z''$ . We can use any axis as a branch cut since all 4 are eq.16 large extremum so for the 2<sup>nd</sup> rotation we move the branch cut  $90^\circ$  and measure the angle off the next diagonal since Pauli matrix dichotomic rotations are actually axis rotations, leaving our  $e$  and  $\nu$  directions the same. In any case  $(dr+dt)z''$  in eq.16 can then be replaced by eq.A1  $(dr^2+dt^2+..)z'' = (dr^2+dt^2+..)e^{\text{quaternionA}}$  Bosons because of eq.A1. Then use eq. 12 to rotate:  $z''$ :

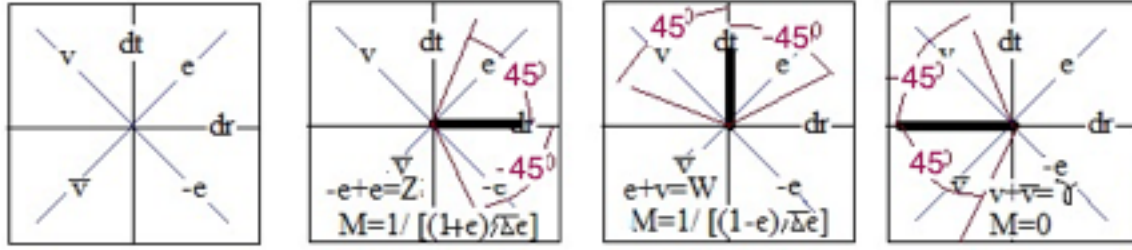


fig4

Fig.4 applies to eq.9  $45^\circ+45^\circ=90^\circ$  case: **Bosons**. These quadrants were defined in eq.7-9 and used in eq.12. The Appendix A4 derivation applies to the far right side figure. Recall from eq.12  $z=0$  result  $C_M=45^\circ+45^\circ=90^\circ$ , gets Bosons.  $45^\circ-45^\circ=$  leptons. The  $\nu$  in quadrants II (eq.5) and III (eq.9).  $e$  in quadrants I (eq.7) and IV (eq.7). Locally normalize out  $1+\varepsilon$  (appendix D). For the **composite  $e,\nu$**  on those required large  $z=0$  eq.9 rotations for  $C \rightarrow 0$ , and for stability  $r=r_H$  (eg., for  $2P_{1/2}$ ,  $I \rightarrow II$ ,  $III \rightarrow IV$ ,  $IV \rightarrow I$ ) unless  $r_H=0$  ( $II \rightarrow III$ ) Example:

**A4 Quadrants II  $\rightarrow$  III rotation** eq.A2  $(dr^2+dt^2+...)e^{\text{quaternion } A} = \text{rotated through } C_M$  in eq.16.

example  $C_M$  in eq.A1 is a  $90^\circ$  CCW rotation from  $45^\circ$  through  $\nu$  and antiv

$A$  is the 4 potential. From eq.9b we find after taking logs of both sides that  $A_0=1/A_r$  (A2)

Pretending we have a only two  $i,j$  quaternions but still use the quaternion rules we first do the  $r$

derivative: From eq. A1  $dr^2\delta z = (\partial^2/\partial r^2)(\exp(iA_r+jA_0)) = (\partial/\partial r)[(i\partial A_r/\partial r + \partial A_0/\partial r)(\exp(iA_r+jA_0))] = \partial/\partial r[(\partial/\partial r)iA_r + (\partial/\partial r)jA_0](\exp(iA_r+jA_0)) + [i\partial A_r/\partial r + j\partial A_0/\partial r]\partial/\partial r(\exp(iA_r+jA_0)) + (i\partial^2 A_r/\partial r^2 + j\partial^2 A_0/\partial r^2)(\exp(iA_r+jA_0)) + [i\partial A_r/\partial r + j\partial A_0/\partial r][i\partial A_r/\partial r + j\partial/\partial r(A_0)] \exp(iA_r+jA_0)$  (A3)

Then do the time derivative second derivative  $\partial^2/\partial t^2(\exp(iA_r+jA_0)) = (\partial/\partial t)[(i\partial A_r/\partial t + \partial A_0/\partial t)$

$(\exp(iA_r+jA_0))] = \partial/\partial t[(\partial/\partial t)iA_r + (\partial/\partial t)jA_0](\exp(iA_r+jA_0)) + [i\partial A_r/\partial t + j\partial A_0/\partial t]\partial/\partial t(\exp(iA_r+jA_0)) + (i\partial^2 A_r/\partial t^2 + j\partial^2 A_0/\partial t^2)(\exp(iA_r+jA_0)) + [i\partial A_r/\partial t + j\partial A_0/\partial t][i\partial A_r/\partial t + j\partial/\partial t(A_0)] \exp(iA_r+jA_0)$  (A4)

Adding eq. A2 to eq. A4 to obtain the total D'Alambertian  $A3+A4=$

$[i\partial^2 A_r/\partial r^2 + i\partial^2 A_r/\partial t^2] + [j\partial^2 A_0/\partial r^2 + j\partial^2 A_0/\partial t^2] + ii(\partial A_r/\partial r)^2 + ij(\partial A_r/\partial r)(\partial A_0/\partial r) + ji(\partial A_0/\partial r)(\partial A_r/\partial r) + jj(\partial A_0/\partial r)^2 + ii(\partial A_r/\partial t)^2 + ij(\partial A_r/\partial t)(\partial A_0/\partial t) + ji(\partial A_0/\partial t)(\partial A_r/\partial t) + jj(\partial A_0/\partial t)^2$  .

Since  $ii=-1$ ,  $jj=-1$ ,  $ij=-ji$  the middle terms cancel leaving  $[i\partial^2 A_r/\partial r^2 + i\partial^2 A_r/\partial t^2] +$

$[j\partial^2 A_0/\partial r^2 + j\partial^2 A_0/\partial t^2] + ii(\partial A_r/\partial r)^2 + jj(\partial A_0/\partial r)^2 + ii(\partial A_r/\partial t)^2 + jj(\partial A_0/\partial t)^2$

Plugging in A2 and A4 gives us cross terms  $jj(\partial A_0/\partial r)^2 + ii(\partial A_r/\partial t)^2 = jj(\partial(-A_r/\partial r)^2 + ii(\partial A_r/\partial t)^2$

$=0$ . So  $jj(\partial A_r/\partial r)^2 = -jj(\partial A_0/\partial t)^2$  or taking the square root:  $\partial A_r/\partial r + \partial A_0/\partial t = 0$  (A5)

$i[\partial^2 A_r/\partial r^2 + i\partial^2 A_r/\partial t^2] = 0$ ,  $j[\partial^2 A_0/\partial r^2 + i\partial^2 A_0/\partial t^2] = 0$  or  $\partial^2 A_\mu/\partial r^2 + \partial^2 A_\mu/\partial t^2 + .. = 1$  (A6)

A4 and A5 are **Maxwell's equations** (Lorentz gauge formulation) in free space, if  $\mu=1,2,3,4$ .

$\square^2 A_\mu = 1$ ,  $\square \bullet A_\mu = 0$  (A7)

## A5 Other $45^\circ+45^\circ$ Rotations (Besides above quadrants II $\rightarrow$ III)

For the **composite  $e,\nu$**  on those required large  $z=0$  eq.12 rotations for  $C \approx 0$ , and for stability  $r=r_H$  for  $2P_{1/2}$  ( $I \rightarrow II$ ,  $III \rightarrow IV$ ,  $IV \rightarrow I$ ) unless  $r_H=0$  ( $II \rightarrow III$ ) are:

**Ist  $\rightarrow$  IIInd quadrant rotation** is the  $W^+$  at  $r=r_H$ . Do similar math to A2-A7 math and get instead a Proca equation The limit  $\varepsilon \rightarrow 1 = \tau$  (D13) in  $\xi_1$  at  $r=r_H$ . since Hund's rule implies  $\mu = \varepsilon = 1S_{1/2} \leq 2S_{1/2} = \tau = 1$ . So the  $\varepsilon$  is negative in  $\Delta\varepsilon/(1-\varepsilon)$  as in case 1 charged as in appendix C1 case 2.

$E = 1/\sqrt{(\kappa_{00})} - 1 = [1/\sqrt{(1-\Delta\varepsilon/(1-\varepsilon)-r_H/r)}] - 1 = [1/\sqrt{(\Delta\varepsilon/(1-\varepsilon))}] - 1$ .  $E_t = E + E = 2/\sqrt{(\Delta\varepsilon/(1-\varepsilon))} = W^+$  mass.

$E_t = E - E$  gives E&M that also interacts weakly with weak force.

**IIIrd → IV quadrant rotation** is the W-. Do the math and get a Proca equation again.

$$E=1/\sqrt{(\kappa_{00})} -1=[1/\sqrt{(1-\Delta\epsilon/(1-\epsilon)-r_H/r)}]-1=[1/\sqrt{(\Delta\epsilon/(1-\epsilon))}]-1. E_t=E+E=2/\sqrt{(\Delta\epsilon/(1-\epsilon))}=W- \text{ mass.}$$

$E_t=E-E$  gives E&M that also interacts weakly with weak force.

**IVth → Ist quadrant rotation** is the Z<sub>0</sub>. Do the math and get a Proca equation. C<sub>M</sub> charge cancelation. D14 gives  $1/(1+\epsilon)$  gives 0 charge since  $\epsilon \rightarrow 1$  to case 1 in appendix C2.

$$E=1/\sqrt{(\kappa_{00})} -1=[1/\sqrt{(1-\Delta\epsilon/(1+\epsilon)-r_H/r)}]-1=[1/\sqrt{(\Delta\epsilon/(1+\epsilon))}]-1. E_t=E+E=2/\sqrt{(\Delta\epsilon/(1+\epsilon))}-1=Z_0 \text{ mass.}$$

$E_t=E-E$  gives E&M that also interacts weakly with weak force. Seen in small left handed polarization rotation of light.

**IInd→IIIrd quadrant rotation** through those 2 neutrinos gives 2 objects.  $r_H=0$

$E=1/\sqrt{\kappa_{00}} -1=[1/\sqrt{(1-\Delta\epsilon/(1+\epsilon))}]-1=\Delta\epsilon/(1+\epsilon)$ . Because of the +- square root  $E=E+-E$  so E rest mass is 0 or  $\Delta\epsilon=(2\Delta\epsilon)/2$  reduced mass.

$E_t=E+E=2E=2\Delta\epsilon$  is the pairing interaction of SC. The  $E_t=E-E=0$  is the 0 rest mass photon Boson. Do the math (eq.A2-A7) and get Maxwell's equations. Note there was no charge C<sub>M</sub> on the two  $\nu$  s. Note we get SM particles out of composite e,  $\nu$  using required eq.9 rotations for

## A6 Object B Effect On Inertial Frame Dragging (from appendix D)

The fractal implications are that we are inside a cosmological positron inside a proton  $2P_{3/2}$  at  $r=r_H$  state. The cosmological object (electron) we are inside of is a positron and call it object A which orbits electron object B with a given distant 3<sup>rd</sup> object C. Object B is responsible for the mass of the electron since it's frame dragging creates that Kerr metric  $(a/r)^2=m_e c^2$  (D9) result used in eq.D9. So Newpde ground state  $m_e c^2 \equiv \langle H_e \rangle$  is the fundamental Hamiltonian eigenvalue defining idea for composite e,  $\nu$ ,  $r=r_H$  implying Fermi 4 point  $E = \int \psi^\dagger H \psi dV = \int \psi^\dagger \psi H dV = \int \psi^\dagger \psi G$

Recall for composite e,  $\nu$  all interactions occur inside  $r_H$   $(4\pi/3)\lambda^3 = V_{rH} \cdot \frac{1}{V^{1/2}} = \psi_e = \psi_3 \frac{1}{V^{1/2}} =$

$$\psi_\nu = \psi_4 \text{ so 4pt } \iiint_0^{r_H} \psi_1 \psi_2 \psi_3 \psi_4 dV = 2G \iiint_0^{r_H} \psi_1 \psi_2 \frac{1}{V^{1/2}} \frac{1}{V^{1/2}} V$$

$$\equiv \iiint_0^{r_H} \psi_1 \psi_2 G \equiv \iiint_0^{r_H} \psi_1 \psi_2 (2m_e c^2) dV_{rH} = \iiint_0^{V_{rH}} \psi_1 (2m_e c^2) \psi_2 dV_{rH} \quad (A8)$$

## Application of Eq.A8 To Ortho states (created by that $2P_{3/2}$ 2body motion at $r=r_H$ )

The composite 3e ortho state (partII) operator adds spin (eg., as in 2<sup>nd</sup> derivative eq.A1) so 2<sup>nd</sup> derivative  $\Sigma((\gamma^\mu \sqrt{\kappa_{\mu\mu}} dx_\mu) - i\kappa)(\gamma^\nu \sqrt{\kappa_{\nu\nu}} dx_\nu + i\kappa)\chi = \Sigma((\gamma^\mu \sqrt{\kappa_{\mu\mu}} dx_\mu) - i\kappa)\psi$  so  $\frac{1}{2}(1 \pm \gamma^5)\psi = \chi$ . In that regard the expectation value of  $\gamma^5$  is speed and varies with  $e^{i3\phi/2}$  in the trifold. The spin $^{1/2}$  decay proton  $S_{1/2} \propto e^{i\phi/2} \equiv \psi_1$ , the original ortho  $2P_{1/2}$  particle is chiral  $\chi = \psi_2 \equiv \frac{1}{2}(1 - \gamma^5)\psi = \frac{1}{2}(1 - \gamma^5 e^{i3\phi/2})\psi$ . Initial  $2P_{1/2}$  electron  $\psi$  is constant. Start with initial ortho state  $\chi$ . These  $\gamma^5$  terms then modify equation

$$A8 \text{ to read } = \iiint_0^{V_{rH}} \psi_1 \psi_2 (2m_e c^2) dV_{rH} = \iint \psi_{S1/2}^* (2m_e c^2 V_{rH}) \chi dV_\phi = K \int \langle e^{\frac{i\phi}{2}} [\Delta\epsilon V_{rH}] \left( 1 - \right.$$

$$\left. \gamma^5 e^{i\phi/2} \right) \psi \rangle d\phi = K G_F \int \langle e^{i\phi/2} - \gamma^5 i e^{i(4/2)\phi} \rangle d\phi = K G_F \left( \frac{2e^{i\phi}}{i} \Big|_0^{2\pi+C} - \frac{2\gamma^5 e^{i4\phi}}{i4} \Big|_0^{2\pi+C} \right) =$$

$$k(1/4 + i\gamma^5) = k(.225 + i\gamma^5 0.974) = k(\cos 13^\circ + i\gamma^5 \sin 13^\circ) \text{ deriving the } 13^\circ \text{ Cabbibo angle. With}$$

previously mentioned CP result(direct evidence of fractal universe) get CKM matrix.

**Review of 2P<sub>3/2</sub>** Next higher fractal scale (X10<sup>40</sup>), cosmological scale proton.Observor inobjectA

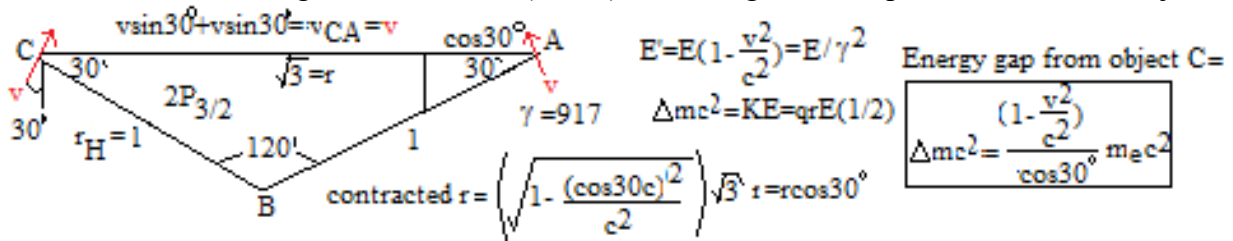


Fig.7 Recall from D9  $m_e c^2 = \Delta \epsilon$  is the energy gap for object B vibrational stable eigenstates of composite  $3e(\text{part II})$ . Recall for the positron motion  $\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = 917$  and  $E = (1/917^2)E'$  (from

Feynman's lectures) in the forward or backward direction of the CA line (since  $v \sin 30^\circ + v \sin 30^\circ = v$ )  $1/\cos \theta$  away from forward direction line (the weakest E field direction), toward the line in the object B direction. But object C is  $30^\circ$  from object B direction and  $\frac{1}{2} E_{qr} = KE$  for circular motion with  $v$   $30^\circ$  from object B direction object C scissors eigenstates of  $r/\cos \theta$  (= the only variable  $r$  in Frobenius solution) Ch.8,9 instabilities Also recall law of cosines  $r^2 = 1^2 + 1^2 + 2(1)(1)\cos 120^\circ = 3$ , So relative to the A-B line Fitzgerald contract

$$r = \sqrt{1 - \frac{\cos^2 30^\circ c^2}{c^2}} \sqrt{3} = .866 = \cos 30^\circ$$
 Making object C appear .866X closer than object B. So to make object C appear as the same distance as object B (to compare with  $m_e c^2$ ) divide by  $\cos 30^\circ$ . Allowing us to finally compare the energy gap caused by object C to the energy gap caused by object B. So  $E_{qr} = \Delta E = (m_e c^2 / ((\cos 30^\circ)^9 17^2)) = m_e c^2 / 728000$ . So energy gap caused by object C is  $\Delta E = (m_e c^2 / ((\cos 30^\circ)^9 17^2)) = m_e c^2 / 728000$ . The weak interaction occurs inside of  $r_H$  with those electrons  $m_e$ . The G can be written for E&M decay as  $(2m_e c^2) X V_{r_H} = 2m_e c^2 [(4/3)\pi r_H^3]$ . So for weak decay from equation A8 it is  $G_F = (2m_e c^2 / 728,000) V_{r_H} = \mathbf{G_F}$  **the strength of the Fermi weak interaction constant** which is the coupling constant for the Fermi 4 point weak interaction. Note  $2m_e c^2 / 729,000 = 1.19 \times 10^{-19} \text{J}$ . So  $\Delta E = 1.19 \times 10^{-19} / 1.6 \times 10^{-19} = .7 \text{eV}$  which is our  $\Delta E$  gap for the weak interaction inside the integral for  $G_F$ .

## A8 Derivation of the Standard Model from Newpde but with No Free parameters

Since we have now derived  $M_W$ ,  $M_Z$  and their associated Proca equations, and Dirac equations for  $m_\tau, m_\mu, m_e$  etc., and  $G, G_F, k^2$  Maxwell's equations, etc. we can now write down the usual Lagrangian densities that implies these results. In the formulation  $M_Z = M_W / \cos\theta_W$  you can find the Weinberg angle  $\theta_W$ ,  $g \sin\theta_W = e$ ,  $g' \cos\theta_W = e$ ; solve for  $g$  and  $g'$ , etc., We will have thereby derived the standard model from first principles (i.e., postulate 1). **It no longer contains free parameters!**

## Appendix B

### B2 List-Define Mathematics from postulate 1 (Part2 for details)

So in postulate 1  $z=zz$  why did 0 come along for the ride? There is a deeper reason in set theory. Note  $\emptyset$  and 0 aren't really new postulated observables since they are literally postulating "nothing".

**More fundamental than the  $zz=z$  {1,0} solutions is the set theory: {set, $\emptyset$ }**

The null set  $\emptyset$  is the subset of every set. In the more fundamental set theory formulation  $\{\emptyset\} \subset \{\text{all sets}\} \Leftrightarrow \{0\} \subset \{1\}$  since  $\emptyset = \emptyset \cup \emptyset \Leftrightarrow 0 = 0 + 0$ ,  $\{\{1\} \cup \emptyset\} = \{1\} \Leftrightarrow 1 + 0 = 1$ .

So list  $1 \cup 1 = 1 + 1 = 2$ ,  $2 \cup 1 = 1 + 2 = 3$ , ... all the way up to  $10^{82}$  (see Fiegenbaum point) and **define** all this list as  $a+b=c$ , etc., to create our algebra and numbers which we use to write [equation 1](#)  $z=zz+C$ ,  $\delta C=0$  for example. Recall every set has the null set as a subset. So from above set  $\{1\}$  ( $\xi_1$  for  $z=1$ ) has the 0 ( $\xi_0$  for  $z=0$  ground state) as a subset. So  $\xi_1 = \xi_{2S_{1/2}} + \xi_{1S_{1/2}} + \xi_0 = \tau + \mu + m_e$ . (B1)

### 2D+2D→4D Orthogonality

So given this added 2D  $\Delta$  perturbation we get curved space  $2D \otimes 2D = 4D$  independent  $x_1, x_2 \rightarrow x_1, x_2, x_3, x_4$ . Also assuming orthogonality  $dr^2 \equiv dx_1^2 + dx_2^2 + dx_3^2$  (as  $r \rightarrow \infty$  in eq.13,15) 5 so  $\{dr^2 - dt^2\}, (dr'^2 - dt'^2) \rightarrow dx^2 + dy^2 + dz^2 - dt^2$  must imply since there is no other way to preserve orthogonality and the 2D Minkowski and Clifford algebra limits  $(\gamma^t dr' + i\gamma^t dt')$ ,  $(\gamma^t dr + i\gamma^t dt) \rightarrow \gamma^x dx + \gamma^y dy + \gamma^z dz + \gamma^t dt$  so that

$$(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 - \kappa_{tt} dt^2 = ds^2.$$

The right side of eq.14a therefore has the 2 in the sum replaced by a 4 implying the left side then has to be in eq.14a for the 2D form to be a special case (of any 2  $x_i x_j$ ): Imposing orthogonality thereby creates 6 pairs of eqs.4&5.

## Appendix C

**Actually sect.1 e, $\nu$  wasn't the only  $N=1$  observer result: the  $N=1$   $\mu, \tau$  also results as Mandelbrot set induced excited states of e**

Recall the Mandelbrot set in small C boost  $C_M = \xi C$  sect.2. From eq.3  $\delta z + \delta z \delta z = C$  or  $N=1$   $\delta z \delta z = C$  68.7° from eq3 quadratic equation at Fiegenbaum point. 45° from  $ds^2$  minimalization.  $\mu$  then is not a constant in time because of eq.12 angle New pde zitterbewegung contribution to the  $\delta z$  perturbation of the 45°. In contrast the ratio  $\tau/e$  is here constant, is "absolute stability", the angle 68.74° never changes, irregardless of the perturbation.  $\tau, \mu, e$  are Newpde free space eigenvalues of some eigenstates but which eigenstates? Note that  $\tau/e$  must be "absolute stability" (the angle does not change) or the eigenstates would cease to exist, and so the Mandelbulbs would disappear which they can't. There is also the three source absolute invariance  $\tau, \mu, e$  mapping only into a  $2P_{3/2}$  at  $r=r_H$ . 3 object geometry eigenstate. So these eigenstate is uniquely single absolutely stable 2positron (+e) at  $r=r_H$  (central electron) Newpde  $2P_{3/2}$  state and so by Hund's rule  $2S_{1/2}$  and  $1S_{1/2}$ . as  $\tau$  and  $\mu$  respectively. Otherwise these Newpde eigenstates of  $\mu$  and  $\tau$  are forever unknown except for their masses. Also the absolutely stable  $2P_{3/2}$  state at  $r=r_H$  ( $dt'^2 = (1-r_H/r)dt^2$  makes  $r=r_H$  and the 1/20barn creation cross-section absolutely stable) has to exist for all this to turn out to be true. Note then the two body 2 positron COM so also reduced mass so  $\tau + \mu = \xi_1 = 2m_p$ .  $2P_{3/2}$  at  $r=r_H$  is 3 lobed stable state we define as the  $m_p$  state since it is caused by same required COM 2 positron motion around the electron.

Well it turns out this *absolutely* stable unique  $2P_{3/2}$  state at  $r=r_H$  does not have to be postulated, *It actually exists* (Part II and below). We can actually calculate  $m_p$  from the quantization of the magnetic flux  $\Phi_0=BA$  and from that get  $\tau+\mu+e.=2m_p$  using the Mandelbrot set  $2m_p=\tau+\mu+e.=\xi_1$  and the Mercuron equation D15 for  $\mu$  and also use the location of object B to find the underlying value of  $m_e$ .

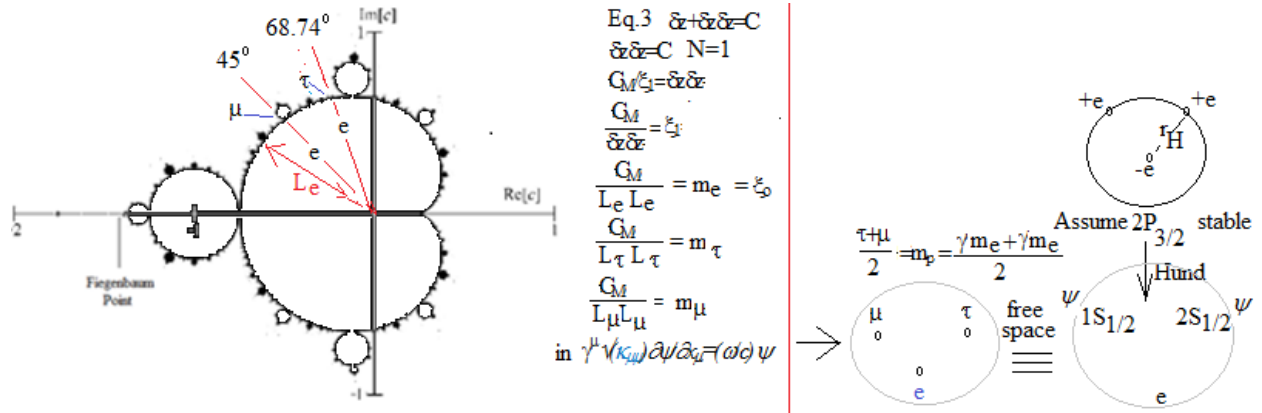


Fig.6

Small C boost provided by Newpde  $2P_{3/2}$   $r=r_H$  **Composite 3e**

Recall from section 3.1 that small C boost gets  $z=zz$  (so postulate 1) but also gets the numerical **numerical value of Large  $\xi_1$** . or that stable  $z=0$  the only way to get stable large  $\xi$  (required by that small C' boost) is with the Newpde **composite 3e**  $2P_{3/2}$  at  $r=r_H$  state (partII davidmaker.com). So *stability* ( $dt'^2=(1-r_H/r)dt^2$ ) clocks stop at  $r=r_H$ . The *two positron motion* and  $h/2e$  quantization of flux  $BA$  then gives us the exact proton mass  $m_p$  (below) as a reduced mass for the associated Hund rule  $\tau \equiv 2S_{1/2}, 1S_{1/2} \equiv \mu$  states (so  $\tau+\mu=\xi_1$ ,  $m_p=\xi_1/2$ ). That 3<sup>rd</sup> mass also reverses the pair annihilation virtual pair creation inside the  $r_H$  volume given  $\sigma=\pi r_H^2 \approx (1/20)$  barns. which is the reason why only composite 3e gives stability and not other larger composites (except multiples of 3e itself. From object B inertial frame dragging suppression (D9) the ground state  $m_e=\xi_0=\Delta\varepsilon=.0005799$ . (C1)

From Hund's rule mass of  $2P_{3/2}$  is  $2m_p$  (C4)= mass of  $(2S_{1/2}+1S_{1/2})=\xi_1=\tau+\mu=1+\varepsilon$  with cosmological (Ch.7) variable currently at (present day eq.D13)  $\varepsilon=\mu=.06$

### N=0 Magnetic Flux Quantization For Current Around Loop

Our Newpde II  $\rightarrow$  III quadrant eq.12 rotations (appendix A4) gave us Maxwell's equations and E&M so we can apply B fields here. We also derived quantum mechanics from that Circle equation (giving eq.11). Thus we can have quantization of the B field flux  $\oint \vec{B} \cdot \vec{dA} = \Phi_0 N$ . Just above (and below) the coil plane toward the edge of the coil the B direction changes and the magnitude of B goes up. So some  $\vec{B} \cdot \vec{dA} = \Delta\Phi$  minimum deviation from  $BdA$  for some constant  $|\vec{dA}|$  above the coil plane. Given B is perpendicular to  $dA$  at the center and the radius  $r_H$  of the coil cancels out (eq.2 below) this  $\Delta\Phi$  flux could be over the center where the relevant  $\gamma$  is needed. Thus we must write  $\Sigma\Delta\Phi=\Phi=BA= B\pi r_H^2$  with the B at the center of the coil for  $z=0$  (appendix). So effective  $r_H$  slightly bigger (making B smaller) but  $r_H$  cancels anyway. So

$$BA = \left(\frac{\mu_0 i}{2r_H}\right) \pi r_H^2 = \Phi_0 (\#2P_{3/2} \text{ lobes}). \quad (1)$$

Also  $r_H=e^2/m_e c^2$ ,  $q/t=i$ .  $q=e=1.6 \times 10^{-19}$  C,  $\Phi_0=$  NIST:  $2.067833848 \times 10^{-15}$  Wb,  $1/\gamma$  dilation of  $r_H$  but it and  $r_H$  get canceled out here. The time  $t$  dilation  $\gamma$  remains in the current 'i' moving frame of reference. Recall that for circular motion:  $c=D/t=2\pi r_H/t$  so:



$$t = \frac{2\pi r_H}{\gamma c}, \text{ so } i = \frac{e}{\left(\frac{2\pi r_H}{\gamma c}\right)}$$

$$BA = \frac{\mu_0 i}{2r_H} (\pi r_H^2) = \frac{\mu_0}{2r_H} \left( \frac{e}{\left(\frac{2\pi r_H}{\gamma c}\right)} \right) (\pi r_H^2) = \Phi_0 N = \frac{h}{2e} (3 \text{lobes} \times 2 \text{Positron Motion}) \quad (2)$$

$B = \mu_0 i / 2r_H$  is the minimum B inside the loop, and given  $r_H$  cancels out in eq.2, can be taken as a variational principle optimization of the energy  $B^2$ .

Each of the 2 positron flux contributions around the circle ( $N=2$ ). But each positron moves through all 3  $2P_{3/2} = N=2$  lobes. So doing the cancelations in eq.2:

$$\gamma(\mu_0/4)ec = (h/2e)(2 \text{positrons} \times 3 \text{lobes}). \quad (3)$$

So

$\gamma(\mu_0/4)ec = (h/2e)6$ , But there already is a populated state (Hund's rule)  $1S_{1/2}(\mu) = 1.125 = \mu/P$  so we add it in (For example recall in the hydrogen atom that the 1S states fill before the 2P states.).

So:

$$\gamma = \frac{h}{2e} 6(1 + \mu) \frac{1}{\frac{\mu_0}{4}ec} \quad (\text{Note that 4 cancels the 4 in } \mu_0 = 4\pi \times 10^{-7} \text{ Wb-m/Amps.})$$

$$\gamma = \frac{2.0678 \times 10^{-15} (6)(1 + \mu)}{\pi \times 10^{-7} 1.6 \times 10^{-19} 3 \times 10^8} = \frac{1.2407 \times 10^{-14} \times (1.11255)}{1.5086 \times 10^{-17}} = \frac{1.38034 \times 10^{-14}}{1.5086 \times 10^{-17}} = 915 \quad (4)$$

We must add in the  $3 \times 511 = 1.533$  for the 3 electrons

$$915 + 1.533 = 916.533$$

$2P_{3/2}$  at  $r=r_H$  implies also twice our 2 positron  $\gamma$  result will be the proton mass.

$$2(916.533)m_e c^2 = 1.50087 \times 10^{-10} \text{ J} = 937 \text{ MeV}$$

Finally we must add that 1MeV binding energy between that  $\mu$  and the (Fitzgerald contracted) net +e positrons and electron (Fitzgerald contracted to a point Coulomb source) from axial frame of reference (sect.10.5) and get 938.23MeV.

Actual proton mass = 938.272MeV =  $m_p$ .

An exact answer!

938.272MeV =  $m_p$  **Therefore we have derived the mass of the proton from first principles.**

Small C (Part II) of this book starts out with this result.

## Appendix D digital analogy of this theory

**Review** This is an Occam's razor *optimized* (i.e.,  $\delta C=0$ ,  $\|C\|=\text{noise}$ )

POSTULATE OF 1

So

$z=zz$  (2) is the algebraic definition of 1, and add real constant C (i.e.,  $z'=z'z'$ ,  $\delta C=0$ ) (1)

**Digital communication analogy:** Binary ( $z=zz$ ) 1,0 signal (Boolean algebra) with white noise  $\delta C=0$  in  $z'+C=z'z'$ . Recall the algebraic definition of 1 is  $z=zz$  which has solutions 1,0.(eq.11a)

Also you

could say white noise C has a variation of zero ( $\delta C=0$ ) making it easy to filter out (eg., with a Fourier cutoff filter).

So you could easily make the simple digital communication analogy of this being a binary ( $z=zz$ ) 1,0 signal with white noise  $\delta C=0$  in  $z'+C=z'z'$ .

(However the noise is added a little differently here ( $z+C=zz$ ) than in statistical mechanics (eg., There you might use deconvolved signal=convolution integral [(transfer function)signal]dA)). where the 'signal' actually would equal  $z+C$  So this is not quite the same math as in statistical mechanics.)

## Ch.2 Details of List define Mathematics and Fractalness

### 2.1 List- Define Mathematics (continuation of section 1 appendix B)

Because of our postulate of 1 we can then *list* all cases such as  $1 \cup 1 \equiv 1+1 \equiv 2$  and define  $a+b=c$ . Note along the way we have defined union and so define set theory as well.

| The Progressive "List" Origin Of Mathematics                       |                                        |
|--------------------------------------------------------------------|----------------------------------------|
| Microcosm Math 3 Numbers<br>(allowed by finite precision)          | Cosmic Math $10^{82}$ Numbers          |
| $1 \cup 1 \equiv 1+1 \equiv 2$                                     | $1+1 \equiv 1*2$                       |
| $1 \cup 2 \equiv 1+2 \equiv 3$                                     | $2+2 \equiv 2*2$                       |
| Defines $A+B \equiv C$                                             | Defines $A*B \equiv C$ That being eq.2 |
|                                                                    | Finite precision $\equiv$ noise $> 0$  |
| Eq.2 can now define 0 with $0*0=0$                                 |                                        |
| Use 0 to define subtraction with                                   |                                        |
| $1-1 \equiv 0$                                                     |                                        |
| $2-2 \equiv 0$                                                     |                                        |
| $3-3 \equiv 0$                                                     |                                        |
| Defines $\delta C=0$ That being Eq.1 in this particular microcosm. |                                        |

Note there are no axioms for defining relations  $A+B=C$  or  $A*B=C$ , just the list above those relations.

Fig.7 in that particular microcosm. There are no postulated rings or fields here either.

Recall section appendix B. We use 3 number math to progressively develop the 4 number math etc., eg.,  $2+2 \equiv 4$ ., so yet another list. Go on to define division from  $A*B \equiv C$  then  $A \equiv B/C$ . So the method is List-define, list-define, list-define, etc., as we proceed into larger and larger microcosms. There are no new postulates (axioms) in doing that. It follows from our generation of those 6 Clifford algebra cross terms one after the other and that sequence of 4D electrons, the objects we are counting. We require integers and so no new axoms. Note C implies finite precision and we can always multiply a finite precision number by a large enough integer to make a finite precision number an integer in any case. So we also have our required integers here. So we don't need any more axioms such as Peano's mathematical induction or ring and field axioms. We generate each microcosm number and algebra with this list define method until we reach  $10^{82}$  (sect.2).

Subtraction  $a-b=c$ :

List

$1-1=0$  (is defined as the null (0)set here).

$1+1=2$  from earlier.

$2-1=1$  etc., etc

Define  $a-b=c$

So you can define subtraction with a list-define procedure as well.

### Recall from Appendix B Mathematics Resulting From Postulate of 1

**Note  $z=0$  is also a solution to  $z=zz$**

So for added  $z \approx 0$ ,  $z\sqrt{2} = (z+\Delta)\sqrt{2}$  which we incorporate into  $\xi \equiv \xi_1 \equiv \xi + \xi_0$  where  $\xi_0 \equiv m_c$  is small. If  $\xi = \xi_0$  then  $C_M/\xi$  is big and so those big rotations in sect 1.2.

In the more fundamental set theory formulation  $\{\emptyset\} \subset \{\text{all sets}\} \Leftrightarrow \{0\} \subset \{1\} = \xi C = z_1$ . So  $\xi_0$  acts as 0 in eq.1.1.1 since  $\emptyset = \emptyset \cup \emptyset \Leftrightarrow 0+0=0$ ,  $\{\{1\} \cup \emptyset\} = \{1\} \Leftrightarrow 1+0=1$ . Thus  $z_1 = \xi_1 = m_L$  contains  $z_0 \approx 0$  in  $\xi_1 = \xi + \xi_0$  is the same algebra as the core idea of set theory and so of both mathematics and physics (as we saw above).

## Definitions Of Cantor's Cauchy Sequence And The Mandelbrot Set Set Theory Review

We postulate a single real set 1 so that the null set  $\emptyset$  is also a subset (appendix C). Note we have also *defined set theory* and also arithmetic in operator equation 11 with simultaneous eq.(7+7) and its  $1 \cup 1 \equiv 1+1 \equiv 2$  eigenvalues.

### Null Set $\emptyset$ Review

In the context of set theory the null set  $\emptyset$  is the subset of every set. Note  $\emptyset$  and 0 are not new postulates because in that case they would be postulating “nothing”.

So here you postulate {One real set} which automatically has the null set as a subset.

Note we earlier developed the whole numbers from  $1 \cup 1 \equiv 1+1$ , in the context of set theory. But  $\emptyset \cup \emptyset = \emptyset$  is the only property of the null set  $\emptyset$  we use and of course it is isomorphic to  $0 \cup 0 \equiv 0+0=0$  the *only* property of 0 we need in the development of the whole numbers.

Note also the null set is the lack of anything and so is 0.

Note the  $z_1 = z_\infty$  at  $C \rightarrow 0$  gives  $z = zz + C$  which does correspond with the 1 set ( $1 = 1 \times 1$ ) and null set dichotomy of set theory given also that  $0 = 0 \times 0$ . Also the Mandelbrot set sequence gives the Cauchy sequence of the real set.

So this {one real set} starting point maps (uniquely) directly to the **Mandelbrot set**.

Why  $\min(z-zz) > 0$ ? **Completeness and Choice** (since that implies  $z$  is a real number)

The Feigenbaum point sits on the negative  $r$  axis so equation 1 can be rewritten as  $z = zz + C$ ,  $\delta C = 0$ ,  $C < 0$  which is the same as  $\min(z-zz) > 0$ . Yes, ONE indeed is the simplest idea imaginable. But unfortunately we have to complicate matters by algebraically defining it as universal  $\min(z-zz) > 0$  and so as the two most profound axioms in **real#** mathematics:

"completeness" ( $\exists$  **min**sup) and "choice" (Here the choice function is  $f(z) = z-zz$ ). But here they are mere definitions (of “min” and “ $z-zz$ ”) since  $z = zz$ , so no  $1z = z$  field axiom for multiple  $z$ , implies our one  $z$  (See  $z \approx 1$  result below.). We did this also because that list-define math (appendix C PartI) *replaces the rest* (i.e., the order axioms, mathematical induction axiom (giving **N**) and the rest of the field axioms); Thus we have algebraically defined the **real numbers** thereby implying the usual Cauchy sequence of rational numbers definition of the **real#**  $z$ .

By the way that ‘incompleteness theorem’ of Godel is thereby negated by our *single* pick of (axiom of choice) choice function  $f(z) = z-zz$  (in association with our list-define mathematics definition defining the rest.) and incompleteness of the real numbers is negated by the “completeness” (minsup) of real number mathematics above which here are not axioms but a restatement of what we mean by  $\min(z-zz) > 0$  which itself is taken to be a restatement of the postulate of real 1. So in conclusion the postulate of real 1 negates Godel’s incompleteness theorem, makes it wrong.

Also given our  $z = zz$  and the list define math definitions we no longer need the rest of the field axioms, order axioms and mathematical induction axiom (giving **N**)

But 1,0 can define the binary system and so the rest of the real numbers through the union of eq.1.11. (See appendix D). eq.1.16a defines the finite +integer *list* (i.e.,  $1 \cup 1 \equiv 1+1 \equiv 2$ )--*define* (i.e.,  $A+B=C$ ) math *required* for the algebraic rules underpinning eq.1 **without any added postulates** (axioms). Also

*list*  $2*1=2$ ,  $1*1=1$  *defines*  $A*B=C$ . Division and **rational numbers** defined from  $B=C/A$ .

We repeat with the list  $3*1=3$ , etc., with the Clifford algebra terms satisfaction keeping this going all the way up to  $10^{82}$  and start over given the above fractal result given the  $r_H$  horizons of eq.1.18. This list-define method replacing the usual ring and field algebraic formalism Note the noise C guarantees limited precision so we can multiply any number in our list with the above trifurcation number integer  $10^{82}$  to obtain the integers in which iteration of the new pde into the Klein Gordon equation gives us quantization of the Boson fields. Cantor also used that binary number diagonal to prove the uncountability of the real numbers (with the  $r_H$  horizon from the the fractalness the observability counting limit is  $10^{82}$ ). further illustrating the importance of the binary numbers in the development of the real numbers.

**Uniqueness Of These Operator Solutions:** Note the invariant operator  $\sqrt{2}=ds$  here. So the eq.1.1.15 operator invariant  $ds^2$  and eq. 7, eq.8  $\sqrt{2}ds \equiv \delta z_M = dr \pm dt$  is the **operator** (eq.16) solution  $\delta z_M$  (so *not* others such as  $ds^3$ ,  $ds^4$ , etc., which would then imply higher derivatives, hence a functionally different operator.

## Origin O Mathematics List-define, List-Define $\rightarrow 10^{82}$ Derivation Of Mathematics Without Extra Postulates

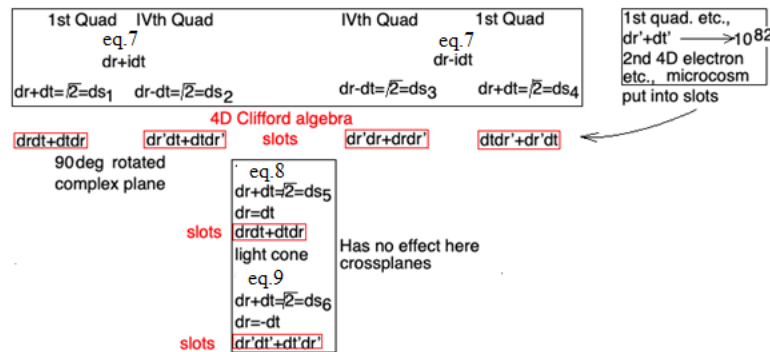


Fig.6 These added cross term eq.11a objects (1.11) extend eigenvalue equation 11 from merely saying  $1+1=2$  all the way to the number  $10^{82}$ .

From section 1 we generate 6 cross terms directly from one application of eq.1a that may or may not be the ones required for our 4D Clifford algebra. To get precisely the 6 cross terms of a 4D Clifford algebra we had to repeatedly plug into eq.2 the associated  $dr, dt$  of the required cross term  $drdt+dt dr$ . Note **by doing this we include the two  $v$  fields in the definition of the electron!** electrons and so a sequence of electrons. We thereby generate the universe! Thus we have derived the below progressive generation of list- define microcosms in eq.1.11a. We then plug that into eq.1.24 as sequence of electrons. This allows us to use eq.11a to go beyond 1U1, beyond 2 to 3 let's say. So we can then define  $1 \cup 1$  from equation eq.11  $\delta z_M$  just like postulate 1 was defined from eq.13 and eq.2. So consistent with eq.11a and eq.1.2 we can then develop +integer mathematics from 1U1 beyond 2 because of these repeated substitutions into eq.11a using a list-define method so as not to require other postulates. So by deriving the 6 crossterms of one 4D electron we get all  $10^{82}$  of them! So just multiply any number (given our limited precision) by  $10^{82}$  and it becomes an integer implying all integers here. Given the  $\psi$ s of equation 9 for  $r < r_c$  (So a allowed zitterbewegung oscillation thus SHM analogy) we can then redefine this integer  $N-1$  also as an eigenvalue of a coherent state Fock space  $|\alpha\rangle$  for which  $a|\alpha\rangle=(N-1)|\alpha\rangle$ . Also recall eigenvalue  $1 \cup 1$  is defined from equation 1.16a. Note  $10^{82}$  limit from section 6.1. Any

larger and it's back to one again. But in this process we thereby create other 1.11 terms for other electrons and so build other 4D . Fig.7

Recall section 1.3. We use 3 number math to progressively develop the 4 number math etc., eg.,  $2+2=4$ ., so yet another list. Go on to define division from  $A*B=C$  then  $A=B/C$ . So the method is List-define, list-define, list-define, etc., as we proceed into larger and larger microcosms. There are no new postulates (axioms) in doing that. It follows from our generation of those 6 Clifford algebra cross terms one after the other and that sequence of 4D electrons, the objects we are counting. We require integers and so no new axioms. Note C implies finite precision and we can always multiply a finite precision number by a large enough integer to make a finite precision number an integer in any case. So we also have our required integers here. So we don't need any more axioms such as Peano's mathematical induction or ring and field axioms. We generate each microcosm number and algebra with this list define method until we reach  $10^{82}$  (sect.2).

**Our Limit Definition** (eg., in the Cauchy Sequence)

In section 2 you notice (attachment) our **numbers** are also eigenvalues (observables) in eq.11 and also **are the # of electrons**. But there is no observation possible through the fractal  $r_H$  horizons in eq.2 (and sect.2.5) and  $10^{82}$  is the maximum such number inside  $r_H$  ( $C_M$ ). Also all small limits are then only to the next smaller fractal baseline ( $C_{M-1}$ ) horizon and no farther. *This is stated several places in the paper* (eg., definition paragraph first page).

So since our numbers here are observables and so **all limits**, big and small, are limited by these fractal scales (eg., instead of limit  $x \rightarrow 0$  we have limit  $x \rightarrow \Delta$  where  $\Delta$  is the next smaller fractal scale.). This makes it so there is only one thing we are postulating, **1**, the electron given by eq.2 (see the inside-outside comment in the summary below).

So these limits (eg., for the Cauchy sequences) are all required by the postulate of **1**.

You could call them "fractal based limits" if you like. Recall that: given a number  $\epsilon > 0$  there exists a number  $\delta > 0$  such that for all  $x$  in  $S$  satisfying

$$|x - x_0| < \delta$$

we have

$$|f(x) - L| < \epsilon$$

Then write  $\lim_{x \rightarrow x_0} f(x) = L$

Thus you can take a smaller and smaller  $\epsilon$  here, so then  $f(x)$  gets closer and closer to  $L$  even if  $x$  never really reaches  $x_0$ . "Tiny" for  $h \rightarrow L_1$  and  $f(x+h) - f(x) \rightarrow L_2$  then means that  $L = 0 = L_1$  and  $L_2$ . 'Tiny' is this difference limit.

### **Hausdorf (Fractal) s dimensional measure using $\epsilon, \delta$**

Diameter of  $U$  is defined as

$$|U| = \sup\{|x - y| : x, y \in U\}. \quad E \subset \cup_i U_i \quad \text{and} \quad 0 < |U_i| \leq \delta$$

$$H_\delta^s(E) = \inf \sum_{i=1}^{\infty} |U_i|^s$$

analogous to the elementary  $V = U^s$  where of  $s=3$ ,  $U=L$  then  $V$  is the volume of a cube  $\text{Volume} = L^3$ . Here however 's' may be noninteger (eg., fractional). The volume here would be the respective Hausdorf outer measure.

The infimum is over all countable  $\delta$  covers  $\{U_i\}$  of  $E$ .

To get the Hausdorf outer measure of  $E$  we let  $\delta \rightarrow 0$   $H^s(E) = \lim_{\delta \rightarrow 0} H_\delta^s(E)$

The restriction of  $H^s$  to the  $\sigma$  field of  $H^s$  measurable sets is called a Hausdorf s-dimensional measure. Dim E is called the Hausdorf dimension such that

$$H^s(E) = \infty \text{ if } 0 \leq s < \dim E, \quad H^s(E) = 0 \text{ if } \dim E < s < \infty$$

So if s implies a zero H or infinite H it is not the correct dimension. This rule is analogous to the definition of the (fractal) Mandelbrot set itself in which a C that gave infinity is rejected by the definition  $\delta C = 0$  we can model as a binary pulse ( $z = zz$  solution is binary  $z = 1, 0$ ) with

**$zz = z(1)$  is the algebraic definition of 1 and can add real constant C** (so  $z' = z'z' - C$ ,  $\delta C = 0$ )  
 (2)) Plug  $z' = 1 + \delta z$  into eq.2 and get  $\delta z + \delta z \delta z = C$  (3)

so  $\delta z = (-1 \pm \sqrt{1 + 4C})/2 = dr + idt$  (4)

for  $C < -1/4$  so real line  $r = C$  is immersed in the complex plane. To find C itself substitute  $z'$  on left (eq.2) into right  $z'z'$  repeatedly & get  $z_{N+1} = z_N z_N - C$ .  $\delta C = 0$  requires us to reject the Cs for which  $-\delta C = \delta(z_{N+1} - z_N z_N) = \delta(\infty - \infty) \neq 0$ .  **$z = zz$  solution is 1,0** so initial

**$z = z_0 = 0$  gets the Mandelbrot set  $C_M$**  (fig2) out to some  $\|\Delta\|$  distance from  $C = 0$ .  $\Delta$  found from  $\delta C \equiv (\partial C_M / \partial (\|C\|)) d\|C\| = 0$  extreme giving the Feigenbaum point  $\|C_M\| = \|-1.400115..\|$  global max given this  $\|C_M\|$  is biggest of all.

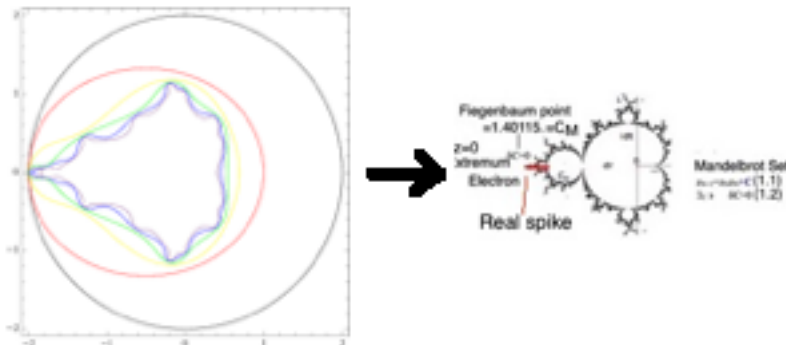
If s is not an integer then the dimensionality it has a fractal dimension.

But because the Feigenbaum point  $\Delta$  uncertainty limit is the  $r_H$  horizon, which is impenetrable (sect.2.5, partI),  $\epsilon, \delta$  are not  $dr/ds$  eq.11a observables for  $0 < \epsilon, \delta < r_H$ . Instead  $\epsilon, \delta > \Delta = r_H$  = the next  $10^{40}X$  smaller fractal scale Mandelbrot set at the Feigenbaum point.

## 2.2 The isolated lemniscate Mandelbrot Set implied by the circle (eq.11) observability

In section 1 we got the Circle  $dr^2 + dt^2 = ds^2$  and so *observability* of eq.11. So including observability *only* we could have instead postulated  $1^2 = 1^2 1^2$  or  $C_{N+1} = C_N C_N + C$ .  $C = C_1 = dr^2 + dt^2$ ,  $C_0 = 0$  instead of the more general  $z = zz$  ( $1 = 1X1$ ) implying  $z_{N+1} = z_N z_N + C$ . This gets the lemniscate sequence and so just the bare bones Mandelbrot set without all the flourishes of the smaller scale versions of  $z_{N+1} = z_N z_N + C$ .

Note then *observability* thereby implies *only* the basic Mandelbrot set structure and so not all the other parts, the flourishes, of that zoom. Thus for *observability* the  $\|C_M\|$  **extremum really is at the Feigenbaum point** (and  $-1/4$ ) for all fractal scales. So a given **Mandelbrot set is an observable!!** (irregardless of the clutter it resides in)



point  $C_M$ .

fig.7

From the sect.1 Circles resulting in the 'observability' of eq.11 these  $z=0$  lemniscates constructed from these circles give  $\delta z = r_H = C_M 10^{40N} / \xi_1 = \Delta$  perturbations to C and so  $\Delta$  perturbations to  $z=0$  from eq.3. So  $z=0 \rightarrow z=0 + \Delta$ . (2.2.1)



Fig.7 Lemniscate sequence (Wolfram, Weisstein, Eric)  $C_{N+1}=C_N C_N + C$ .  $C=C_1=dr^2+dt^2$ ,  $C_0=0$ . After an infinite number of successive approximations  $C''=C'C'+C=C_M^2$  Mandelbrot calls  $C_M$  the ER, Escape Radius (see Muency).

POSTULATE OF 1

So

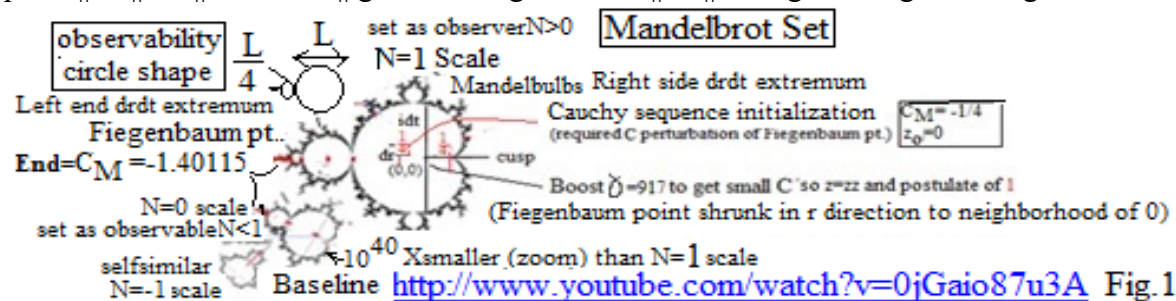
$z=zz$  (1) is the algebraic definition of 1,0. So add constant  $C$  (i.e.,  $z'=z'z'-C$ ,  $\delta C=0$ ) (2)),  $C \ll 1$  Iteration (eq.1 gives  $z=0$ )

Plug  $z'=1+\delta z$  into eq.2 and get  $\delta z + \delta z \delta z = C$  (3)

For real  $C < -1/4$   $\delta z = (-1 \pm \sqrt{1 + 4C})/2 = dr + idt$  (4)

is complex. To find  $C$  itself substitute  $z'$  on left (eq.2) into right  $z'z'$  repeatedly & get iteration  $z_{N+1}=z_N z_N - C$ .  $\delta C=0$  requires us to reject the  $C$ s for which  $-\delta C = \delta(z_{N+1} - z_N z_N) = \delta(\infty - \infty) \neq 0$ .

Eq1 solution is 1,0 so initial  $z=z_0=0$  gets the Mandelbrot set  $C_M$  (fig1) out to some  $\|\Delta\|$  distance from  $C=0$ .  $\Delta$  is found from  $\delta C \equiv (\partial C_M / \partial (\|C\|)) d\|C\| = 0$  extremum giving the Fiegenbaum point  $\|C_M\| = \|-1.40115..\|$  global max given this  $\|C_M\|$  is largest in fig.1 and fig.7



Note at the Fiegenbaum point the Mandelbrot set is  $10^{40} \times$  fractal with a  $45^\circ$  between successive Mandelbrot sets. See youtube <http://www.youtube.com/watch?v=0jGaio87u3A>

Need to search around the clutter in this zoom for the lemniscates (eg.fig.8) to find the circle derived shapes(fig.7) and hence the observables (sect.1)  $drdt > 0$  extremum requirement comes from eq.7 below for  $\delta C_r = 0$  in the baseline lemniscate formulation (fig.7) giving the Fiegenbaum point  $f = -1.40115.. = C_M$  ( $\equiv e^2$  later ansatz) thereby a vector. So it is a first rank contravariant tensor  $f^i$ , defined from the Mandelbrot set fig1  $N$  fractal scale zoom (unitary matrix) orientation  $U$ , length  $S$  and displacement  $D$  so

$$\begin{bmatrix} f_{1N} \\ f_{2N} \end{bmatrix} = S_N \begin{bmatrix} U_{11} & U_{12} \\ U_{21} & U_{22} \end{bmatrix} \begin{bmatrix} f \\ 0 \end{bmatrix} + \begin{bmatrix} D_{1N} \\ D_{2N} \end{bmatrix} \text{ where from the zoom the useful quantity is } S_N = 10^{40N}.$$

**Observed Selfsimilarity of Mandelbrot Sets On Next Larger (N+1) And Next Smaller (N) Fractal Scales**(we live in between these two scales)at the Fiegenbaum point

## 2.2 Fractal Invariants

Speed of light  $c$  is a fractal invariant, stays the same in going from one fractal scale to another since  $dr$  and  $dt$  (in  $c=dr/dt$ ) change the same as you go through  $r_H$  branch cut. Note nontrivial (eq.1.16a) eignefunction is  $\delta z = -1$  for  $C \rightarrow 0$  so given  $z=1+\delta z$  then  $\delta z \delta z = (-1)(-1) = drdr = ds^2 = 1$  in the large  $N+1$  fractal baseline  $C \rightarrow 0$  limit so since  $ds^2$  is invariant for all angles then  $ds=1$  from selfsimilarity of the small  $N$ th and large  $N+1$  th fractal baselines so  $ds$  in eq.2 is also a fractal invariant. With  $c$  and  $ds$  both invariants in eq.11 we have 11 giving us the Hermitian operators with associated eq.16 eigenfunction Hilbert space.

It is well known that information is stored as horizon  $r_H$  surface area  $= 4\pi r_H^2 = 4\pi(10^{40})^2 \approx 10^{81}$  thus giving us our appendix A counting limit.

## 2.3 section 2 addendum $C_M$ Fractal Consequences

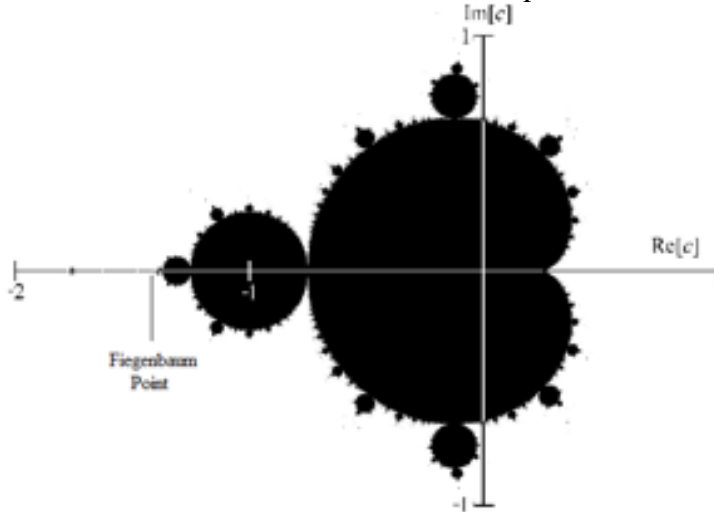


fig. 9

Note that the center of mass (COM, fig.9) is at the (negative inverse of the) golden mean  $-0.618033.. (= -1/\phi)$  and is also a solution of our equation 2 written as  $z=zz-1$ . So  $C=-1$ .  $-1$  is right in the middle of the biggest circle above. Given this goofy  $(-1/\phi)$  is also at the average of the Mandelbrot set the golden mean seems to be connected to the Mandelbrot set. But this result doesn't mean anything because we need the  $\delta C=0$  extremum at the Fiegenbaum point  $= -1.40115..$ , (and  $C=-1/4$ ) not the average position of the Mandelbrot set.

### 2.3 {{neighborhood $C_M \cap \{-r \text{ axis}\}}$ } $-dr$ Fractal Branch Cut

Recall section 1 and the derivation of the fractal space time. So there is more to these 2D complex number solutions to eq.3 than just irrational and rational numbers, there is also this underlying space-time fractal structure  $\{\text{neighborhood}\{C_M\} \cap \{-r \text{ axis}\}\}$  that contains even fewer elements than the rational numbers and which only "exists" when the "fog" is not thick, i.e. when  $C$  goes to 0. It permeates all of space and yet has zero density. It is a very mysterious subset of the complex plane indeed.

Note to be a part of what is postulated (eq.3)  $C \rightarrow 0$  we must be in the neighborhood of the tip of the horizontal Mandelbrot set  $dr$  axis with extremum given by the circle lemniscate fig.7. But from the perspective (scale) of this  $N+1$  th scale observer one of the  $10^{40}X$  smaller ( $N$ th fractal scale)  $45^\circ$  rotated Mandelbrot sets (fig.8) is still near his own  $dr$  axis putting it within the  $\epsilon, \delta$  limit neighborhoods of  $C \rightarrow 0$  of eq.2. Thus in this narrow context we are allowed the  $45^\circ$  rotations to the extremum directions of the solutions of equation 2. Thus we also have the Riemann surfaces of fig.4 if we continue our rotations beyond  $360^\circ$ . Our  $C$  increases (eg.,  $C \rightarrow 0$ ) discussed later sections are also all in this  $N$ th fractal scale context. For example eq. 7 is then reachable on the  $N$ th fractal scale ( $r > r_H$ ) as a noise object ( $C > 0$ ). So 8 at  $135^\circ$  must then also

result from noise ( $C > 0$ ) introduction and so from that first fractal jump rotation in the 2D plane. Later we even note a limit on  $C$  (sect.4.3.1).

## 2.4 Fourier Series Interpretation Of $C_M$ Solution

Recall from equation 7 that on the diagonals we have particles (and waves) and on the  $dr$  axis where  $C=0$  only waves, see A1 Recall 2AC solution  $dr=dt$ ,  $dr=-dt$  gives 0 as a solution and so  $C=0$ . But in equation 2 for  $C \rightarrow 0$   $\delta z=0, -1$ . So eq.3 implies the two points  $\delta z=0, -1$ . So for waves to give points implies a Fourier superposition of an infinite number of sine waves and so wave lengths. In terms of eq.7 these are solutions to the Dirac equation and so represent fractalness, smaller wave lengths inside smaller wavelengths. So it is fractal.

### S states

Need boosted  $C$  small in  $z=zz+C$  or the postulate of 1 does not hold. So need boost so  $C_M/\xi_1=C$  is small so with  $\xi_1$  big with  $\xi_0$  stable core (electron) mentioned above..

For  $z=1$   $\xi_1$  is big so  $\tau, \mu, e$  can be free S states (since  $\xi_1=\tau+\mu+e$  is still in denominator of the  $C=C_M/\xi_1$  for each of  $\tau, \mu$  and  $m_e$  so  $C$  is still small for each. This same effect also makes leptons (nearly) point sources whereas baryons are not (with their much larger  $r_H$  radius

## 2.5 Observer-object alternative way (to iterating eq.2) to understand fractalness

Recall also that eq.7 has two solution and associated two points one of which we define as the observer. In the new pde:  $\sqrt{\kappa_{\mu\mu}}\gamma^\mu\partial\psi/\partial x_\mu=(\omega/c)\psi$  16, (given that it requires these two points), we allow the observer to be anywhere. So just put the observer at  $r < r_H$  and you have derived your fractal universe in one step without iterating eq.2 as we did at the outset. To show this note from equations 14 we have the Schwarzschild metric event horizon of radius  $R \equiv 2Gm/c^2$  in the  $M+1$  fractal scale where  $m$  is the mass of a point source. Also define the null geodesic tangent vector  $K^m$  to be the vector tangent to geodesic curves for light rays. Let  $R$  be the Schwarzschild radius or event horizon for  $r_H=2e^2/m_e c^2$ . Thus (Hawking, pp.200) in the case that equation applies we have:  $R_{mn}K^m K^n > 0$  for  $r < R$  in the Raychaudhuri ( $K_n$ =null geodesic tangent vector) (4.5.1) equation. Then if there is small vorticity and shear there is a closed trapped surface (at horizon distance “ $R$ ” from  $x$ ) for null geodesics. No observation can be made through such a closed trapped surface. Also from S.Hawking, *Large Scale Structure of Space Time*, pp.309...instead he will see O’s watch apparently slow down and asymptotically (during collapse) approach 1 o’clock...”. So  $g_{rr}=1/(1-r_H/r)$  in practical terms never quite becomes singular and so we cannot observe through  $r_H$  either from the inside or the outside (space like interval, not time like) as long as the bigger horizon  $r_H$  is isolated (for nearby object B there is some metric perturbation). Note we live in between fractal scale horizon  $r_H=r_{M+1}$  (cosmological) and  $r_H=r_M$  (electron). Thus we can list only two observable (Dirac) vacuum Hamiltonian sources (also see section 1).

$H_{M-1}$  and  $H_M$

But we are still entitled to say that we are made of only ONE “observable” source i.e.,  $r_H$  of equation 13 (which we can also observe from the inside (cosmology) and study from the outside (particle physics). Thus this is a Ockam’s razor optimized unified field theory using:

**ONE** “observable” source

of nonzero proper mass which is equivalent to our fundamental postulate of equation 1. Metric coefficient  $\kappa_{rr}=1/(1-r_H/r)$  near  $r=r_H$  (given  $dr'^2=\kappa_{rr}dr^2$ ) makes these tiny  $dr$  observers just as big as us viewed from their frame of reference  $dr'$ . Then as observers they must have their own  $r_{HS}$ , etc. . You might also say that the fundamental Riemann surface, and Fourier superposition are therefore the *source* of the “observer”.

Recall we get  $\min(zz-z)>0$  from that and 1 as a explicit real observable which goes back to the implicit real observable 1 we started with.

Anthropomorphic **Observer implications of CM solution and eq.7**

### Review

Recall the algebraic definition of **1** is  $z=zz$  (with noise)

i.e.,  $z=zz$  (eq.1),  $z'=z'z'+C$ ,  $dC=0$  (eq.2)

Solve eqs.1,2 for  $C, z'$ .

Start with eq.1 solutions  $z=0$ ,  $z=1$ .

**$z=0$**  For  $z=0$  to find  $C$  itself substitute  $z'$  on left (eq.2) into right  $z'z'$  repeatedly & get iteration

$z_{N+1}=z_N z_N - C$ .  $\delta C=0$  requires us to reject the  $C$ s for which  $-\delta C = \delta(z_{N+1} - z_N z_N) = \delta(\infty - \infty) \neq 0$  **(eq.3)**

The leftover  $C$ s are the Mandelbrot set  $C=CM$  with the smaller fractal scale providing a  $\Delta = CM'$  perturbation.

**$z=1$**  plug in  $z'=1+dz$  [since  $z=0 \rightarrow z=0+\Delta$ ]  $\delta z + \delta z \delta z = C$

with solution  $\delta z = \frac{-1 \pm \sqrt{1-4C}}{2} = \delta z = dr + idt$  **(eq.4)**

into eq.2 and get Dirac eq. for  $e, v$ .

steps  **$z=0, z=1$**  together give you the Newpde.

## 2.6 Observer (humanity) Implications

Eq.4 just above gives you space time  $(r, t)$ , required by physical reality (creation) and eq. 4 is clearly dependent on that  $C=CM$  Mandelbrot set.

But the Mandelbrot set  $CM$  depends on that interesting connection with  $\infty - \infty$  in above equation 3. Normally in physics an infinite quantity is really just a very large quantity, but not here: we actually connected to infinity! Thus Creation itself is caused by *this* (eq.3) extremely sublime *relation with Ainfinity*! So we understand creation at the deepest possible level.. Understanding creation itself makes life worth living, makes humanity *unique* among all physical things.

Also since Newpde equation 16 is essentially all there is there is then also the above (sect.2.5) anthropomorphic (i.e., observer) based derivation of that fractalness using equation 7 that requires both the observer and object to solve eq.5. (Postulate 1 and so equation 5 is not solved unless **both parts** of equation 7 hold). There is then a powerful ethics lesson that comes out of this result (eg., negation of solipsism (of sociopathology) part V): ethical equality of observer and observed (i.e., golden rule).

Also the postulate of 1 reminds us of Paul Tillich's 'One' ultimate truth, ground of being.

So we just found that "life is worth living" and "reason to act ethically" (but cautiously toward solipsists (sociopaths) who consider themselves the only observers), so be kind: These are unexpected but wonderful results coming out of the **postulate 1**  $\rightarrow$  **Newpde**.

## Ch.3 Quantum Mechanics Is The Newpde $\psi$ (for each $N$ fractal scale)

**Also** Equation 4, **2D Isotropic and Homogenous Space-Time vs A B3**

Review: Recall we used a **successive approximation (to  $z=0$ )** in solving eqs.1,2.

$N=-1$   $C_M \equiv \Delta$  extremum solution  $\|\Delta\| \ll 1$  *must perturb  $z \approx 0$*  with  $C_M \equiv \delta z' = \Delta$  given  $\delta z' \delta z' \ll \delta z'$  for this  $|\delta z'| \ll 1$  in eq.3. So  **$0 \approx z' \approx 1 + \delta z$** ,  $\delta z = -1 + \Delta$  (4a) in eq.3:  $\delta(\delta z + \delta z \delta z) = \delta \delta z(1)$

$+ 2\delta \delta z(\delta z) = \delta \delta z(1) + 2(\delta \delta z)(-1 + \Delta) = \delta \delta z(-1 + 2\Delta) = \frac{1}{2}\delta(\delta z \delta z) + \delta \delta z \Delta \approx \frac{1}{2}\delta(\delta z \delta z) = 0 = (\text{plug in}$

eq.4) =  $\delta\delta z\Delta + \frac{1}{2}\delta[(dr+idt)(dr+idt)]$  (If  $\delta z C^2$  at least locally  $\delta\delta z=0$ )  $\approx \frac{1}{2}\delta[(dr^2-dt^2) + i(dr dt + dt dr)] = 0$  (5)

**Factor eq.5**  $\delta(dr^2-dt^2) = \delta[(dr+dt)(dr-dt)] = 0 = [[\delta(dr+dt)](dr-dt)] + [(dr+dt)[\delta(dr-dt)]] = 0$  (6)  
 so  $(\rightarrow \pm e)$   $dr+dt=ds$ ,  $dr-dt=ds \equiv ds_1$  for  $+ds \rightarrow$  I, IV quadrants Fig3 (7)

Note these quadrants are used in appendix A. Also note the positive scalar  $dr dt$  of eq.7 (since I<sup>st</sup> quadrant) implies the eq.5 *non* infinite extremum **imaginary**  $dr dt + dt dr = 0 = \gamma^i dr \gamma^j dt + \gamma^j dt \gamma^i dr = (\gamma^i \gamma^j + \gamma^j \gamma^i) dr dt$  so Clifford algebra  $(\gamma^i \gamma^j + \gamma^j \gamma^i) = 0, i \neq j$ . (7a)

$(\rightarrow \text{light cone } v)$   $dr+dt=ds$ ,  $dr=-dt$ , for  $+ds \rightarrow$  II quadrant (8)

“ “  $dr-dt=ds$ ,  $dr=dt$ , “ “ III quadrant (9)

$(\rightarrow \text{vacuum}, z=1)$   $dr=dt$ ,  $dr=-dt$  so  $dt=0=dr$  (So eigenvalues of  $dt$ ,  $dr=0$  in eq.11) (10)

**We square eq.7**  $ds_1^2 = (dr+dt)(dr+dt) = [dr^2+dt^2] + (dr dt + dt dr) \equiv ds^2 + ds_3 = ds_1^2$ . Since  $ds_3$  (is max or min) and  $ds_1^2$  (from eq.7) are invariant then so is **Circle**  $ds^2 = dr^2 + dt^2$  Recall this led to the eq.11 observability condition and the new pde  $\psi$  function core of QM. The circle implies the isolated lemniscate(circle) definitions (sect.2.2) of each Mandelbrot set implying a finite extremum of the set.

## Implications for QM

### B3 Quantum Mechanics Is The Newpde $\psi$ (for each N fractal scale)

Recall the solution to (postulate 1)  $z=zz$  is **1, o**. In  $z=1-\delta z$ ,  $\delta z^* \delta z$  is (defined as) the probability of  $z$  being **o**. Recall  $z=o$  is the  $\xi_o = m_e$  solution to the new pde so  $\delta z^* \delta z$  is the probability we have just an electron (sect.3). Note  $z=zz$  also thereby conveniently provides us with an automatic normalization of  $\delta z$ . Note also that  $(\delta z^* \delta z)/dr$  is also then a one dimensional probability ‘density’. So Bohr’s probability density “postulate” for  $\psi^* \psi (\equiv \delta z^* \delta z)$  is derived here. It is not a postulate anymore. (So Bohr was very close to the postulate of 1, and so using  $z=zz$  here.)

Note the electron eq.7 has *two* parts (i.e.,  $dr+dt$  &  $dr-dt$ ), that solve eq.3 *together*, same kind of  $\delta(p_A - p_B)$  conservation relation as between Alice and Bob; signal, idler, Bell’s stuff. We could then label these two parts *observer* and *object* with associated eq.7 wavefunctions  $\delta z \equiv \psi_1$ ,  $\delta z \equiv \psi_2$ . So if there is no observer eq.7 (So no  $\psi_1$ ) then eq.3 doesn’t hold at all and so there is no object “observed” wavefunction.  $\psi_2$ . Thus the object wave function  $\psi_2$  “collapses” to the wavefunction ‘observed’  $\psi_2$  (or eq.5 and so **postulate 1** does not even hold), if “observed”  $\psi_1$  exists. Then apply the same mathematical reasoning to every other  $\delta(p_A - p_B)$  situation and we will also have thereby derived Bell’s theorem and its general cases. Thus we derived the Copenhagen interpretation of Quantum Mechanics QM mathematically, from eq.16 and so first principles **postulate 1**, not from the usual hand waving arguments.

Recall from appendix A  $dr^2 + dt^2$  is a second derivative *operator* wave equation(A1), that holds all the way around the circle (even for the eq.10 vacuum solutions), gives waves. In eq.12, error magnitude C (sect.2.3) is also a  $\delta z$ ’ angle measure on the  $dr, idt$  plane. One extremum  $ds$  ( $z=0$ ) is at  $45^\circ$  so the largest C is on the diagonals ( $45^\circ$ ) where we have eq.4 extremum holding: particles. So a wide slit has high uncertainty, so large C (rotation angle) so we are at  $45^\circ$  (eg., particles, eq.16 photoelectric effect). For a *small slit* we have less uncertainty so smaller C, not large enough for  $45^\circ$ , so only the *wave equation* A1 holds (small slit diffraction). Thus we derived wave particle duality here.

Recall wave equation eq.A1 iteration of the New pde with eq.11 operator formalism. So  $dr/ds = k$  in the sect.1  $\delta z = ds e^{i\theta}$  exponent then becomes  $k = 2\pi/\lambda$ . Multiplying both sides by  $\hbar$  with  $\hbar k \equiv mv$  as before we then have the DeBroglie equation that relates particle momentum to wavelength in quantum mechanics. Equation 8a (sect.1) then counts units N of  $(dt/ds) = \hbar \omega = \hbar ck$  on the diagonal



so that  $E=p\hbar\omega$  for all energy components, universally. Thus this eq.11a counting  $N$  does not require the (well known) quantization of the E&M field with SHM. First, set the unit of distance  $r_H$  on our baseline fractal scale: (eq.1  $N=0$ . See figure 1 attachment.).The lemniscate Mandelbrot set formulation allows only these finite extremum.

**Quantum mechanics is also fractal.** In that regard recall that (from sect.1)

the postulate of 1 frame of reference (i.e.,small  $C$ ) *only* allows (ground state)  $r' = CM/\xi_1$  for stationary electron *and* composite  $3e$  positron which implies  $\gamma=2X917$ . The central electron then sees the  $r_H=2e^2/m_e c^2$  which is a factor of  $2\gamma$  bigger

**Fractal Planck's constant**

Recall that  $Gm_e^2/ke^2=6.67X10^{-11}(9.11X10^{-31})^2/9X10^9X1.6X10^{-19}=2.4X10^{-43}$ .  $2.4X10^{-43}X2m_p/me=2.4X10^{-43}X(2(1836))=2.2X10^{-40}$ . We rounded this to  $10^{-40}$  which was read off the Mandelbrot set (observable circle) **zoom** as the ratio of the two successive Mandelbrot set lengths.

Recall in eq.12  $r_H=CM/\xi=ke^2/m_e c^2$ .  $C_M$  is the Fiegenbaum point= $-1.40115(10^{40N})$ ,  $N=..,-1,0,1,..$ =fractal scale,  $m_e$ =electron mass. Solve for  $m_e$  in  $m_e c^2=ke^2/r_H$ . From the Dirac equation (Newpde) double Einstein relation  $hf=2m_e c^2$  we then solve for  $h$  (using  $m_e f'=10^{-40}f$  and  $m_e'=10^{-80}m_e$ ) *outside*  $r_H$ .

$h=(m_e/f)2c^2$ . Solve for  $h$ , Planck's constant *outside*  $h_{N=-1}=h_N 10^{-80}/10^{-40}=h_N 10^{-40}$

Note here then that  $h$  is directly proportional to  $C_M$  and  $C_M$  is fractal  $\propto 10^{40N}$  so Planck's constant is fractal  $h_N$ .

Note for  $N=-1$   $m$  is small so  $v$  is large ( $\approx c$ ). Next plug this result into the uncertainty principle  $\Delta x \Delta (mc) \geq \hbar$ . So

**Different Fractal Quantum Mechanics implied by Mixed State Contributions Outside  $r_H$**

A)  $m_{N-1}$  *inside*  $r_{HN-1}$  uses  $h_{N-1}$  (eg.,  $[\Delta x \Delta (m_{N-1})]c = h_{N-1}$ ).  $h_{N-1}f = m_{N-1}c^2$ . (Usual fractal result. Fractal universe implies  $(10^{-40}\Delta x)(10^{-80}m_e c) = h 10^{-120} \propto$ energy density accounting for that  $10^{120}X$  discrepancy in the qed cosmological constant  $\Lambda$  with GR's (See also sect.7.6.).

B)  $m_{N-1}$  *outside*  $r_{HN-1}$  uses  $h_{N=1}=10^{-40}h$ . (eg.,  $[\Delta x \Delta (m_{N-1})]c = h_{N=1}$  (large  $\Delta x$ )  $\Delta x 10^{-80}m_e c = 10^{-40}h$  then  $\Delta x$  is the size of the universe ( $\sim 10^{12}LY$ ) and tiny  $f$  the frequency of oscillation of the universe. This is also our old Newpde  $N=1$  case. But for the mixedstate muon  $1S_{1/2}$  component  $m_{\mu N-1}$ , frame of reference  $f$  is about  $10^5$  year period oscillation and  $\Delta x = \Delta r = 10^5 LY$  is the size of a galaxy. Note this  $N=-1$  case is gravitational.

Note also that  $mv^2/r = kGM/r$  comes from a field with local cylindrical symmetry so that  $r$  cancels out allowing us to set  $g_{00} = \kappa_{00}$  which results in orbital stability. So a mixed pancake shaped  $1S_{1/2}$  state uncertainty cloud in the plane of the galaxy provides gravitational stability for planar structures of this size since it implies the cylindrical symmetry  $g_{00} = \kappa_{00}$  case in the halo and so metric quantization stability for this shape.(see partIII). Other shapes can exist but they are not as stable and so eventually the flat  $1S_{1/2}$  state prevails. Note (from partIII) 100km/sec is this  $S$  state metric quantization, 200km/sec  $P$  state (barred spiral) metric quantization (so internal square symmetry). If the galaxy  $\Delta r$  gets too large case B above is no longer realized and so the  $1S_{1/2}$  state is gone and so the pancake cylindrical symmetry (shape) goes away and so  $g_{00} \neq \kappa_{00}$  and so the cylindrical shape (metric quantization) stability goes away and so this flat spiral shape disappears and we only have an high entropy elliptical (galaxy) shape left. So we have explained, with this Planck's constant analysis, why both the universe and (the evolution of) galaxies exist! Also we have shown that Planck's constant is fractal!



So given all these properties of eq.11 New pde  $\psi$  we really have derived Quantum Mechanics.

## Thermodynamics

Note that a "single state  $\delta z$  per particle" comes out of 1 particle per  $\delta z$  state per solution in 11 and eq.16. So the number of ways  $W$  of filling  $g_i$  single states with  $n_i$  particles is  $g_i!/(n_i!(g_i-n_i)!)$  thereby giving us  $k \ln W \equiv S$  and so thermodynamics.

### The Most General (noise) Uncertainty C In Eq.1 Is Composed Of Markov Chains

This final variation wiggling around inside  $dr =$  error region near the Fiegenbaum point also implies a  $dz$  that is the sum of the total number of all possible individual  $dz$  as in a *Markov chain* (In that regard recall that the Schrodinger equation free particle Green's function propagator mathematically resembles Brownian motion, Bjorken and Drell) where we in general let  $dt$  and  $dr$  be either positive or negative allowing several  $\delta z$  to even coexist at the same time (as in Everett's theory and all possible paths integration path integral theories below). Recall  $dt$  can get both a  $\sqrt{(1-v^2/c^2)}$  Lorentz boost (with the nonrelativistic limit being  $1-v^2/2c^2 + \dots$ ) and a  $1-r_H/r = \kappa_{00}$  contraction time dilation effects here. In section 2.2.6 we note that for a flat space Dirac equation Hamiltonian the potentials are infinite implying below an unconstrained Markov chain and so unconstrained phase in the action So  $dt \rightarrow dt\sqrt{(1-v^2/c^2)}\sqrt{\kappa_{00}}$ .  $r_H = 2e^2/(m_e c^2)$ . We also note the alternative (doing all the physics at the point  $ds$  at  $45^\circ$ ) of allowing  $C > C_1$  to wiggle around instead between  $ds$  limits mentioned above results in a Markov chain.

$dZ = \psi \equiv \int dz = \int e^{i d\theta} dc = \int e^{i dt/so} dc = \int e^{i dt/\sqrt{(1-v^2/c^2)}\sqrt{\kappa_{00}}/so} ds' ds..$  In the nonrelativistic limit this result thereby equals  $\int e^{i k e^{i k dt(v^2-k/r)} = \int e^{i k (T-V) dt} ds' ds... = \int e^{i S} ds' ds \equiv dz_1 + dz_2 + .. \equiv \psi_1 + \psi_2 + ..$  many more  $\psi$ s (note  $S$  is the classical action) and so integration over all possible paths  $ds$  not only **deriving the Feynman path integral but also Everett's alternative** (to Copenhagen) many worlds (i.e., those above many Markov chain  $\delta z_i = \psi$ s in  $\int dz = \psi \equiv \psi_1 + \psi_2 + ..$ ) interpretation of quantum mechanics where the possibility of  $-dt$  allows a pileup of  $\delta z$ s at a given time just as in Everett's many worlds hypothesis. But note equation 9 curved space Dirac equation does not require infinite energies and so unconstrained Markov chains making the need for the path integral and Everett's many worlds mute.: We don't need them anymore. Thus we have derived both the Many Worlds (Everett 1957) and Copenhagen interpretations (Just below) of quantum mechanics (why they both work) and also have derived the Feynman path integral.

In regard to the Copenhagen interpretation if we stop our J.S.Bell analysis of the EPR correlations at the quantum mechanical  $-\cos\theta$  polarization result we will not get the nonlocality (But if instead we continue on and (ad hoc and wrong) try to incorporate hidden variable theory (eg., Bohm's) we get the nonlocality, have transitioned to classical physics two different ways. We then have built a straw man for nothing. Just stick with the  $\hbar \rightarrow 0$ , Poisson bracket way. So just leave hidden variables alone. The Copenhagen interpretation thereby does not contain these EPR problems. And any lingering problems come from that fact that the Schrodinger equation is parabolic and so with these noncausal instantaneous boundary conditions. But the Dirac equation is hyperbolic and so has a retarded causal Green's function. Since the Schrodinger equation is a special nonrelativistic case of the Dirac equation we can then ignore these nonlocality problems all together. You take a Log of both sides and use Stirling's approximation and you get the Fermi Dirac distribution for example.

## NONhomogeneous and NONisotropic Space-Time

From equation 3 solution eq.4 we note that this theory is fundamentally 2D. So what consequences does a 2D theory have? We break the 2D degeneracy of eq. 7 at the end by rotating by  $C_M$  (fig.1) and get a 4D Clifford algebra. Recall 7 and 8 are dichotomic variables with the noise rotation  $C$  going from eq.7 at  $45^\circ$  to eq.8 at  $135^\circ$ .

Recall eq.7 implies simultaneous eq.7+eq.8 are  $2D \oplus 2D = 4D$ . But single eq.7 plus single eq.8 are *not* simultaneous so are still 2D. So this theory is still 2D complex  $Z$  then. Recall the  $\kappa_{\mu\nu}$ ,  $g_{\mu\nu}$  metrics (and so  $R_{ij}$  and  $R$ ) were generated in section 1.4.

In that regard for 2D for a homogenous and isotropic  $g_{ij}$  we have identically  $R_{\mu\mu} - \frac{1}{2}g_{\mu\mu}R = 0$  (3.1.1  $\equiv$  source  $= G_{00}$  since in 2D  $R_{\mu\mu} = \frac{1}{2}g_{\mu\mu}R$  identically (Weinberg, pp.394) with  $\mu=0, 1 \dots$  Note the 0 ( $=E_{\text{total}}$  the energy density source) and we have thereby proven the existence of a net zero energy density vacuum. Thus our 2D theory implies the vacuum is really a vacuum! It is then the result of the fractal and 2D nature of space time!

A ultrarelativistic electron is essentially a transverse wave 2D object (eg., the  $2P_{1/2}$  electron in the neutron). In a isotropic homogenous space time  $G_{00}=0$ . Also from sect.2 eqs. 7 and 8 occupy the same complex 2D plane. So eqs. 7+8 is  $G_{00}=E_e + \sigma \cdot p_r = 0$  so  $E_e = -\sigma \cdot p_r$ . So given the negative sign in the above relation the neutrino chirality is left handed.

### 3.1 Casimir Effect

Also for this complex space 2D  $0=G_{00}=E_e + \sigma \cdot p_r$  for two nearby conducting plates the low energy neutrinos can leave (since their cross-section is so low) but the E&M ( $E_e$  standing waves) has to remain with some modes (from the  $\nu$  and anti  $\nu$ ), not existing due to not satisfying boundary conditions, because of outside  $\Delta\epsilon$  ground state oscillations implying less energy between the plates and so a attractive force between them (We have thereby derived the Casimir effect).

*Thus the zero energy vacuum and left handedness of the neutrino in the weak interaction are only possible in this 2D equation 4  $Z$  plane.* If the space-time is not isotropic and homogenous the neutrino must then gain mass  $m_0$  (see section 3.3 for what happens to this mass) and it becomes an electron at the horizon  $r_H$  if it had enough kinetic energy to begin with. It changes to an electron by scattering off a neutron with at  $W^-$  and  $e^-$  resulting along with a proton. So the neutrino transformed into an electron with other decay products. Recall that the electron eq.7 and the neutrino eq.8 are dichotomic variables (one can transform into the other, sect.2) and can share the same spinor as we assumed in section 2. The neutrino in this situation is left handed.  $\gamma^5$  is the parity operator part of the Cabibbo angle calculation.

### 3.2 Helicity Implications 2D Isotropic And Homogenous State

From eq.11  $p_x \psi = -i\hbar \partial \psi / \partial x$ . We multiply equation  $p_x \psi = -i\hbar \partial \psi / \partial x$  in section 1 by normalized  $\psi^*$  and integrate over the volume to *define* the expectation value of operator  $p_x$  for this *observer representation*:

$$\langle p, t | p | p, t \rangle \equiv \int \psi^* p \psi dV$$

(implies Hilbert space if  $\psi$  is normalizable). Or for any given operator 'A' we write in general as a definition of the expectation value:

$$\langle A \rangle = \langle a, t | A | a, t \rangle \quad (3.2.1)$$

The time development of equation 16 is given by the Heisenberg equations of motion (for equation 16. We can even define the expectation value of the (charge) chirality in terms of a generalization of eq.16 for  $\psi_e$  spin  $\frac{1}{2}$  particle creation  $\psi_e$  from a spin 0 vacuum  $\chi_e$ . In that regard

let  $\chi_e$  be the spin0 Klein Gordon vacuum state in zero ambient field and so  $\frac{1}{2}(1 \pm \gamma^5)\psi_e = \chi_e$ .

Thus the overlap integral of a spin  $\frac{1}{2}$  and spin zero field is:

$$\langle \text{vacuum helicity of charge} \rangle \equiv \int \psi_e' \chi_e dV = \int \psi_e' \frac{1}{2}(1 \pm \gamma^5)\psi_e dV \quad (3.2.2)$$

So  $\frac{1}{2}(1 \pm \gamma^5)$  = helicity creation operator for spin  $\frac{1}{2}$  Dirac particle: This helicity is the origin of charge as well for a spin  $\frac{1}{2}$  Dirac particle. See additional discussion of the nature of charge near the end of 3.2 Alternatively, in a second quantization context, equation 3.3.2 is the equivalent to the helicity coming out of the spin 0 vacuum  $\chi_e$  and becoming spin  $\frac{1}{2}$  source charge with  $\frac{1}{2}(1 \pm \gamma^5) \equiv a^\dagger$  being the charge helicity creation operator.

The expectation value of  $\gamma^5$  is also the velocity. Also  $\gamma^i$  (i=x,y,z) is the charge conjugation operator. 3.1.3 Note from section 3.1.1 the field and the wavefunction of the entangled state are related through  $e^{i\text{field}} = \psi = \text{wavefunction}$ .  $\gamma^i \sqrt{(\kappa_{rr})} \partial / \partial r (\gamma^i \sqrt{(\kappa_{rr})} \partial \chi / \partial r) = 0$  where  $\psi = (\gamma^i \sqrt{(\kappa_{rr})} \partial \chi / \partial r)$  and  $\frac{1}{2}(1 \pm \gamma^5)\psi = \chi$ .  $\langle \gamma^5 \rangle = v = \langle c/2 \rangle = c/4$  So  $1 \pm \gamma^5 = \cos 13.04 \pm i \sin 13.04$ ,  $\theta = 13.04 = \text{Cabbibo angle}$ .

Here we can then normalize the Cabibbo angle  $1 + \gamma^5$  term on that 100km/sec object B component of the metric quantization. We then add that CP violating object C 1km/sec as a  $\gamma^5 X \gamma^i$  component. You then get a normalized value of .01 for CKM(1,3) and CKM(3,1).

The measured value is .008.

## Review

### Vacuum eq.10

Recall some solutions to eq.10 gives us a vacuum solution as well. Also recall eq.1.1, 1.2 bis 2D. Recall the  $\kappa_{\mu\nu}$ ,  $g_{\mu\nu}$  metrics (and so  $R_{ij}$  and  $R$ ) were generated in above section 1.2.5. In that regard for 2D for a homogenous and isotropic  $g_{ij}$  we have identically  $R_{\mu\mu} - \frac{1}{2}g_{\mu\mu}R = 0 \equiv \text{source} = G_{00}$  since in 2D  $R_{\mu\mu} = \frac{1}{2}g_{\mu\mu}R$  identically (Weinberg, pp.394) with  $\mu=0, \dots$ . Note the 0 ( $G_{00} = E_{\text{total}}$  the energy density source) and we have thereby proven the existence of a net zero energy density eq.9 vacuum. Thus our 2D theory implies the **vacuum is really a vacuum**.

### Left handedness

From sect.1 eqs.7 and 8 and 9 are combined. Note also from section 1.4 C rotation in a homogenous isotropic space-time. So eqs. 7+8 =  $G_{00} = E_e + \sigma \bullet p_r = 0$  so  $E_e = -\sigma \bullet p_r$ . So given a positive  $E_e$  (AppendixB) and the negative sign in the above relation implies the neutrino chirality  $\sigma \bullet p$  is negative and therefore is left handed.

### 3.3 Nonhomogenous NonIsotropic Mass Increase For eq.7

But a free falling coordinate system in a large scale gravity field is equivalent to a isotropic and homogenous space-time and so even in a spatially large scale field the neutrino has negligible mass if it is free falling.

To examine the effect of all three ambient metric states 1,  $\varepsilon$ ,  $\Delta\varepsilon$  we again start out with a set of initial condition lines on our figure 3. In this case recall that in the presence of a nonisotropic non homogenous space time we can raise the neutrino energy to the  $\varepsilon$  and repeat and get the muon neutrino with mass  $m_{0v} = (3\text{km}/1\text{AU})m_e = .01\text{eV}$  (for solar metric inhomogeneity. See Ch.3 section on homogenous isotropic space time). So start with eq. 2AII singlet filled  $135^\circ$  state  $1S_{\frac{1}{2}}$ . In that well known case  $E = \sqrt{(p^2c^2 + m_0^2c^4)} = E = E(1 + (m_0^2c^4/2E^2))$ .  $E' \approx E \approx pc \gg m_0c^2$ ;  $\psi = e^{i(\omega t - kx)}$  with  $k = p/\hbar = E/(\hbar c)$ . Set  $\hbar = 1, c = 1$  so  $\psi = e^{i(\omega t - kx)} e^{ixm_0^2/2E^2}$ . So we transition through the given  $\psi_{ev}, \psi_{\bar{e}v}, \psi_{1v}$  masses (fig.6, section 6.7) as we move into a stronger and stronger metric gradient. (strong gravitational field) =  $\psi$  electron neutrinos can then transform into muon neutrinos. Starting with

a isotropic homogenous space time in the ground state we then we go into steeper metric gradients in a inertial frame as seen from at constant metric gradient and higher energies thereby the rest of the states fill consecutively. We apply this result to the derivation of the eq.7+7+7 proton in section 8.1, starting out with infinitesimal eqs. 8+8+8 mass and going into the region of high nonisotropy, non homogeneity close to object B, thereby gaining mass in the above way. This process is equivalent to adding noise C to eq.8.

## Chapter 4 Simultaneous (union) Broken 2D Degeneracy $C_M$ rotation of eq. 7 Implies $2D \oplus 2D = 4D$

### 4.1 Details of $2D \oplus 2D$ formulation of eqs. 7+7

We do a rotational self similarity dyadic coordinate transformation of  $\kappa_{\mu\nu}$  to get the Kerr metric which is all we need for our GR applications. So from eqs.4,5,14,15 we found the relation

between  $x_i, x_j$  pairs:  $(\sum_{i=1}^2 \gamma^i \sqrt{\kappa_{ii}} dx_i)^2 = \sum_{i=1}^2 \kappa_{ii} d^2 x_i$  (14a). So given this added  $2D \Delta$  perturbation we get curved space  $2D \otimes 2D = 4D$  independent  $x_1, x_2 \rightarrow x_1, x_2, x_3, x_4$ . Also assuming orthogonality  $dr^2 \equiv dx_1^2 + dx_2^2 + dx_3^2$  (as  $r \rightarrow \infty$  in eq.13,15) the right side of eq.14a therefore has the 2 in the sum replaced by a 4 implying the left side then has to be in eq.14a for the 2D form to be a special case (of any 2  $x_i x_j$ ): Imposing orthogonality thereby creates 6 pairs of eqs.4&5. So eq.14a becomes:  $(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 + \kappa_{tt} dt^2 = ds^2$ .

Multiplying the bracketed term by  $1/ds$  &  $\delta z \equiv \psi$  so eq 11 implies 4D Newpde (lemniscates 2.1):

$$\gamma^\mu (\sqrt{\kappa_{\mu\mu}}) \partial \psi / \partial x_\mu = (\omega/c) \psi \quad \text{for } e, \nu, \quad \kappa_{00} = 1 - r_H/r = 1/\kappa_{rr} \quad r_H = e^2 X 10^{40} N/m \quad N(= -1, 0, 1), \quad (16)$$

So the solution 2 rotation by  $C_M$  at  $45^\circ$  (eq.12) causes the two simultaneous eq.7 electron terms to have different  $dr, dt$ . since the random C can be different in each case. These 2 new degrees of freedom for the only particle with nonzero proper mass in this theory are what create the 4D we observe.

The two 2D plane simultaneous solutions of eq.7 then imply  $2D + 2D = 4D$  thereby allowing for a imbedded 3D spherical symmetry. So we can without loss of generality use the Cartesian product  $(dr, dt)X(dr', dt') = (dr, dt)X(d\phi, d\theta)$  to replace  $r \sin \theta d\phi$  with  $dy$ ,  $rd\theta$  with  $dz$ ,  $cdt$  with  $dt'$  as in  $ds^2 = -dr^2 - r^2 \sin^2 \theta d^2 \phi - r^2 d^2 \theta + c^2 dt^2 \equiv -dx^2 - dy^2 - dz^2 + dt'^2$ . Note the two  $r, t$  and  $\theta, \phi$ , sets of coordinates are written self consistently as a Cartesian product  $(AXB) = (r, t, \phi, \theta)$  space. where  $r, t \in A$  and  $\phi, \theta \in B$ .

Note the orthogonal space of  $\theta, \phi$  with the  $\phi = \omega t'$  carrying the second time dependence (note there are two time dependent parameters in  $(dr, dt)X(dr', dt')$ ). Given the intrinsic 2D applied twice in the Cartesian product the covariant derivative is equal to the ordinary derivative in the operator formalism. Thus here  $[\sqrt{(\kappa_{rr})} dr] \psi = -i [\sqrt{(\kappa_{rr})} (d\psi/dr)]$  replaces the old operator formalism result  $(dr) \psi = -i d\psi/dr$  in the old Dirac equation allowing us to then multiply by the same  $\gamma$  in  $\gamma^r [\sqrt{(\kappa_{rr})} dr] \psi = -i \gamma^r [\sqrt{(\kappa_{rr})} (d\psi/dr)]$ . So using this substitution we can use the same Dirac  $\gamma^x, \gamma^y, \gamma^z, \gamma^t$  s that are in the old Dirac equation.

### 4.2 $ds^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 + \kappa_{tt} dt^2$ For spherical Symmetry From reference 2

Pedagogical method of deriving new pde

Here we easily show that our new pde (eq.16) is generally covariant since it comes out of this 4D Pythagorean Theorem reference 2, section 1.

$\kappa_{xx} = \kappa_{yy} = \kappa_{zz} = -1, \kappa_{tt} = 1$  in Minkowski flat space, Next divide by  $ds^2$ , define  $p_x \equiv dx/ds$ , so get

$$\kappa_{xx}p'_x{}^2 + \kappa_{yy}p'_y{}^2 + \kappa_{zz}p'_z{}^2 + \kappa_{tt}p'_t{}^2 = 1$$

To get eq.2.1.3 we can then linearize like Dirac did (however we leave the  $\kappa_{ij}$  in. He dropped it).

$$\text{So: } (\gamma^x \sqrt{\kappa_{xx}} p_x + \gamma^y \sqrt{\kappa_{yy}} p_y + \gamma^z \sqrt{\kappa_{zz}} p_z + i\gamma^t \sqrt{\kappa_{tt}} p_t)^2 = \kappa_{xx} p_x^2 + \kappa_{yy} p_y^2 + \kappa_{zz} p_z^2 + \kappa_{tt} p_t^2 \quad (4.2.1)$$

So just pull the term out of between the two ( ) lines in equation 2.1.3 and set it equal to 1 (given  $1*1=1$  in eq.1) to get eq.14 in 4D and divide by  $ds$

$$\gamma^x \sqrt{\kappa_{xx}} p_x + \gamma^y \sqrt{\kappa_{yy}} p_y + \gamma^z \sqrt{\kappa_{zz}} p_z + i\gamma^t \sqrt{\kappa_{tt}} p_t = 1$$

and multiply both sides of that result by the  $\psi$  and write this linear form of equation 14a as its own equation:

$$\gamma^x \sqrt{\kappa_{xx}} p_x \psi + \gamma^y \sqrt{\kappa_{yy}} p_y \psi + \gamma^z \sqrt{\kappa_{zz}} p_z \psi + i\gamma^t \sqrt{\kappa_{tt}} p_t \psi = \psi$$

Then use eq.4.6. This proves that the new pde (eq.16) is covariant since it comes out of the Minkowski metric for the case of  $r \rightarrow \infty$ .

### 4.3 2 Simultaneous Equations 16: 2D $\oplus$ 2D Cartesian Product, Spherical Coordinates and $\sqrt{\kappa_{\mu\nu}}$

Note from eq.1.11 the  $(dr, dt; dr', dt')$  has two times in it so can be rewritten as

$$(dr, rd\theta, r\sin\theta d\phi, cdt) \equiv (dr, rd\theta, r\sin\theta d\phi, cdt)$$

$$\begin{aligned} dr &= dr & \text{gives} & \gamma^r [\sqrt{(\kappa_{rr})} dr] \psi = -i\gamma^r [\sqrt{(\kappa_{rr})} (d\psi/dr)] = -i\gamma^r [\sqrt{(\kappa_{rr})} (d\psi/dr)] \\ rd\theta &= dy & \text{gives} & \gamma^\theta [\sqrt{(\kappa_{\theta\theta})} dy] \psi = -i\gamma^\theta [\sqrt{(\kappa_{\theta\theta})} (d\psi/dy)] = -i\gamma^\theta [\sqrt{(\kappa_{\theta\theta})} (d\psi/dy)] \\ r\sin\theta d\phi &= dz & \text{gives} & \gamma^\phi [\sqrt{(\kappa_{\phi\phi})} dz] \psi = -i\gamma^\phi [\sqrt{(\kappa_{\phi\phi})} (d\psi/dz)] = -i\gamma^\phi [\sqrt{(\kappa_{\phi\phi})} (d\psi/dz)] \\ cdt &= dt'' & \text{gives} & \gamma^t [\sqrt{(\kappa_{tt})} dt''] \psi = -i\gamma^t [\sqrt{(\kappa_{tt})} (d\psi/dt'')] = -i\gamma^t [\sqrt{(\kappa_{tt})} (d\psi/dt'')] \end{aligned} \quad (4.3.1)$$

For example for the old method (without the  $\sqrt{\kappa_{ij}}$  for a spherically symmetric diagonalizable metric):

$$ds^2 = \{\gamma^x dx + \gamma^y dy + \gamma^z dz + \gamma^t cdt\}^2 = dx^2 + dy^2 + dz^2 + c^2 dt^2 \text{ then goes to}$$

$$ds^2 = \{\gamma^x [\sqrt{(\kappa_{xx})} dx] + \gamma^y [\sqrt{(\kappa_{yy})} dy] + \gamma^z [\sqrt{(\kappa_{zz})} dz] + \gamma^t [\sqrt{(\kappa_{tt})} dt]\}^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 + c^2 \kappa_{tt} dt^2$$

and so we can then derive the same Clifford algebra (of the  $\gamma$  s) as for the old Dirac equation

with the terms in the square brackets (eg.,  $[\sqrt{(\kappa_{xx})} dx] \equiv p'_x$ ) replacing the old  $dx$  in that derivation.

Also here there is a spherical symmetry so there is no loss in generality in picking the  $x$  direction to be  $r$  at any given time since there is no  $\theta$  or  $\phi$  dependence on the metrics like there is for  $r$ .

If the two body equation 7 is solved at  $r \approx r_H$  (i.e., our  $-dr$  axis,  $C \rightarrow 0$  of eq.3) using the separation of variables and the Frobenius series solution method we get the hyperon energy-charge

eigenvalues but here from first principles (i.e., our postulate) and not from assuming those usual

ad hoc qcd gauges, gluons, colors, etc. See Ch.8-10 for this Frobenius series method and also see

Ch.9. Also  $E_n = \text{Rel}(1/\sqrt{g_{00}}) = \text{Rel}(e^{i(2\varepsilon + \Delta\varepsilon)}) = 1 - 4\varepsilon^2/4 + \dots = 1 - 2\varepsilon^2/2 \equiv 1 - \frac{1}{2}\alpha$ . Multiply both sides by  $\hbar c/r$

(for 2 body S state  $\lambda=r$ , sec.16.2), use reduced mass (two body  $m/2$ ) to get  $E = \hbar c/r + (\alpha \hbar c/(2r)) =$

$\hbar c/r + (ke^2/2r) = \text{QM}(r=\lambda/2, 2 \text{ body S state}) + E\&M$  where we have then derived the fine structure

constant  $\alpha$ .

### 4.4 Single eq.7 Source Implies Equivalence Principle And So Allows You To Use Metric $\kappa_{\mu\nu}$ Formalism

Recall that the electrostatic force  $Eq = F = ma$  so  $E(q/m) = a$ . Thus there are different accelerations

'a' for different charges 'q' in an ambient electrostatic field 'E'. In contrast with gravity there is a single acceleration for two different masses as Galileo discovered in his tower of Pisa

experiment. Thus gravity (mass) obeys the equivalence principle and so (in the standard result)

the metric formalism  $g_{ij}$  (eq.7) can apply to gravity.

Note that E&M can also obey the equivalence principle but in only one case: if there is a *single*  $e$  and Dirac particle  $m_e$  in  $Eq=ma$  and therefore (to get the correct geodesics,): Given an equivalence principle we can write E&M metrics such as rewriting 13:

$$\kappa_{00} = g_{00} = 1 - 2e^2/rm_e c^2 = 1 - r_H/r \quad (4.4.1)$$

(with  $\kappa_{rr}=1/\kappa_{00}$ , in section 1.2) and so then trivially all charges will have the same acceleration in the same E field. This then allows us to insert this metric  $g_{ij}$  formalism into the standard Dirac equation derivation instead of the usual Minkowski flat space-time  $g_{ij}$ s (below). Thus by noting E&M obeys the equivalence principle you force it to have ONE nonzero mass with charge. Thus you force a unified field theory on theoretical physics! But eq.7 only applies when you have a equivalence principle. So a metric does not exist for eq.7 for three or more eq.7 objects unless ultrarelativistic motion makes the plates not intersect and so there is the “approximation” of two objects as in part II eqs., 7+7+7.

$ma=eE$  so  $a=(e/m)E$ . Since only the new pde electron has a nonzero proper mass there is only one mass and charge here. So for 2 electrons  $a=(2e/(2m))E=(e/m)E$  we still have the same acceleration. So we can apply the equivalence principle here as well. Even relativistically the mass increases but the E field lines are Fitzgerald contracted and so  $m$  (denominator) gets bigger and  $E$  (numerator) gets bigger so acceleration is still the same! Thus we definitely can apply the equivalence principle to the new pde and so we can use metrics  $\kappa_{\mu\nu}$  with our new pde.

#### 4.5 Implications of $g_{00}=1-2e^2/rm_e c^2=1-eA_0/mc^2 v^0$ In The Low Temperature Limit Of Small Noise C

In fig.2 IVth quadrant could also be a negative velocity electron. So combinations of negative and positive velocity electron (Cooper pairs) are also solutions to eq.1, 2. Solution to eq..3  $z=zz+C$  (where  $C$  is noise),  $z=1+\delta z$  is:

$\delta z = \frac{-1 \pm \sqrt{1-4C}}{2} = dr + idt$ . But if  $C < 1/4$  then  $dt$  is 0 and **time stops** for eq.7. Note eq.7 has two counterrotating opposite velocity (paired) simultaneous components  $dr+dt$  and  $dr-dt$ . Note electron scattering by Cooper pairs is time dependent so the scattering stops and so electrical resistance drops, and so superconductivity ensues, at small enough noise  $C$  or  $v^2$  in  $Adv/dt/v^2$  below.

Or we could as the mainstream does just postulate ad hoc creation and annihilation operators (Bogoliubov) for the Cooper pairs that behave this way and give an energy gap.

In any case ***the time stopping because the noise C is small (in eq.1) is the real source of superconductivity.***

#### Geodesics

Recall equation 4.3.  $g_{00}=1-2e^2/rm_e c^2 \equiv 1-eA_0/mc^2 v^0$ . We determined  $A_0$ , (and  $A_1, A_2, A_3$ ) in appendix A4, eq.A2. We plug this  $A_i$  into the geodesics

$$\frac{d^2 x^\mu}{ds^2} = -\Gamma_{\nu\lambda}^\mu \frac{dx^\nu}{ds} \frac{dx^\lambda}{ds} \quad (4.5.1)$$

where  $\Gamma_{ij}^m \equiv (g^{km}/2)(\partial g_{ik}/\partial x^j + \partial g_{jk}/\partial x^i - \partial g_{ij}/\partial x^k)$

So in general

$$g_{ii} \equiv \eta_{ii} + h_{ii} = 1 - \frac{eA_i(x,t)}{m_e c^2 v^i}, i \neq 0, \quad (4.5.2)$$



$A'_0 \equiv e\phi / m_\tau c^2$ ,  $g_{00} \equiv 1 - \frac{e\phi(x,t)}{m_\tau c^2} = 1 - A'_0$ , and define  $g'_{\alpha\alpha} \equiv 1 - A'_\alpha / v_\alpha$ , ( $\alpha \neq 0$ ) and

$g''_{\alpha\alpha} \equiv g'_{\alpha\alpha} / 2$  for large and near constant  $v$ , see eq. 14 also. In the weak field  $g^{ii} \approx 1$ . Note  $e=0$  for the photon so it is not deflected by these geodesics whereas a gravity field does deflect them. The photon moves in a straight line through a electric or magnetic field. Also use the total

differential  $\frac{\partial g_{11}}{\partial x^\alpha} dx^\alpha = dg_{11}$  so that using the chain rule gives us:

$$\frac{\partial g_{11}}{\partial x^\alpha} \frac{dx^\alpha}{dx^0} = \frac{\partial g_{11}}{\partial x^\alpha} v^\alpha = \frac{dg_{11}}{dx^0} \approx \frac{\partial g_{11}}{\partial x^0}.$$

gives a new  $A(1/v^2)dv/dt$  force term added to the first order Lorentz force result in these geodesic equations (Sokolnikoff, pp.304). So plugging equation 4.5.2 into equation 4.5.1, the geodesic equations gives:

$$\begin{aligned} -\frac{d^2 x^1}{ds^2} &= \Gamma_{11}^1 v_1 v_1 + \Gamma_{12}^1 v_1 v_2 + \Gamma_{13}^1 v_1 v_3 + \Gamma_{10}^1 v_0 v_1 + \Gamma_{21}^1 v_2 v_1 + \Gamma_{22}^1 v_2 v_2 + \Gamma_{23}^1 v_2 v_3 + \Gamma_{20}^1 v_2 v_0 + \\ &\Gamma_{31}^1 v_3 v_1 + \Gamma_{32}^1 v_3 v_2 + \Gamma_{33}^1 v_3 v_3 + \Gamma_{30}^1 v_3 v_0 + \Gamma_{01}^1 v_0 v_1 + \Gamma_{02}^1 v_0 v_2 + \Gamma_{03}^1 v_0 v_3 + \Gamma_{00}^1 v_0 v_0 = \\ &\frac{g^{11}}{2} \left( \frac{\partial g'_{11}}{\partial x^1} \right) v_1 + \frac{g^{11}}{2} \left( \frac{\partial g'_{11}}{\partial x^2} \right) v_2 + \frac{g^{11}}{2} \left( \frac{\partial g'_{11}}{\partial x^3} \right) v_3 + \frac{g^{11}}{2} \left( \frac{\partial g'_{11}}{\partial x^0} \right) v_0 + \\ &\frac{g^{11}}{2} \left( \frac{\partial g'_{11}}{\partial x^2} \right) v_2 - \frac{g^{11}}{2} \left( \frac{\partial g'_{22}}{\partial x^1} \right) v_2 + 0 + 0 + \frac{g^{11}}{2} \left( \frac{\partial g'_{11}}{\partial x^3} \right) v_3 + 0 - \frac{g^{11}}{2} \left( \frac{\partial g'_{33}}{\partial x^1} \right) v_3 + 0 + \\ &\frac{g^{11}}{2} \left( \frac{\partial g'_{11}}{\partial x^0} \right) v_0 + 0 + 0 - \frac{g^{11}}{2} \left( \frac{\partial g'_{00}}{\partial x^1} \right) v_0 + O\left(\frac{A_i dv}{v^2 dt}\right) = v_2 \left( \frac{\partial g''_{11}}{\partial x^2} - \frac{\partial g''_{22}}{\partial x^1} \right) + v_3 \left( \frac{\partial g''_{11}}{\partial x^3} - \frac{\partial g''_{33}}{\partial x^1} \right) + \\ &\left( \frac{\partial g''_{11}}{\partial x^\alpha} v_\alpha + \frac{\partial g''_{11}}{\partial x^0} v_0 \right) - \left( \frac{\partial g''_{00}}{\partial x^1} \right) v_0 + O\left(\frac{A_i dv}{v^2 dx}\right) \approx - \left( \frac{\partial g''_{00}}{\partial x^1} \right) v_0 + v_2 \left( \frac{\partial g''_{11}}{\partial x^2} - \frac{\partial g''_{22}}{\partial x^1} \right) + v_3 \left( \frac{\partial g''_{11}}{\partial x^3} - \frac{\partial g''_{33}}{\partial x^1} \right) \\ &+ O\left(\frac{A_i dv}{v^2 dt}\right) \approx \frac{e}{m_\tau c^2} \left( -\vec{\nabla} \phi + \vec{v} X (\vec{\nabla} X \vec{A}) \right)_x + O\left(\frac{A_i dv}{v^2 dr}\right). \text{ Thus we have the Lorentz force equation form} \\ &\left( - \left( \frac{e}{m_\tau c^2} \right) (\vec{\nabla} \phi + \vec{v} X (\vec{\nabla} X \vec{A})) \right)_x \text{ plus the derivatives of } 1/v \text{ which are of the form: } \mathbf{A}_i (d\mathbf{v}/d\mathbf{r})_{av}/v^2. \text{ This} \end{aligned}$$

**new term  $A(1/v^2)dv/dr$  is the pairing interaction (4.5.3).** This approximation holds well for nonrelativistic and nearly constant velocities and low B fields but fails at extremely low velocities so it works when  $v \gg (dv/dA)A$ . This constraint also applies to this ansatz if it is put into our Maxwell equations in the next section. Recall at the beginning of the BCS paper abstract the authors say that superconductivity results if the phonon attraction interaction is larger than the electrical repulsion interaction

Given a stiff crystal lattice structure (so  $dv/dr$  is large also implying that lattice harmonic oscillation isotope effect in which the period varies with the (isotopic) mass.) this makes the pairing interaction force  $A_i(dv/dr)_{av}/v^2$ . The relative velocity “v” will then be small in the denominator in some of the above perturbative spatial derivatives of the metric  $g_{\alpha\alpha}$  (e.g., the  $1/v$  derivative of  $H_2 (A/v^2)(dv/dr)_{av}$ . This fact is highly suggestive for the velocity component “v” because it implies that at cryogenic temperatures (extremely low relative velocities in normal mode antisymmetric motion) new forces (pairing interactions?) arise from the above general relativity and its spin 0 (BCS) and spin 2 states<sup>i</sup> (D

states for  $\text{CuO}_4$  structure). For example the mass of 4 oxygens ( $4 \times 16 = 64$ ) is nearly the same as the mass of a Cu (64) so that the SHM dynamics symmetric mode (at the same or commensurate frequencies) would allow the conduction electrons to oscillate in neighboring lattices at a relative velocity of near zero (e.g.,  $v \approx 0$  in  $(A/v^2)(dv/dr)_{av}$  making a large contribution to the force), thus creating a large BCS (or D state) type pairing interaction using the above mechanism. Note from the  $dv/dt$  there must be accelerated motion (here centripetal acceleration in BCS or linear SHM as in the D states) as in pair rotation but it must be of very high frequency for  $(dv/dr)_{av}$  (lattice vibration) to be large in the numerator also so that  $v$ , the velocity, remain small in the denominator with the phase of "A" such that  $A(dv/dr)_{av}$  remain the same sign so the polarity giving the A is changing rapidly as well. This explains the requirement of the high frequency lattice vibrations (and also the sensitivity to valence values giving the polarity) in creating that pairing interaction force. Note there should be very few surrounding  $\text{CuO}_4$  complexes, just the ones forming a line of such complexes since their own motion will disrupt a given  $\text{CuO}_4$  resonance, these waves come in at a filamentary isolated sequence of  $\text{CuO}_4$  complexes passing the electrons from one complex to another would be most efficient. Chern Simons developed a similar looking formula to  $A_i(dv/dr)_{av}/v^2$  by trial and error. This pairing interaction force  $A(dv/dt)/v^2$  drops the flat horizontal energy band (with very tiny variation in energy) saddle point (normally at high energy) associated with a particular layer down to the Fermi level making these energies (band gaps) large and so allowing superconductivity to occur.

### Twisted Graphene

Monolayer graphene is not a superconductor by the way.

But what about two layers? For example a graphene bilayer twisted by 1.1deg rotation creates a quasi Moire' pattern with periodic hexagonal lattice.

It is amazing that in this Moire pattern for each hexagonal structure there are carbons far apart inside the hexagon and carbons close together around the edge of the hexagon making these two groups of carbon atoms distinguishable in terms of their bonding lengths.

So how many high density carbons are in the less dense region of the hexagon?

$3+4+5+6+5+4+3=30$ . How many carbons are in the more dense region of the Moire pattern hexagon boundary?  $5 \times 6=30$  again. So these two groups have the same aggregate mass (but are distinguishable) just like the 4 Os and one Cu in the cuprates.

So if you twist one layer of graphene that is on top of another layer by 1.1deg it should become a superconductor. And it is.

This pairing interaction force also lowers the energy gap to near the Fermi level.

$\delta z = [-1 \pm \sqrt{1-4C}]/2$ . If  $C < 1/4$  there is no time and the and so  $dt/ds=0$  and so the scattering Hamiltonian is 0. Thus there is no scattering and so no electrical resistance.

This is the true source of superconductivity.

### High Pressure

The main constituent of these high pressure superconductors is hydrogen.

Chemical bonding strengths change under high pressure so at some given pressure you would expect the heavier element (eg., nitrogen or sulfur) to behave dynamically as though it was a multiple of the mass of hydrogen since all nuclei are ALMOST a multiple of the mass of hydrogen ANYWAY. Thus at some given pressure you are going to have an antisymmetric normal mode (so relative  $v=0$ ) of some integer numbers of hydrogens in that  $F = A dv/dt/v^2$  term.

So if you have N hydrogens with just ONE other lower nucleus atomic mass  $m$  it just takes a small change of the bonding to create that effective mass relation  $Nh=m$  (where N is an integer) since the atomic weight  $m$  is ALMOST a multiple of  $h$  anyway. That antisymmetric normal mode oscillation is then realized. Pressure changes would provide that bonding alteration. For higher

mass nuclei added binding energy mass energy starts making integer N harder to realize. A highly electronegative atom, like that sulfur, would also provide the 'A' in  $A dv/dt/v^2 = F$ . The lattice interaction provides the  $dv/dt$ .

Recall the pairing interaction  $F = A(dv/dt)/v^2$ . (1)

For a superconductor the same effective masses, including the effects of the bonding with the upper and lower layers, contribute to effective masses moving in the antisymmetric mode so that makes the relative velocity of the two masses  $v=0$  which means that quantum fluctuations are small.

The mainstream is very close to this phenomenology in it's pnictide analysis.

They just use different words for the same thing. For example they call these quantum fluctuations 'nematic'.

They also define nematic QCP: the Quantum Criticality Point

At  $v=0$  critical nematic fluctuations are quenched at high  $T_c$ . The mainstream goes further and states that this QCP is where the (orbital) Order, Fermi liquid and nematic states all meet. So at QCP that  $v=0$  and so we have the critical temperature superconductivity molecular concentrations. Also high pressure quenches these fluctuations thereby making  $v$  small.

So the mainstream seems surprisingly close to understanding the (pairing interaction) effects of equation 1. But yet without equation 1 they will never understand the source of the pairing interaction, they will be forever guessing.

#### 4.6 Summary of Consequences of the Uncertainty In Distance (separation) C In $-\delta z = \delta z \delta z + C$ eq.3

1) C as width of a slit determines uncertainty in photon location and resulting wave particle duality (see above section 4.3.8).

2) C is uncertainty in separation of particles which is large at high temperatures. Note degeneracy repulsion (two spin  $\frac{1}{2}$  can't be in a single state) is not necessarily time dependent and is zero only for bosons. Also given the already extremely small Brillouin zone bosonization separation (see equation 4.3 for pairing interaction source) then C is small so not much more is needed for C to drop below  $\frac{1}{4}$  to the r axis for Bosons. Thus time axis  $\Delta t=0$  so  $\Delta v = a \Delta t = 0$ . (note relative  $v$  is big here. Therefore there is no  $\Delta v$  and so no force ( $F=ma$ ) associated with the time dependent acceleration 'a' for this Boson flowing through a wire with the stationary atoms in the wire. So there is no electrical resistance to the flow of the Bosons in this circuit and we have therefore derived superconductivity from first principles. But there is a force between electrons in a pairing interaction (that creates the Boson) because  $v$  between them is so small. Use pairing interaction force  $mv^2/r$  between leptons from sect.4.8:  $F_{\text{pair}} = A(dv/dt)/v^2$  is large. Recall that a superfluid has no viscosity. But doesn't viscosity constitute a force F as well ( $F/m=a$  in  $dv=adt$ ) and isn't helium 4 already a boson so that when C drops below  $\frac{1}{4}$  then  $dt$  drops to zero as well? So superfluidity for helium 4 is also a natural outcome of a small C.

At low temperatures you start seeing some of the same phenomena you see in high energy physics (at high temperatures) such as this fractional charge. There is a reciprocity between high energy and low energy physics. That pairing interaction force  $A(dv/dt)/v^2$  that gets larger as  $v$  (temperature) in the denominator gets smaller. These forces get into the new pde and play a similar role to the high energy forces.

3) C is separation between particle-antiparticle pair (pair creation). For  $C < 1/4$  we leave the  $135^\circ$  and  $45^\circ$  diagonals jump to the r axis and simple  $ds^2$  wave equation dependence (Ch1, section 2). Thus we have derived pair creation and annihilation. The  $dt$  is zero giving no time dependence

thus stable states. On the superconductivity we derived the pairing interaction (eq.4.5.3) and superfluidity (sect.4.6). So for two paired leptons (via the pairing interaction) the Hamiltonian of each one is then a function of both wavefunctions:  $\hbar \partial \psi_1 / \partial t = u_1 \psi_1 + v_2 \psi_2$  and  $\hbar \partial \psi_2 / \partial t = u_2 \psi_1 + v_1 \psi_2$  which gives the superconductivity. See Feynman lectures on superconductivity.

#### **Alternative Method Of Doing QM: Markov Chains (eg., Implying Path Integral)**

#### **4.7 Markov Chain Zitterbewegung For $r > \text{Compton Wavelength}$ Is A Blob**

Recall that the mainstream says that working in the Schrodinger representation and starting with the average current (from Dirac eq.  $(\hat{p} - mc)\psi(x) = 0$ ) assumption and so equation 9 gives  $J^{(+)} = \int \psi^{(+)\dagger} c \alpha \psi^{(+)} d^3x$ . Then using Gordon decomposition of the currents and the Fourier superposition of the  $b(p,s)u(p,s)e^{-ipx/\hbar}$  solutions ( $b(p,s)$  is a normalization constant of  $\int \psi^\dagger \psi d^3x$ ) to the free particle Dirac equation (1.2.7) we get for the observed current (u and v have tildas):

$$J^k = \int d^3p \left\{ \sum_{\pm s} [ |b(p,s)|^2 + |d(p,s)|^2 ] p^k c^2 / E + i \sum_{\pm s, \pm s'} b^*(-p, s') d^*(p, s) e^{2ix_0 p_0 / \hbar} u(-p, s') \sigma^{k0} v(p, s) \right. \\ \left. + i \sum_{\pm s, \pm s'} b(p, s') d(p, s) e^{2ix_0 p_0 / \hbar} v(p, s') \sigma^{k0} u(p, s) \right\} \quad (4.11.4)$$

(2) E. Schrodinger, Sitzber. Preuss. Akad. Wiss. Physik-Math., 24, 418 (1930)

Thus we can either set the positive energy  $v(p,s)$  or the negative energy  $u(p,s)$  equal to zero and so we no longer have a  $e^{2ix_0 p_0 / \hbar}$  zitterbewegung contribution to  $J_u$ , the zitterbewegung no longer can be seen. Thus we have derived the mainstream idea that the zitterbewegung does not exist. But if we continue on with this derivation we can also show that the zitterbewegung does exist if the electron is in a confined space of about a Compton wavelength in width, so that a nearby confining wall exists then.

(3) Bjorken and Drell, *Relativistic Quantum Mechanics*, PP.39, eq.3.32, (1964)

Note negative energy does exist from  $E^2 = p^2 c^2 + m_0^2 c^4$  so  $E = \sqrt{p^2 c^2 + m_0^2 c^4}$  so that E can be negative (positrons). Note if p small m can be negative since  $E = pc$  then. In  $E = mgh + \frac{1}{2}mv^2$  a negative energy E does indeed create absurd results but not if E is also negative since the negative sign cancels out.

#### **Derivation Of Eq.1.2.7 From (uncertainty) Blob (reference 1)**

Recall from section 3.4.4 that we can derive the zitterbewegung blob (within the Compton Wavelength) from the equation 1.24. (see reference 2.) Also recall from section 1 that we postulated a blob that was nonzero, non infinite and with constant standard deviation (i.e., we found  $3 \delta \delta z = 0$ ). But that is the same thing as Schrodinger's zitterbewegung blob mentioned above. So we postulated the electron and derived the electron rotated 7 (i.e., eq.16) from that postulate. We therefore have created a mere trivial tautology.

#### **4.8 2D ⊕ 2D**

Also with eq.7 first 2D solution there is no new pde and so no wave function. The other solution to 1.11 adds the other 2D (observer) and so we get the eq.16 new pde and thereby its wave function. So we needed the observer to "collapse" the wave function. This is the proof of the core part of the Copenhagen interpretation. Eq.7 gives the probability density  $\delta z^* \delta z$  (another component of the Copenhagen interpretation so we have a complete proof of the Copenhagen interpretation of quantum mechanics here.

#### **4.9 Mixed State eq.7+eq.7 Implies There Is No Need For A Dirac Sea**

The 1928 solution to the Dirac equation has for the positron and electron simultaneous x,y,z coordinates (bottom of p.94 Bjorken and Drell derivation of the free particle propagator) creating the need for the Dirac sea of filled states so the electron will not annihilate immediately with a collocated negative energy positron which is also a solution to the same Dirac equation. Recall

$\psi(+)$  and  $\psi(-)$  are separate but (Hermitian) orthogonal eigenstates and so  $\langle\psi(+)|\psi(-)\rangle=0$  without a perturbation so we can introduce a displacement  $\psi(x)\rightarrow\psi(x+\Delta x)$  for just one of these eigenfunctions. But the mixed state positron and electron separated by a substantial distance  $\Delta x$  will not necessarily annihilate. Note in the eq.7  $2D\oplus 2D$  (i.e.,  $\sqrt{\kappa_{\mu\nu}}\gamma^{\mu}\partial\psi/\partial x_{\mu}=(\omega/c)\psi$ ) equation the electron is at  $45^{\circ}$   $-dr,dt$  and the positron is at  $135^{\circ}$   $dr',-dt'$  which means formally they are not in the same location in this formulation of the Dirac equation. In that regard note that  $dr/\sqrt{(1-r_H/r)}=dr'$ ,  $r_H=2e^2/m_e c^2=\epsilon$  so that different  $e$  leads in general to different  $dr'$  spatial dependence for the  $\psi(x)$  in the general representation of the  $4\times 4$  Dirac matrices. So in the multiplication of 4  $\psi$ s the antiparticle  $\psi$  will be given a  $r_H$  displacement  $\Delta r$  ( $dr\rightarrow dr'$  here) by the  $\pm\epsilon$  term in the associated  $\kappa_{\mu\nu}$ . So the  $\psi(+)$  and  $\psi(-)$  in the Dirac equation column matrix will have different  $(x,y,z,t)$  values for the  $\psi(+)$  than for the  $\psi(-)$ . As an analogy an electron in a given atomic state of a given atom can't decay into a empty state of a completely different atom located somewhere else. Thus perturbation theory (eg., Fermi's golden rule) cannot lead to the electron spontaneously dropping into a negative energy state since such eq.7 states are not collocated for a given solutions to a single Dirac equation (other positrons from *other* Dirac equation solutions can always wonder in from the outside in the usual positron-electron pair annihilation calculation case but that is not the same thing). Thus the Dirac sea does not have to exist to explain why the electron does not decay into negative energy.

#### 4.10 No Need for a Running Coupling Constant

If the Coulomb  $V=\alpha/r$  is used for the coupling instead of  $\alpha/(k_H-r)$  then we must multiply  $\alpha$  in the Coulomb term by a floating constant ( $K$ ) to make the coulomb  $V$  give the correct potential energy. Thus if an isolated electron source is used in  $Z_{00}$  we have that  $(-K\alpha/r)=\alpha/(k_H-r)$  to define the running coupling constant multiplier "K". The distance  $k_H$  corresponds to about  $d=10^{-18}m=ke^2/m_e c^2$ , with an interaction energy of approximately  $hc/d=2.48\times 10^{-8}$ joules= 1.55TeV. For 80 GeV,  $r\approx 20$  ( $\approx 1.55\text{TeV}/80\text{GeV}$ ) times this distance in colliding electron beam experiments, so  $(-K\alpha/r)=\alpha/(r_H-r)=\alpha/(r(1/20)-r)=-\alpha/(r(19/20))=(20/19)\alpha/r=1.05\alpha/r$  so  $K=1.05$  which corresponds to a  $1/K\alpha\approx 1/\alpha'\approx 130$  also found by QED (renormalization group) calculations of (Halzen, Quarks). Therefore we can dispense with the running coupling constants, higher order diagrams, the renormalization group, adding infinities to get finite quantities; all we need is the correct potential incorporating  $\sqrt{\kappa_{00}}$ .

Note that the  $\alpha'=\alpha/(1-[\alpha/3\pi(\ln\chi)])$  running coupling constant formula (Faddeev, 1981)] doesn't work near the singularity (i.e.,  $\chi\approx e^{3\pi/\alpha}$ ) because the constant is assumed small over all scales (therefore there really is *no formula to compare*  $\alpha/(r-r_H)$  to over all scales) but this formula works well near  $\alpha\sim 1/137.036$  which is where we used it just above.

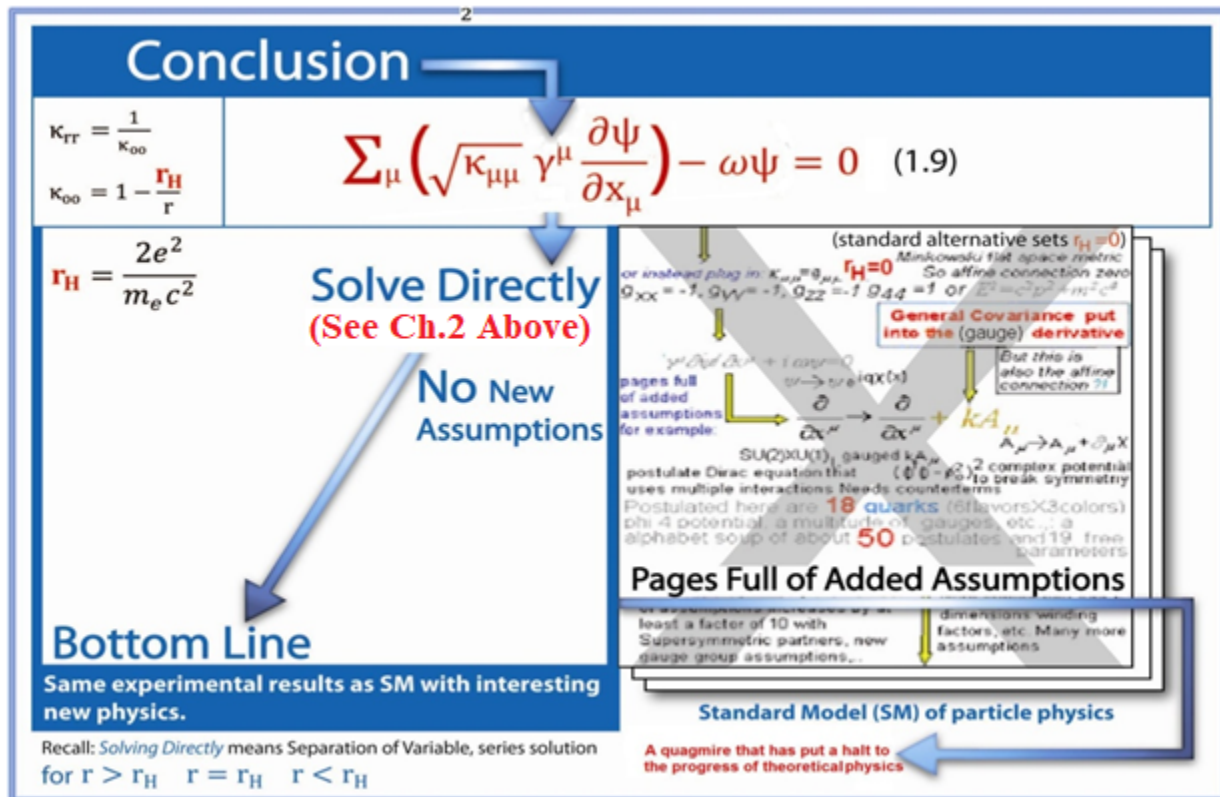
#### 4.11 Rotated 1.24 Implies $\kappa_{00}=1-r_H/r\approx 1/\kappa_{rr}$ So No Klein Paradox As Is In The Original 1928 Dirac Equation

Recall that  $\kappa_{rr}=1/(1-r_H/r)$  in the new pde eq.7. Recall that for the ordinary Dirac equation that the reflection ( $R_s$ ) and transmission ( $T_s$ ) coefficients at an abrupt potential rise are:  $R_s=((1-\kappa)/(1+\kappa))^2$  and  $T_s=4\kappa/(1+\kappa)^2$  where  $\kappa=p(E+mc^2)/k_2(E+mc^2-V)$  assuming  $k_2$  (ie., momentum on right side of barrier) momentum is finite.. Note in section1  $dr'^2=\kappa_{rr}dr^2$  and  $p_r=mdr/ds$  in the eq.7+eq.7 mixed state new pde so  $p_r=(\sqrt{\kappa_{rr}})p=(1/\sqrt{(1-r_H/r)})p$  and so  $p_r\rightarrow\infty$  so  $\kappa\rightarrow\infty$  the huge values of the rest of the numerator and denominator cancel out with some left

over finite number. Therefore for the actual abrupt potential rise at  $r=r_H$  we find that  $p_r$  goes to infinity so  $R_s=1$  and  $T_s=0$  as expected. Thus nothing makes it through the huge barrier at  $r_H$  thereby resolving the Klein paradox: there is no paradox anymore with the new pde. No potentials that have infinite slope. Therefore the new pde applies to the region inside the Compton wavelength just as much as anywhere else. So if you drop the  $\sqrt{\kappa_{rr}}$  in the new pde all kinds of problems occur inside the Compton wavelength such as more particles moving to the right of the barrier than as were coming in from the left, hence the Klein paradox(4).

(4) O.Klein, Z. Physik, 53,157 (1929)

So by adopting the new pde (eq.9 ) instead of the old 1928 Dirac equation you make the Dirac equation generally covariant and selfconsistent at all scales and so find no more paradoxes.



#### 4.12 Mixed State eq.7+eq.7 $C>1/4$ and $C<1/4$ Implications For Pair Creation And Annihilation

Note

that if  $C<1/4$  in equation 1 ( $dz=(-B\pm\sqrt{(B^2-4AC)})/2A$ ,  $A=1$ ,  $B=1$ ) the two points are close together and time disappears since  $dz$  is then real for the neighborhood of the origin where opposite charges can exist along the  $135^\circ$  line. So we are off the  $45^\circ$  diagonal and therefore the equation 2 extrema does *not* apply. So the eq.7 2 fermions disappear and we have only that original second boson derivative  $\delta ds^2=0$  circle ( $\square^2 A_\mu=0$ ,  $\square \bullet A=0$ ) Maxwell equations. So when two fundamental fermions are too near the origin and so get too close together (ie.,  $dr=dr'$ ,  $dt=dt'$ ) you only have a boson and the fermions disappear. So we have explained particle-antiparticle annihilation from first principles. In contrast two fermions of equal charge require energies on the order of 100GeV to get this close together in which case they also generate bosons in the same way and



again the fermions do disappear from existence. You then generate the W and the Z bosons (since above sect.4.11 nonweak field  $k^\nu k_\nu \kappa_{\mu\mu}$ =Proca equation term) .

## Chapter 5 Second Solution $C_M$ Contribution To $\kappa_{\mu\nu}$ Due To Object B

Note we are within the Compton wavelength of the next higher fractal scale new pde (we are inside of  $r_H$ ). Also our new pde does not exhibit the Klein paradox within the Compton wavelength (because of the  $\kappa_{ij}$  s) or anywhere else so our new pde is valid there also. Note for  $r < r_H$  then  $E = \hbar\omega = E = 1/\sqrt{\kappa_{00}} = 1/\sqrt{(1-r_H/r)}$  and therefore this square root is imaginary and so  $i\omega \rightarrow \omega$  in the Heisenberg equations of motion. Therefore  $r = r_0 e^{i\omega t}$  becomes instead  $r = r_0 e^{\omega t}$  (that accelerating cosmological expansion) which is observable zitterbewegung motion since  $\omega t$  does not cancel out in  $\psi^* \psi$  in that case and again we are within the Compton wavelength and so even according to the Bjorken&Drell PP.39 criteria the zitterbewegung therefore exists.

Also note in the above  $\kappa_{rr} = 1/\kappa_{tt}$  we have derived GR from our theory in eq. 13-14a. For loosely bound states (eg.,  $2P_{1/2}$  at  $r \approx r_H$ ) object C contributes a  $\xi_{WZ}$ . (see B4)

### 5.1 The $R_{\mu\nu}$ Is Also A Quantum Mechanical Operator.

Recall section 4 implies General relativity (recall eq.13,14 and the Schwarzschild metric derivation there). Note this all exists in the context of appendix B MandelbulbLepton results. So it is a local metric normalization to get the ambient eq.4 flat background metric. and so equation 1 and observables. Note also in section 1.2 above we defined the quantum mechanical  $[A, H]|a, t\rangle = (\partial A / \partial t)|a, t\rangle$  Heisenberg equations of motion in section 1.2 with  $|a, t\rangle$  a eq.2 (7) eigenstate. Note the commutation relation and so second derivatives (H relativistic eq.2 (7) Dirac eq. iteration 2nd derivative) taken twice and subtracted.  $(\partial A / \partial t)|a, t\rangle$ . For example if 'A' is momentum  $p_x = -i\hbar \partial / \partial x$ .  $H = \partial / \partial t$  then  $[A, H]$  so we must use the equations of motion for a curved space. In this ordinary QM case I found for  $r < r_H$  that  $r = r_0 e^{\omega t}$   $H|a, t\rangle = (\partial A / \partial t)|a, t\rangle = (\partial / \partial t)(\partial / \partial x) - (\partial / \partial x)(\partial / \partial t) = p \cdot \dot{t}$ . But  $\sqrt{\kappa_{rr}}$  is in the kinetic term in the new pde with merely perturbative  $t' = t / \kappa_{00}$ . But using the  $C^2$  of properties of operator A ( $C^2$  means continuous first and second derivatives and is implied in sect.1.1) in a curved space time we can generalize the Heisenberg equations of motion to curved space *nonperturbatively* with:  $(A_{i,jk} - A_{i,kj})|a, t\rangle = (R^m_{ijk} A_m)|a, t\rangle$  where  $R^a_{bcd}$  is the Riemann Christoffel Tensor of the Second Kind and  $\kappa_{ab} \rightarrow g_{ab}$ . Note all we have done here is to identify  $A_k$  as a quantum vector operator here, which it should be. Note again the second derivatives are taken twice and subtracted looking a lot like a generalization of the above Heisenberg equations of motion commutation relations. Note also  $R^m_{ijk}$  could even be taken as an eigenvalue of  $p \cdot \dot{t}$  since it is zero when the space is flat, where force is zero. These generalized Heisenberg equations of motion reduce to the above QM form in the limit  $\omega \rightarrow 0$ , outside the region where angular velocity is very high in the expansion (now it is only one part in  $10^5$ ).

### 5.2 Solution To The Problem Of General Relativity Having 10 Unknowns But 6 Independent Equations

From Chapter 4 this zitterbewegung (de Donder **harmonic** motion (2) ) plays a much more important role in general relativity (GR) The reason is that General Relativity has ten equations (e.g.,  $R_{\mu\nu} = 0$ ) and 10 unknowns  $g_{\mu\nu}$ . But the Bianchi identities (i.e.,  $R_{\alpha\beta\mu\nu;\lambda} + R_{\alpha\beta\lambda\mu;\nu} + R_{\alpha\beta\nu\lambda;\mu} = 0$ ) drop the number of independent equations to 6. Therefore the four

equations (ie.,  $(\kappa^{\mu\nu}\sqrt{-\kappa})_{,\mu}=0$ ) of the (zitterbewegung) harmonic condition fill in the four degrees of freedom needed to make GR 10 equations  $R_{\mu\nu}=0$  and 10 unknown  $g_{\mu\nu}$ . We thereby do not allow the gauge formulations that give us wormholes or other such arbitrary, nonexistent phenomena. In that regard this de Donder **harmonic** gauge (equivalent condition) is what is used to give us the historically successful theoretical predictions of General Relativity such as the apsidal motion of Mercury and light bending angle around the sun seen in solar eclipses. So the harmonic 'gauge' is not an arbitrary choice of "gauge". It is not a gauge at all actually since it is a physically real set of coordinates: the zitterbewegung oscillation harmonic coordinates.

(3) John Stewart (1991), "Advanced General Relativity", Cambridge University Press, ISBN 0-521-44946-4

### 5.3 $r < r_H$ Observational Evidence For Object B

Recall there are two metrics in section 3.1 and outside Schwarzschild and inside De Sitter. But because of eq.7 (and so eq.16 modified Dirac equation) we are in a rapidly rotating object, the electron rotating at rate  $c$  (in the fractal theory at least. It is the solution to the Dirac equation eq.16). But because of inertial frame dragging in object A observed spin is extremely small except for a small contribution to reducing inertial frame dragging of object B (section 4.1.2). So the geodesics are parallel (flat space holonomy) just like the cylinder. Inertial frame dragging should not destroy the holonomy, just rotate the cylinder but it stays a cylinder. We can realize that for a spherical metric by maintaining the parallel transport which means the expansion is needed to maintain the cylinder. From our perspective we see a sphere with a flat space. Recall the mainstream guy also said this space is in fact that of a 3D cylinder, which it is. This 'seeing ourselves' is also predicted by the mainstream stuff too given the observations of the flat space and the requirement of the cylinder topology. But seeing ourselves is so weird to the mainstream that they have postulated a pretzel space instead at large distances. So the universe is fractal with the (Dirac spinor) the Kerr metric high angular momentum local cylinder near  $r_H$  dominates and creates the flat space time associated with a cylinder so that two parallel lines do remain parallel within the time like interval at least. When we look out at the edge of the universe in some specific direction, beyond that space like interval (that we cannot see beyond) we are very nearly (just over the space- like edge) looking at ourselves as we were over 12by years ago. We are looking back in time at ourselves! (in this fractal model). The hydra-centaurus supercluster of galaxies is about 150MLY away. We would find it by looking in the opposite direction of the sky from where we see it now, it would be a smudge at submillimeter wave lengths.

So create a map of the giant galaxy clusters within 2By of the Milky Way galaxy and invert each object by  $180^\circ$  to find the map of the oldest redshift galaxy clusters

Given 2D piece of paper, you can connect the ends a few different ways by folding it. Connect one of the dimensions normally and you have a cylinder. Flip one edge over >before connecting and you've made a Mobius strip. Connect two dimensions, the top to the bottom and one side to the other, and you have a torus (aka a donut). In our 3D universe, there are lots of options — 18 known ones, to be precise. Mobius strips, Klein bottles and Hantzsche-Wendt space manifolds are all non-trivial topologies that share something in common: if you travel far enough in one direction, you come back to where you started. Bg gravimagnetic dipole from the new pde provides the spherical torus shape for this.

In this fractal universe we do this. In fact there is only one way to do it: in the  $r_H$  cylinder region of the Kerr metric near c rotation rate, so the topology is a given.

#### 5.4. N=0 (eq.13,14,15 give our Newpde metric $\kappa_{\mu\nu}$ at $r < r_H$ , $r > r_H$ )

Found GR from eq.13 and eq.14 so we can now write the Ricci tensor  $R_{\mu\nu}$  (and self similar perturbation Kerr metric since frame dragging decreased by external object B, sect.A6). Also for fractal scale  $N=0$ ,  $r_H=2e^2/m_e c^2$ , for  $N=-1$   $r'_H=2Gm_e/c^2=10^{-40}r_H$ .

#### Nonzero Generic maximally symmetric (MS) ambient metric

So start with complete frame dragging suppression eq.13, 15 but with ambient metric (provided by later **perturbation**  $a < r$  **provided by some rotation**) metric ansatz:  $ds^2 = -e^\lambda (dr)^2 - r^2 d\theta^2 - r^2 \sin\theta d\phi^2 + e^\mu dt^2$  so that  $g_{00}=e^\mu$ ,  $g_{rr}=e^\lambda$ . From eq.  $R_{ij}=0$  for spherical symmetry in free space

$$R_{11} = \frac{1}{2}\mu'' - \frac{1}{4}\lambda' \mu' + \frac{1}{4}(\mu')^2 - \lambda'/r = 0 \quad 5.1.1$$

$$R_{22} = e^{-\lambda} [1 + \frac{1}{2} r(\mu' - \lambda')] - 1 = 0 \quad (5.1.2)$$

$$R_{33} = \sin^2\theta \{ e^{-\lambda} [1 + \frac{1}{2} r(\mu' - \lambda')] - 1 \} = 0 \quad (5.1.3)$$

$$R_{00} = e^{\mu-\lambda} [-\frac{1}{2}\mu'' + \frac{1}{4}\lambda' \mu' - \frac{1}{4}(\mu')^2 - \mu'/r] = 0 \quad (5.1.4)$$

$$R_{ij} = 0 \text{ if } i \neq j$$

(eq. 5.1.1-5.1.4 from pp.303 Sokolnikof): Equation D2 is a mere repetition of equation 5.1.3. We thus have only three equations on  $\lambda$  and  $\mu$  to consider. From equations 5.1.1, 5.1.4 we deduce that

$\lambda' = -\mu'$  so that radial  $\lambda = -\mu + \text{constant} = -\mu + C$  where  $C = 1 + \varepsilon$  for our generic nonzero free space metric caused by object B (sect.A7)  $C = \xi_1$  because it normalizes into the denominator of  $r_H = C_M/\xi_1$  through eq.9a, and D9 in sect.D2. So  $e^{-\mu+C} = e^\lambda$ . Then 5.1.2 can be written as:

$$e^{-C} e^\mu (1 + r\mu') = 1 \quad 5.1.5$$

Set  $e^\mu = \gamma$ . So  $e^{-\lambda} = \gamma e^{-C}$  and so integrating this first order equation (equation.5.1.11) we get ⊗

$$\gamma = -2m/r + e^C \equiv e^\mu = g_{00} \text{ and } e^{-\lambda} = (-2m/r + e^C) e^{-C} = 1/g_{rr} \quad (5.1.6)$$

From equation D6 we can identify radial  $C = 1 + 2\varepsilon$  with also rotational oblateness perturbation  $\Delta\varepsilon$  already a component here (D8 below).  $\kappa_{00} = 1 - (C + C^2/2 + \dots) - 2m/r$ ;  $e^{-\lambda} = 1/\kappa_{rr} = 1/(1 - 2m'/r)$  (5.1.7)

#### Perturbative self similar rotation providing the ambient metric

Our new pde has spin S and so the self similar ambient metric on the  $N=0$  th fractal scale is the Kerr metric which contains those **perturbation rotations** ( $d\theta/dt$  T violation so (given CPT) then

$$\text{CP violation) } ds^2 = \rho^2 \left( \frac{dr^2}{\Delta} + d\theta^2 \right) + (r^2 + a^2) \sin^2 \theta d\phi^2 - c^2 dt^2 + \frac{2mr}{\rho^2} (a \sin^2 \theta d\theta - c dt)^2,$$

5.1.9.(5.1.8)

where  $\rho^2(r, \theta) \equiv r^2 + a^2 \cos^2 \theta$ ;  $\Delta(r) \equiv r^2 - 2mr + a^2$ , In our 2D  $d\phi=0$ ,  $d\theta=0$  Define:

$$\left( \frac{r^2 + a^2 \cos^2 \theta}{r^2 - 2mr + a^2} \right) dr^2 + \left( 1 - \frac{2m}{r^2 + a^2 \cos^2 \theta} \right) dt^2 \quad \theta \neq 0$$

$\rho^2(r, \theta) \equiv r^2 + a^2 \cos^2 \theta$ ;  $\Delta(r) \equiv r^2 - 2mr + a^2$ ,  $r^{\wedge 2} \equiv r^2 + a^2 \cos^2 \theta$ ,  $r'^2 \equiv r^2 + a^2$ . Inside  $r_H$   $a < r$ ,  $r > 2m$

$$\left( \frac{(r^{\wedge})^2}{(r')^2 - 2mr} \right) dr^2 + \left( 1 - \frac{2mr}{(r^{\wedge})^2} \right) dt^2 + \dots = \left( \frac{1}{\frac{(r')^2}{(r^{\wedge})^2} - \frac{2mr}{(r^{\wedge})^2}} \right) dr^2 + \left( 1 - \frac{2mr}{(r^{\wedge})^2} \right) dt^2. \text{ The } (r^{\wedge}/r')^2 \text{ term is}$$

$$\frac{(r^{\wedge})^2}{(r')^2} = \frac{r^2 + a^2}{r^2 + a^2 \cos^2 \theta} = \frac{1 + \frac{a^2}{r^2}}{1 + \frac{a^2}{r^2} \cos^2 \theta} \approx 1/g_{rr} (\approx g_{00}) \quad (3e \text{ frame of reference } z=1: \xi_1 = 1 + \varepsilon + \Delta\varepsilon \text{ for } \Delta\varepsilon)$$

$$\left(1 + \frac{a^2}{r^2}\right)\left(1 - \frac{a^2}{r^2}\cos^2\theta\right) + \dots = 1 - \frac{a^4}{r^4}\cos^2\theta - \frac{a^2}{r^2}\cos^2\theta + \frac{a^2}{r^2} + \dots = 1 + \frac{a^2}{r^2}(1 - \cos^2\theta) + \dots$$

(Replace  $a^2/r^2$  Kerr object B term with inertial frame dragging mass  $\xi_1$ . Subtract  $2mr/(r')^2 = r_H/r_H$ )

$$= 1 + \frac{a^2}{r^2}\sin^2\theta + \dots \equiv 1 + \frac{\frac{a^2}{r^2}u^2}{2} = 1 + \xi_1 - \frac{r_H}{r_H} = 1 + \varepsilon + \Delta\varepsilon + \dots \quad (5.1.9)$$

Kerr metric inertial frame dragging Newpde zitterbewegung oscillation suppression outside object B is  $((a/r)\sin\theta)^2 = 1/g_{rr} = e^{i\Delta\varepsilon}$  from D7 in the proper frame. Inside object A  $((a/r)\sin\theta)^2 = 1 - \Delta\varepsilon$ . Composite 3e frame of reference  $\Delta\varepsilon \rightarrow 1 + \varepsilon + \Delta\varepsilon$  (section 2).  $\varepsilon$  changes with time. Object B oscillation observed compression in Shapely, rarefaction in Eridanis.

### 11.1 Is metric quantization possible? So does it have a Hamiltonian?

Recall eq.D9 object B generation in the Kerr metric  $((a/r)\sin\theta)^2 = \Delta\varepsilon$  with outside object B  $r_H$   $\kappa_{00} = \varepsilon^{i\Delta\varepsilon}$  with inside  $\kappa_{00} = 1 - \Delta\varepsilon$ . Finally in the composite 3e frame of reference  $\Delta\varepsilon \rightarrow \Delta\varepsilon + \varepsilon$  for both in Eg.,  $\kappa_{00} = e^{i(\varepsilon + \Delta\varepsilon)}$  outside object B.

Also recall the fractal separation of variables in the universe wave function  $\Psi$  solution to the Newpde:

$$\Psi = \prod \psi_N = \dots \psi_{-1} \bullet \psi_0 \bullet \psi_1 \bullet \dots$$

N is the fractal scale. Not also that New pde  $\Delta\varepsilon \equiv H_{\Delta\varepsilon}$  or  $\varepsilon \equiv H_\varepsilon$   $r > r_H$  have nothing to do with each other (like  $H_{SHM} & H_J$ ) so  $\Delta\varepsilon \varepsilon \psi_N = E \psi_N$  is undefined (just as  $H_{SHM} * H_J$  is undefined). In contrast for  $r_{(\varepsilon, \Delta\varepsilon)} e^{kt} = \psi_{N+1}$  from new pde cosmological  $r_H > r$  there is a common time  $t = t'$  in

$$-i \frac{\partial \left( -i \frac{\partial \psi_{N+1}}{\partial t'} \right)}{\partial t} = \varepsilon \Delta\varepsilon \psi_{N+1}$$

on the zitterbewegung cloud radius expansion (see 7.4.2)  $r_{\Delta\varepsilon \varepsilon} e^{kt} = \psi_{N+1}$  so that  $\varepsilon \Delta\varepsilon \psi_{N+1}$  is defined. So  $\langle i | \varepsilon \Delta\varepsilon | i \rangle$  (from  $\varepsilon \Delta\varepsilon \psi_{N+1}$ ) is observable and  $\langle i | \varepsilon \Delta\varepsilon | i \rangle$  (from  $\varepsilon \Delta\varepsilon \psi_N$ ) is not observable.

But normally, given space-like  $r_H$  barrier separations, the operators (sect.2.5) are on quantities only within a given fractal scale. Here  $\Delta\varepsilon$  is N+1 th and  $r_H$  Nth so as an operator equation:  $\Delta\varepsilon r_H = 0$  in:

$$E = \frac{1}{\sqrt{1 - \frac{\Delta\varepsilon}{1 - \varepsilon} \frac{r_H}{r}}} = 1 - \frac{\Delta\varepsilon}{2(1 - \varepsilon)} - \frac{r_H}{2r} + \frac{3}{8} \left( \frac{r_H}{r} \right)^2 + 2 \frac{\Delta\varepsilon}{1 - \varepsilon} \left( \frac{r_H}{r} \right) + \dots = 1 - \frac{\Delta\varepsilon}{2(1 - \varepsilon)} - \frac{r_H}{2r} + \frac{3}{8} \left( \frac{r_H}{r} \right)^2 + 0 + \dots$$

## 6.1 Examples of this ambient metric

### N=0 Composite 3e

For  $z=0$  just inside  $r_H$ , the two positrons each have constant  $\psi$  (N=0 ch.8) inside  $r_H$ . So from

$$\text{eq.D9 divide } \kappa_{rr} \text{ by } 1 + \varepsilon + \varepsilon = 1 + 2\varepsilon. \text{ So } \frac{1}{\kappa_{rr}} = \left( 1 + \frac{e^2}{\xi_0 r} \right) (1 + 2\varepsilon) \equiv 1 + 2 \left( \varepsilon + \Delta\varepsilon - \frac{e^2}{\xi_0 r} \right)$$

Also divide again by  $1 + \varepsilon$  for the magnetic field (see appendix C flux of B) maximal symmetry

$$\frac{1}{\left( \frac{1 + 2\varepsilon + \Delta\varepsilon}{1 - \varepsilon} - 2m/\xi_0 r \right)} dr^2 + (1 - 2m/r\xi_0) dt^2 = \frac{1}{\left( 1 + \frac{\varepsilon}{1 - \varepsilon} - 2m/\xi_0 r \right)} dr^2 + \left( 1 - \frac{2m}{r\xi_0} \right) dt^2$$

$$= \frac{1}{(1 + \varepsilon' - 2m/\xi_0 r)} dr^2 + \left( 1 - \frac{2m}{r\xi_0} \right) dt^2, \quad \varepsilon' \equiv \varepsilon/(1 + \varepsilon). \quad (6.1.1)$$

For  $z=0$  just outside  $r_H$ , Since randomly the B field disappears ( $dB/dt \neq 0$ ) due to that creation-annihilation we have a Faraday's law Meisner effect. With outside  $r_H$  B results, just divide by  $1 + \varepsilon''$  (D9) for zero point energy  $\varepsilon'' = .08 \pi^\pm$  of eq.9.22 (partII) which has to itself increase and

decrease with (see 5.1.9) each of these annihilation events and  $\pi^\pm$  exists just outside  $r_H$  (from our Frobenius solution):  $\frac{1}{(1+\varepsilon''-2m/\xi_0 r)} dr^2 + ((1-2m/\xi_0 r)) dt^2 = ds^2$  (6.1.2)

For  $z=0 \rightarrow z=1$   $r >> r_H$  then  $\xi_0 \rightarrow \tau$ . Define  $\varepsilon' = \frac{\varepsilon}{1+\varepsilon}$  Must normalize again so multiply by  $\frac{1}{1+\varepsilon'}$  (see 5.1.9 for  $z=1$  outside

$$\frac{1}{(1+\frac{\Delta\varepsilon}{1+\varepsilon}-2m/\xi_1 r)} dr^2 + (1-2m/r\xi_1) dt^2 = \frac{1}{(1+\frac{\Delta\varepsilon}{1+\varepsilon}-2m/\xi_1 r)} dr^2 + \left(1 - \frac{2m}{r\xi_1}\right) dt^2 \quad (6.1.3)$$

### N=1 Use Ricci curvature to obtain Newpde comoving internal observer Cosmology

The Laplacian of the metric tensor (in Newpde zitterbewegung harmonic local coordinates whose components satisfy Ricci tensor =  $R_{ij} = -(1/2)\Delta(g_{ij})$  where  $\Delta$  is the Laplace-Beltrami second derivative operator) is not zero and the right side is the metric source. Geometrically, the Ricci curvature is the mathematical object that controls the (comoving *observer*) *growth rate of the volume* of metric balls in a manifold in this case given by the New pde source

zitterbewegung. Set the phase so real  $\Delta g_{ij}$  is small at time=0 (big bang from  $r_{bb}$ ) then initial  $\sin\theta_0 = \sin 90^\circ$ . Given the  $\varepsilon + \Delta\varepsilon$  on the right side of eq.5.1.2 and eq.5.1.9:

$$R_{22} = \frac{1}{2}\Delta g_{22} = e^{i(\varepsilon + \Delta\varepsilon)} e^{i\pi/2} = \sin(\varepsilon + \Delta\varepsilon) + i\cos(\varepsilon + \Delta\varepsilon). \quad (6.1.4)$$

This is Ricci tensor exterior source to the interior ( $r < r_H$ ) comoving metric.

### N=0 Application example: (mentioned on first page)

#### Separation Of Variables On New Pde

After separation of variables the “r” component of equation 16 (Newpde) can be written as:

$$\left[ \left( \frac{dt}{ds} \sqrt{\kappa_{00}} m_p \right) + m_p \right] F - \hbar c \left( \sqrt{\kappa_{rr}} \frac{d}{dr} + \frac{j+3/2}{r} \right) f = 0 \quad (6.1.5)$$

$$\left[ \left( \frac{dt}{ds} \sqrt{\kappa_{00}} m_p \right) - m_p \right] f + \hbar c \left( \sqrt{\kappa_{rr}} \frac{d}{dr} - \frac{j-1/2}{r} \right) F = 0. \quad (6.1.6)$$

Using the above Dirac equation component we find the anomalous gyromagnetic ratio  $\Delta g_y$  for the spin polarized  $F=0$  case. Recall the usual calculation of rate of the change of spin  $S$  gives  $dS/dt \propto m \propto g_y J$  from the Heisenberg equations of motion. We note that  $1/\sqrt{\kappa_{rr}}$  rescales  $dr$  in

$\left( \sqrt{\kappa_{rr}} \frac{d}{dr} + \frac{j+3/2}{r} \right) f$  in equation . Thus to have the same rescaling of  $r$  in the second term we

must multiply the second term denominator (i.e.,  $r$ ) and numerator (i.e.,  $J+3/2$ ) each by  $1/\sqrt{\kappa_{rr}}$  and set the numerator ansatz equal to  $(j+3/2)/\sqrt{\kappa_{rr}} = 3/2 + J(g_y)$ , where  $g_y$  is now the gyromagnetic ratio. This makes our equation 6.1.5, 6.1.6 compatible with the standard Dirac equation allowing us to substitute the  $g_y$  into the Heisenberg equations of motion for spin  $S$ :  $dS/dt \propto m \propto g_y J$  to find the correction to  $dS/dt$ . Thus again:

$$\begin{aligned} [1/\sqrt{\kappa_{rr}}] (3/2 + J) &= 3/2 + J g_y, \text{ Therefore for } J = \frac{1}{2} \text{ we have:} \\ [1/\sqrt{\kappa_{rr}}] (3/2 + \frac{1}{2}) &= 3/2 + \frac{1}{2} g_y = 3/2 + \frac{1}{2} (1 + \Delta g_y) \end{aligned} \quad (6.1.7)$$

Then we solve for  $\Delta g_y$  and substitute it into the above  $dS/dt$  equation.

Thus solve eq. 5.1.12, 6.1.7 with eq.6.1.1 values in  $\sqrt{\kappa_{rr}} = 1/\sqrt{(1+\Delta\varepsilon/(1+\varepsilon))} = 1/\sqrt{(1+\Delta\varepsilon/(1+0))} = 1/\sqrt{(1+.0005799/1)}$ . Thus from equations 6.1.1, 6.1.5, 6.1.7:

$[1/\sqrt{(1+.0005799)}] (3/2 + \frac{1}{2}) = 3/2 + \frac{1}{2} (1 + \Delta g_y)$ . Solving for  $\Delta g_y$  gives anomalous **gyromagnetic ratio correction of the electron**  $\Delta g_y = .00116$ .

If we set  $\varepsilon \neq 0$  (so  $\Delta\varepsilon/(1+\varepsilon)$ ) instead of  $\Delta\varepsilon$  in the same  $\kappa_{00}$  in eq.16 we get the anomalous **gyromagnetic ratio correction of the muon** in the same way.

**Composite 3e: Meisner effect For B just outside  $r_H$ . (where the zero point energy particle eq. 9.22 is  $.08=\pi^\pm$ ) See 5.1.11**

Composite 3e CASE 1: Plus  $+r_H$ , therefore is the proton + charge component. Eq.6.1.1 & 5.1.11  $1/\kappa_{rr}=1+r_H/r_H+\epsilon''=2+\epsilon''$ .  $\epsilon''=.08$  (eq.9.22). Thus from eq.6.1.7:  $\sqrt{2+\epsilon''}(1.5+.5)=1.5+.5(\text{gy})$ ,  $\text{gy}=2.8$

**The gyromagnetic ratio of the proton**

Composite 3e CASE 2: negative  $r_H$ , thus charge cancels, zero charge:

$$1/\kappa_{rr}=1-r_H/r_H+\epsilon''=\epsilon \quad \text{Therefore from equation 6.1.7 and case 1 eq.12 } 1/\kappa_{rr}=1-r_H/r_H+\epsilon'' \\ \sqrt{\epsilon''}(1.5+.5)=1.5+.5(\text{gy}), \text{gy}=-1.9.$$

the **gyromagnetic ratio of the neutron** with the other charged and those ortho neutral hyperon magnetic moments scaled using their masses by these values respectively.

## C2 Separation of Variables

After separation of variables the “r” component of equation 16 (Newpde) can be written as

$$\left[ \left( \frac{dt}{ds} \sqrt{\kappa_{00}} m_p \right) + m_p \right] F - \hbar c \left( \sqrt{\kappa_{rr}} \frac{d}{dr} + \frac{j+3/2}{r} \right) f = 0 \quad (6.1.5)$$

$$\left[ \left( \frac{dt}{ds} \sqrt{\kappa_{00}} m_p \right) - m_p \right] f + \hbar c \left( \sqrt{\kappa_{rr}} \frac{d}{dr} - \frac{j-1/2}{r} \right) F = 0. \quad (6.1.6)$$

Comparing the flat space-time Dirac equation to the left side terms of equations 6.1.5 and 6.1.6:

$$(dt/ds)\sqrt{\kappa_{00}}=(1/\kappa_{00})\sqrt{\kappa_{00}}=(1/\sqrt{\kappa_{00}})=\text{Energy}=E \quad (6.1.8)$$

Note for electron motion around hydrogen proton  $mv^2/r=ke^2/r^2$  so  $KE=\frac{1}{2}mv^2=(\frac{1}{2})ke^2/r=PE$  potential energy in  $PE+KE=E$ . So for the electron (but not the tauon or muon that are not in this orbit)  $PE_e=\frac{1}{2}e^2/r$ . Here write the hydrogen energy and pull out the electron contribution. So in eq.B1 and 6.1.8:  $r_H'=(1+1+.5)e^2/(m_\tau+m_\mu+m_e)/2=2.5e^2/(2m_p c^2)$ . (6.1.9)

**Variation  $\delta(\psi^*\psi)=0$  At  $r=n^2a_0$**

Next note for the variation in  $\psi^*\psi$  is equal to zero at maximum  $\psi^*\psi$  probability density where for the hydrogen atom is at  $r=n^2a_0=4a_0$  for  $n=2$  and the  $\psi_{2,0,0}$  eigenfunction. Also recall eq.B1  $\xi_1=m_L c^2=(m_\tau+m_\mu+m_e)c^2=2m_p c^2$  normalizes  $\frac{1}{2}ke^2$  (Thus divide  $\tau+\mu$  by 2 and then multiply the whole line by 2 to normalize the  $m_e/2$ .result.  $\epsilon=0$  since no muon  $\epsilon$  here.): Recall in eq.17  $\xi_0$  has to be pulled in a Taylor expansion as an operator since it a separate observable So substituting eqs. 5.1.16, 6.1.1 and eq. 5.1.12 for  $\kappa_{00}$ , and B1, 6.1.1 values in eq.6.1.8:

$$E_e = \frac{(tauon + muon)(\frac{1}{2})}{\sqrt{1 - \frac{r_H'}{r}}} - (tauon + muon + PE_\tau + PE_\mu - m_e c^2) \frac{1}{2} = \\ 2(m_\tau c^2 + m_\mu c^2) \frac{1}{2} + 2 \frac{m_e c^2}{2} + 2 \frac{2.5e^2}{2r(m_L c^2)} m_L c^2 - 2 \frac{2e^2}{2r(m_L c^2)} m_L c^2 - 2 \frac{3}{8} \left( \frac{2.5e^2}{rm_L c^2} \right)^2 m_L c^2 \\ - 2(m_\tau c^2 + m_\mu c^2) \frac{1}{2} \\ = \frac{2m_e c^2}{2} + 2 \frac{e^2}{4r} - 2 \frac{3}{8} \left( \frac{2.5}{rm_L c^2} \right)^2 m_L c^2 = m_e c^2 + \frac{e^2}{2r} - 2 \frac{3}{8} \left( \frac{2.5e^2}{rm_L c^2} \right)^2 m_L c^2$$

So:  $\Delta E_e = 2 \frac{3}{8} \left( \frac{2.5}{rm_L c^2} \right)^2 m_L c^2 = (\text{Third order } \sqrt{\kappa_{\mu\mu}} \text{ Taylor expansion term}) =$

$$\Delta E = 2 \frac{3}{8} \left[ \frac{2.5(8.89 \times 10^9)(1.602 \times 10^{-19})^2}{(4(.53 \times 10^{-10}))^2((1.67 \times 10^{-27})(3 \times 10^8)^2)} \right]^2 (2(1.67 \times 10^{-27})(3 \times 10^8)^2)$$



$=hf=6.626 \times 10^{-34} \times 27,360,000$  so that  $f=27\text{MHz}$  Lamb shift.  
The other  $1050\text{MHz}$  comes from the zitterbewegung cloud.

### Why Does The Ordinary Dirac Equation ( $\kappa_{\mu\nu}=\text{constant}$ ) Require Infinite Fields?

Note from section 1.2 that  $\kappa_{\mu\nu}$ =possibly nonconstant. So it does not have to be flat space, whereas for the standard Dirac equation  $g_{\mu\nu}=\text{constant}$  in eq. 4.2.1. Also eq.16 has closed form solutions (eg. section 4.9), no infinite fields required as we see in the above eq.6.12.1. So why does the mainstream solution require infinite fields (caused by infinite charges)? To answer that question recall the geodesics  $\Gamma^m_{ij}v^i v^j$  give us accelerations, with these  $v^k$  s limited to  $<c$ . Recall  $g_{ij}$  also contains the potentials (of the fields)  $A_i$ . We can then take the pathological case of  $\int g^{ij} = \int A = \infty$  in the S matrix integral context and  $\partial g_{ik}/\partial x^j = 0$  since the mainstream (circa 1928) Dirac equation formalism made the  $g_{ij}$  constants in eq.4.2.1. Then  $\Gamma^m_{ij} \equiv (g^{km}/2)(\partial g_{ik}/\partial x^j + \partial g_{jk}/\partial x^i - \partial g_{ij}/\partial x^k) = (1/0)(0) = \text{undefined}$ , but *not* zero. Take the  $\partial g_{ik}/\partial x^j$  to be mere 0 *limit* values and then  $\Gamma^\alpha_{\beta\gamma}$  becomes *finite* then. Furthermore 9.13 (Coulomb potential) would then imply that  $A_0=1/r$  (and  $U(1)$ ) and note the higher orders of the Taylor expansion of the Energy= $1/(1-1/r)$  term ( $=1-1/r+(1/r)^2-(1/r)^3 \dots$  (geometrical series expansion) where we could then represent these  $n$ th order  $1/r^n$  terms with individual  $1/r$  Coulomb interactions accurate if doing alternatively Feynman vacuum polarization graphs in powers of  $1/r$ ). Also we could subtract off the infinities using counterterms in the standard renormalization procedure. *Thus in the context of the S matrix this flat space-time could ironically give nearly the exact answers if pathologically  $\int A = \infty$  and so we have explained why QED renormalization works!* Thus instead of being a nuisance these QED infinities are a necessity if you *mistakenly* choose to set  $r_H=0$  (so constant  $\kappa_{ij}$ ).

But equation 16 is not in general a flat space time (i.e., in general  $\kappa_{\mu\nu} \neq \text{constant}$ ) so **we do not need these infinities and the renormalization** and we still keep the precision predictions of QED, where in going from the  $N+1$ th fractal scale to the  $N$ th fractal scale  $r_H=2GM/c^2 \rightarrow 2e^2/m_e c^2$  See sect.3.9 and Ch.1.2.4 where we calculate the Lamb shift and anomalous gyromagnetic ratio in closed form from our eq.16 energy 1.21:  $E=1/\sqrt{\kappa_{00}}=1/\sqrt{(1-r_H/r+\Delta\epsilon)}$  (Ch.3.9) and the square root in the separable eq.16 (Ch.1.2.4 and section 6.12 for Lamb shift calculation without renormalization.).

### Metric quantization (and C) As A Perturbation Of the Hamiltonian

$$H_0 \psi = E_n \psi_n$$

for normalized  $\psi_n$ s. We introduce a strong *local* metric perturbation  $H'=\Delta G$  due to motion through matter let's say so that:

$H'+H=H_{\text{total}}$  where  $H \equiv \Delta G$  is due to the matter and  $H$  is the total Hamiltonian due to all the types of neutrino in that  $H_{M+1}$  of section 4.6.  $H'=C^2$ . Because of this metric perturbation

$\psi = \sum a_i \psi_{i1}$  = orthonormal eigenfunctions of  $H_0$ .  $|a_i|^2$  is the probability of being in the neutrino state  $i$ . The nonground state  $a_i$ s would be (near) zero for no perturbations with the ground state energy  $a_i$  (electron neutrino) largest at lowest energy given for ordinary beta decay for example. Thus the passage through matter creates the nonzero higher metric quantization states (i.e.,  $H'$  can add energy) with:

$$a_k = (1/(\hbar i)) \int H'_{ik} e^{i\omega_{lk}t} dt$$

$$\omega_{lk} = (E_k - E_l)/\hbar$$

Thus in this way motion through matter perturbs these mixed eigenstates so that one type of neutrino might seemingly change into another (oscillations).

Note: Need infinities if **flat space Dirac 1928 equation**. For flat space  $\partial g_{ik}/\partial x^j = 0$  as a limit. Then must take field  $g^{km} = 1/0 = \infty$  to get finite Christoffel symbol  $\Gamma^m_{ij} \equiv (g^{km}/2)(\partial g_{ik}/\partial x^j + \partial g_{jk}/\partial x^i - \partial g_{ij}/\partial x^k) = (1/0)(0) = \text{undefined}$  but still implying *nonzero* acceleration on the left side of the

geodesic equation:  $\frac{d^2 x^\mu}{ds^2} = -\Gamma^\mu_{\nu\lambda} \frac{dx^\nu}{ds} \frac{dx^\lambda}{ds}$  So we need infinite fields for flat space. Thus QED

requires (many such) infinities. But we have in general curved space  $g_{ij} = \kappa_{ij}$  in the New pde so do not require that anything be infinite and yet we still obtain for the third order Taylor expansion term of  $\sqrt{\kappa_{\mu\nu}}$  the Lamb shift and anomalous gyromagnetic ratio correction (see above sections C2, C3).

So renormalization is a perturbative way (given it's flat space Dirac equation and minimal interaction gauge origins) of calculating these (above) same, *NON* perturbative results, it's a perturbative GR theory. But renormalization gives lots of wrong answers too, eg.,  $10^{96}$  grams/cm<sup>3</sup> vacuum density for starters. (So we drop it here since we don't need it any longer for the high precision QED results.) In contrast note near the end of reference 5 our  $G_{00} = 0$  for a 2D MS. Thus a vacuum really is a vacuum. Also that large  $\xi_1 = \tau(1 + \varepsilon')$  in  $r_H$  in eq.14 is the reason leptons appear point particles (in contrast to the small  $\xi_0$  in the composite  $3e$  baryons).

## 6.2 N=1 internal Observer cosmological physics from Laplace Beltrami

The Laplacian of the metric tensor (in Newpde zitterbewegung harmonic local coordinates whose components satisfy Ricci tensor  $= R_{ij} = -(1/2)\Delta(g_{ij})$  where  $\Delta$  is the Laplace-Beltrami second derivative operator) is not zero and the right side is the metric source. Geometrically, the Ricci curvature is the mathematical object that controls the (commoving *observer*) *growth rate of the volume* of metric balls in a manifold in this case given by the New pde source zitterbewegung. Set the phase so real  $\Delta g_{ii}$  is small at time=0 (big bang from  $r_{bb}$ ) then initial  $\sin\theta_0 = \sin 90^\circ$ . Given the  $\varepsilon + \Delta\varepsilon$  on the right side of eq.5.1.9:

$$R_{22} = 1/2 \Delta g_{22} = e^{i(\varepsilon + \Delta\varepsilon)} e^{i\pi/2} = \sin(\varepsilon + \Delta\varepsilon) + i \cos(\varepsilon + \Delta\varepsilon). \quad 6.2.1$$

This is Ricci tensor exterior source to the interior ( $r < r_H$ ) comoving metric.

Recall  $N > 0$  observer sees next smaller fractal scale objects  $N = 0$ . (sect.1) Laplace Beltrami for  $N = 1$ , with inside  $\mu \rightarrow i\mu$  tells us what we see of the much larger cosmos from the *inside*.

**Real part  $R_{22}$  commoving inside**  $r_H$  for small  $i\mu = \varepsilon$  (so  $\sin \rightarrow -\sinh$ ) over large region so neglect tiny  $\Delta\varepsilon$ :  $R_{22} = e^{-\nu} [1 + 1/2 r(\mu' - \nu')] - 1 = -\sinh \nu = -(e^\nu - e^{-\nu})/2$ ,  $\nu' = -\mu'$  so  $e^{-\mu} [-r(\mu')] = -\sinh \mu - e^{-\mu} + 1 = (-e^{-\mu} + e^\mu)/2 - e^{-\mu} + 1 = (-e^{-\mu} + e^\mu)/2 + 1 = -\cosh \mu + 1$ . So  $e^{-\nu} [-r(\mu')] = 1 - \cosh \mu$ . Thus  $e^{-\mu} r(d\mu/dr) = 1 - \cosh \mu$ . This can be rewritten as:  $e^\mu d\mu / (1 - \cosh \mu) = dr/r$ . The integration is from  $\xi_1 = \mu = \varepsilon = 1$  to the present day mass of the muon = .06 (X tauon mass) 6.2.2.

$$\text{We then get: } \ln(r_{M+1}/r_{bb}) + 2 = [1/(e^\mu - 1) - \ln[e^\mu - 1]]/2 \quad 6.2.3$$

then  $r_{bb} \approx 50 \text{ Mkm} \equiv \text{mercuron}$  (initial  $r = r_H$  each baryon. Big bang  $10^{82}$  baryons sect.2.3).

(approximayely the orbital radius of Mercury.) Solve for  $r_{M+1}$ , as function of  $\mu$ . Find present derivative, find  $du$  from Hubble constant normalize the number to 13.7 to find total time  $u$ . Find we are now at 370by. This long of time explains the cbr thermalization and mature galaxies at dawn (instead of  $\sim 200 \text{ My}$  after bb, it is 370by). The zitterbewegung (sound wave) of object B creates the condensation (at the Shapely concentration) and rarefaction void in Eridanus: we are astronomically observing here selfsimilar sound waves *inside* of a proton.

After a large expansion from  $r_{bb}$  our eq.14 eq.15 Schwarzschild finally becomes **Minkowski**  $ds^2 = -dx_0^2 + \sum_{i=1}^n dx_i^2$ . The submanifold is  $-x_0^2 + \sum_{i=1}^n x_i^2 = \alpha^2$

In static coordinates  $r, t$ : (the **New pde** zitterbewegung **harmonic coordinates**  $x_i$  for  $r < r_H$ )

$x_0 = \sqrt{(\alpha^2 - r^2)} \sinh(t/\alpha)$ : (sinht is small t limit of equation D15. 5Tyears is the period >> 370by)  
 $x_1 = \sqrt{(\alpha^2 - r^2)} \cosh(t/\alpha)$ :  
 $x_i = rz_i$   $2 \leq i \leq n$   $z_i$  is the standard imbedding  $n-2$  sphere.  $R^{n-1}$  which also implies the **De Sitter**  
 metric:  $ds^2 = -(1-r^2/\alpha^2)dt^2 + (1-r^2/\alpha^2)^{-1}dr^2 + d\Omega_{n-2}^2$  (D16) **our observed ambient metric**

**6.3 Mixed states of  $\Delta\epsilon$  and  $\epsilon$**  outside  $r_H$  so  $1S_{1/2}$  state within  $r_{HN}$  ( $\Delta x \Delta m_{N=1} c$ )  $= \hbar/2$ .  $m_{N=1} = 10^{-40} m_e$ . For  $1S_{1/2}$  state  $m_\mu = 207 m_e$  and so  $\Delta x = 10^5 LY$  galaxy.  $1S_{1/2}$  state may be flattened since such states are stable since then  $g_{00} = \kappa_{00}$ .

From D13 metric source note  $\Delta\epsilon$  and  $\epsilon$  operators so  $\Delta\epsilon\epsilon$  (operating on Newpde  $\psi_N$ ) is a new state, a “mixed state” that in the next higher scale classical limit then is a grand canonical ensemble with nonzero chemical potential (i.e., a “mixture” of systems). 2nd derivative of  $\cos x = -\cos x$  so  $\Delta g_{00} = -g_{00} = \cos \Delta\epsilon$ . That  $g_{00} = \kappa_{00}$  in the *halo of the Milky Way galaxy* is the fundamental equation of metric quantization for all the multiples of 100 metric quantization, but here for  $r < r_H$ . So in general  $\kappa_{00} = e^{i(me + mu)}$ ,  $m_e = .000058$  is the electron mass (as a fraction of the Tauon mass.) which is the component in the resulting  $m_e, m_\mu$  operator sequence.

**Imaginary part  $R_{22}$**  locally for 2D MS  $R_{00} = \Delta g_{00} = \kappa_{00}(R/2) = \cos \Delta\epsilon$  gives also the local mixed  $\Delta\epsilon, \epsilon$  states of part III metric quantization. Set  $\cos(\Delta\epsilon/(1-2\epsilon)) = \kappa_{00} = g_{00}$ ,  $mv^2/r = GMm/r^2$  so  $GM/r = v^2$  COM in the galaxy halo (circular orbits)  $(1/(1-2\epsilon))$  term from D9a just inside  $r_H$  so **Pure state  $\Delta\epsilon$**  ( $\epsilon$  excited  $1S_{1/2}$  state of ground state  $\Delta\epsilon$ , so not same state as  $\Delta\epsilon$ )

$Rel \kappa_{00} = \cos \mu$  from D9

**Case 1**  $1 - 2GM/(c^2 r) = 1 - 2(v/c)^2 = 1 - (\Delta\epsilon/(1-2\epsilon))^2/2$  (6.3.1)

So  $1 - 2(v/c)^2 = 1 - (\Delta\epsilon/(1-2\epsilon))^2/2$  so  $=(\Delta\epsilon/(1-2\epsilon))c/2 = .00058/(1-(.06)^2)(3 \times 10^8)/2 = 99 \text{ km/sec}$   
 $\approx 100 \text{ km/sec}$  (Mixed  $\Delta\epsilon, \epsilon$ , states classically here are grand canonical ensembles with nonzero chemical potential.). For ringed (not hub) galaxies the radial value becomes  $100/2 = 50 \text{ km/sec}$ .

**Mixed state  $\epsilon \Delta\epsilon$**  (Again  $GM/r = v^2$  so  $2GM/(c^2 r) = 2(v/c)^2$ .)

**Case 2**  $g_{00} = 1 - 2GM/(c^2 r) = Rel \kappa_{00} = \cos[\Delta\epsilon + \epsilon] = 1 - [\Delta\epsilon + \epsilon]^2/2 = 1 - [(\Delta\epsilon + \epsilon)^2/(\Delta\epsilon + \epsilon)]^2/2 = 1 - [(\Delta\epsilon^2 + \epsilon^2 + 2\epsilon\Delta\epsilon)/(\Delta\epsilon + \epsilon)]^2$

The  $\Delta\epsilon^2$  is just the above first case (Case 1) so just take the mixed state cross term

$[\epsilon \Delta\epsilon / (\epsilon + \Delta\epsilon)] = c[\Delta\epsilon / (1 + \Delta\epsilon/\epsilon)]/2 = c[\Delta\epsilon + \Delta\epsilon^2/\epsilon + \dots \Delta\epsilon^{N+1}/\epsilon^{N+1}]/2 = \Sigma v_N$ . Note each term in this expansion is itself a (mixed state) operator. So there can't be a single  $v$  in the large gradient 2<sup>nd</sup> case so in the equation just above we can take  $v_N = [\Delta\epsilon^{N+1}/(2\epsilon^N)]c$ . (6.3.2)

From eq. D18 for example  $v = m 100^N \text{ km/sec}$ .  $m=2, N=1$  here (Local arm). In part III we list hundreds of examples of D18: (sun,  $1.2 \text{ km/sec}$ , galaxy halos  $m 100 \text{ km/sec}$ ). The linear mixed state subdivision by this ubiquitous  $\sim 100$  scale change factor in  $r_{bb}$  (due to above object B zitterbewegung spherical Bessel function resonance boundary conditions resulting in nodes) created the voids. Same process for  $N-1$  (so 100X smaller) antinodes get galaxies, 100X smaller: globular clusters, 100X smaller solar systems, etc., So these smaller objects were also created by mixed state metric quantization (eq. D18) resonance oscillation inside initial radius  $r_{bb}$ .

We include the effects of that object B drop in inertial frame dragging on the inertial term  $m$  in the Gamow factor and so lower  $Z$  nuclear synthesis at earlier epochs ( $t > 18 \text{ by}$ ) BCE. (see part III)

## Equipartition of Energy

So from the above section at the horizon  $r \rightarrow 1/r^2$  so  $t \rightarrow 1/t^2$  in  $\kappa_{00} = 1 - r_H/r$  and so inside  $r_H$  vibrational states are at low frequency and rotational states at high frequency. Also recall for

quantum mechanical equipartition of energy outside  $r_H$  rotational vibration and rotational states are the same energy inside then that makes each vibrational wave have much more energy than each rotational wave. See equipartition of energy inside deuteron PartII. Ch.11

#### 6.4 This Added Object B $(a/r)^2$ term Is Then The Source Of The Ambient Metric And Mass

Tensor Geometry Consequences of  $C^2$

Recall section 4 implies General relativity (recall eq.14,14a and the Schwarzschild metric derivation there). But the context is that of keeping equation 1  $C^2$  and so that local MandelbulbLepton model.eq.1.10 flat space ambient metric manifold. In that regard given a (observable) vector operator  $A$  that explicitly operates on the  $\psi$  of equation 1.24) we can then construct the Riemann Christoffel Tensor of the Second Kind  $R^a_{bcd}$  (from section 4. we can assume it is a quantum operator) from the  $\kappa_{ab} \equiv g_{ab}$  using the  $C^2$  of  $A$  given by  $(A_{i,jk}-A_{i,kj})|a,t\rangle = (R^m_{ijk}A_m)|a,t\rangle$ . We can then contract this  $R^m_{ijk}A_m|a,t\rangle$  tensor to get the Ricci tensor  $R_{ij}$  (here  $R_{ij} \equiv R^m_{ijm}$ ).

Note here  $A$  is the Quantum Operator and the coefficient  $R_{\mu\nu}$  is a (geometry) tensor. Define the scalar  $R = \kappa^{\mu\nu}R_{\mu\nu}$  We then define conserved quantity  $Z_{\mu\nu}$  from

$$R_{\mu\nu} - \frac{1}{2}\kappa_{\mu\nu}R \equiv Z_{\mu\nu} \quad (6.4.3)$$

after substituting in equations 3.2, 4.1 we see for example that  $Z_{00} = 4\pi r_H$  (6.4.4) where from equation 4.4.3 we have  $r_H = 2e^2/m_e c^2$ .

In free space we can see from equation 4.2 that:  $R_{\mu\nu}A_\nu|a,t\rangle = 0$

#### $\epsilon, \Delta\epsilon$ as operators

Alternatively write  $\epsilon, \Delta\epsilon$  as operators on the eq.1.2.7  $\psi$ . So  $\epsilon$  does not operate on  $\Delta\epsilon$  (for example  $\epsilon\Delta\epsilon\psi=0$ ). allowing us to write the  $\kappa_{00}$  component of 6.4.13 where ansatz  $e^C$  generates  $e^\mu = g_{00} = e^{i(2\epsilon+\Delta\epsilon)} = \kappa_{00}$  above only if  $\epsilon, \Delta\epsilon$  act as operators.

$$g_{00} = e^{i(2\epsilon+\Delta\epsilon)} \quad (6.4.15)$$

for background metric case.  $\epsilon = .060406$ .

Note the  $(a/r)^2$  in 6.4.14 is then the  $\epsilon + \Delta\epsilon$  in the denominator on the right side of eq.6.4.13, the main reason we went to so much trouble to derive 6.4.13. Thus we have shown how a nearby object B creates mass in object A.

Note  $(r,t)X(\phi,\theta)$  is a Cartesian product of two 2D spaces here.

Thus the  $(a/r)^2$  term in Eq.6.4.13 thus provides a background metric and this ambient metric then provides the mass of the fundamental leptons. Tauon (1), muon ( $\epsilon$ ) and electron ( $\Delta\epsilon$ ). Object B and object A are two body object on the next fractal scale (with  $w_B = w_A$  at the  $r_H$  boundary due to causality) effect of causing a drop in inertial frame dragging and a increase in the mass of the particles through the mass degeneracy provided by quantum mechanical vibrational  $\tau$  tauon and rotational  $\epsilon$  muon and ground state  $\Delta\epsilon$  electron metric quantization eigenstates of object A and B together. In  $\kappa_{00} = 1 + \epsilon + \Delta\epsilon - r_H/r$ . (6.4.1)

#### Normalization

Equation 6.1.2 (Kerr) and equation 6.4.1 and 6.4.13 (ambient metric) thereby shows how to normalize. Recall normalization of  $z = (1 + \delta z) + \delta z'$  using  $1/(1 + \delta z)$  was required (sect.1.2) to also have the neighborhood (and not just the point) a subset of the Mandelbrot set.

**Details:** Ambient metric  $1 - \epsilon$  in the Kerr  $(a/r)^2$  is normalized out. The ground state  $\Delta\epsilon$  cannot be normalized out. Because  $\kappa_{00} = \xi_1 - r_H/r$ , all 3 leptons are in sect.1.2. So the new pde normalization results for  $z=1$  are  $\kappa_{00} = 1 - (C_M/\xi_1)/r$ ,  $\kappa_r = 1/(1 - (\Delta\epsilon/(1 - \epsilon)) - (C_M/\xi_1)/r)$ . (6.6.15)

For  $z=0$ ,  $2P_{1/2}$  and  $2P_{3/2}$  at  $r=r_H$  so  $\kappa_{00} = 1 - \epsilon - \Delta\epsilon - (C_M/\xi_0)/r$ ,  $\kappa_r = 1/(1 - \epsilon - ((C_M/\xi_0)/r))$  (6.6.16)

because of the Meisner effect  $\varepsilon$  (partII) as in eq. 6.4.13.  $2P_{1/2}$  at  $r=r_H$   $z=0 \rightarrow z=1$  transition occurs when the internal virtual decay event occurs so that there is no Meisner effect  $\varepsilon$ , just the usual object B background  $\varepsilon$ . See (6.6.17)

In  $2P_{1/2}$  at exactly  $r=r_H$  (with small but nonzero probability) we have  $z=0 \rightarrow 1z=$  case since we have a huge  $\xi_1$  so we again normalize out  $1-\varepsilon$  and so  $\kappa_{00}=1-\Delta\varepsilon/(1\pm\varepsilon)-((C_M/\xi_0)/r)$  for  $r=r_H$ .

(6.6.17) transition case. In summary:

$$\mathbf{z=1,0} \text{ so } r_H = \Sigma C_M / (\xi_3 + \xi_2 + \xi_0) \equiv \Sigma C_M / \xi_1 \text{ in eq.16; sect.6.3} \quad \text{infinitesimal rotation} \\ \kappa_{rr} = 1 / [(1 - \Delta\varepsilon / (1 \pm \varepsilon) - (C_M / \xi_1) / r)], \text{ and } \kappa_{00} = 1 - (\Sigma C_M / \xi_1) / r \quad (6.6.15)$$

$$\mathbf{z=0} \text{ alone sect.1.2 } r_H = C_M / \xi_0 \quad \text{180° rotation} \\ \kappa_{rr} = 1 / [(1 - \varepsilon / (1 \pm \varepsilon) - (C_M / \xi_0) / r)], \text{ and } \kappa_{00} = 1 - (C_M / \xi_0) / r \quad (6.6.16)$$

### Transitions

$\mathbf{z=0} \rightarrow \mathbf{z=1}$

$$\kappa_{rr} = 1 / [(1 - \Delta\varepsilon / (1 \pm \varepsilon) - (\Sigma C_M / \xi_1) / r)], \text{ and } \kappa_{00} = 1 - (\Sigma C_M / \xi_1) / r$$

$\mathbf{z=1} \rightarrow \mathbf{z=0}$  tauon and muon decay into electrons at  $r=r_H$  contained by flux quantization.

$$\kappa_{rr} = 1 / [(1 - \varepsilon / (1 \pm \varepsilon) - (C_M / \xi_0) / r)], \text{ and } \kappa_{00} = 1 - (C_M / \xi_0) / r$$

Small C boost gets  $z=zz$  (so postulate 1) but also gets the **numerical value of Large  $\xi_1$**

For that stable  $z=0$  the only way to get stable large  $\xi$  (required by that small C boost) is with the Newpde **composite 3e**  $2P_{3/2}$  at  $r=r_H$  state (partII davidmaker.com). So *stability*  $(dt')^2 = (1 - r_H/r)dt^2$  clocks stop at  $r=r_H$ . The *two positron motion* and  $h/2e$  quantization of flux BA then gives us the exact proton mass  $m_p$  as a reduced mass for the associated Hund rule  $\tau \equiv 2S_{1/2}, 1S_{1/2} \equiv \mu$  states (so  $\tau + \mu = \xi_1$ ,  $m_p = \xi_1/2$ ). We rewrite this in the Kerr metric formalism with the 3<sup>rd</sup> mass also reversing the pair annihilation (Thus virtual pair creation inside the  $r_H$  volume given  $\sigma = \pi r_H^2 \approx (1/20)$  barns) and reducing the inertial frame dragging due to the spin  $1/2$   $\xi_1$  thereby adding a Kerr metric  $-(a/r)^2$  angular momentum operator in object 'A' ambient metric (see PartI, sect.6.4). Object B is responsible for the electron's nonzero mass. From eq.6.4.13:  $\kappa_{00} = 1 - C_M / (\xi_1 r) = 1 - 2e^2 / (2m_p r)$  (12)

$$\kappa_{rr} = 1 / (1 - \xi_0 / (1 + \varepsilon) - C_M / (\xi_1 r)) = 1 / (1 + \Delta\varepsilon / (1 + \varepsilon) - 2e^2 / (2m_p r))$$

( $C_M$  is  $e^2$  charge) also giving us the **numerical value** of that **large  $\xi_1$**  ( $=2m_p$ ). With  $\tau$  normalized to  $\tau=1$  with the Newpde ground state  $e$  mass then  $\Delta\varepsilon = m_e = .0005799$  with  $\varepsilon = \mu = .06$  (12a)

## 6.7 Fractal Selfsimilarity And Object B Implications

Given our  $dr$  frame of reference between our two fractal baseline scales separated by that  $10^{40}X$  scale jump we have that  $dr dr < < dr = C_M$  (subatomic) and  $dr < < dr' dr' = C'_M$  (cosmological, sect.4.1) in the context of the Kerr metric.

Given object B decreases the effects of frame dragging and so accentuates the effect of the Kerr metric  $(a/r)^2$  term thereby creating a nonzero mass  $\xi$  in the  $g_{00}$  of the Kerr metric: the self similarity between the two baseline scales implies that  $C'_M \propto C_M$  so that  $dr' dr' \propto dr$  and so:

$$K dr' dr' = K \left( \frac{a}{r} \right)^2 = \xi dr \equiv \xi r_H,$$

$$K = \frac{r_{Ho}}{m_0 c^2}, \quad a/r \equiv \xi r \frac{dr}{dt} \frac{1}{r}, \quad dr = \lambda, \quad v = dr/dt, \quad m = \xi, \quad h = Kc/ds. \quad \text{So } \lambda = \frac{h}{mv} \quad (6.6.1)$$

This result in the context of sect.1.1 (eq.1.1.15,  $mv/\hbar \equiv k = 2\pi/\lambda$ ) allows you to interpret  $dr$  as a wave length  $\lambda$ . So we defined both mass  $\xi$  and derived the De Broglie wavelength  $\lambda$  and found the origin of Planck's constant  $h$  and so found the origin of quantum mechanics and mass.

## 6.10 Multiple Applications Of The eq.B6

### Ultrarelativistic Object B Also Source Of The Mexican Hat Potential

Recall equation B6. Equation B6

So from the fractal theory object B has to be ultrarelativistic ( $\gamma=1836$ ) for the positrons to have the mass of the proton. So the time behaves like  $mc^2$  energy: has the same gamma:  $t \rightarrow t_0/\sqrt{(1-v^2/c^2)}=KH$  since energy  $H=m_0c^2$  has the same  $\gamma$  factor as time does. So in the  $e^{iHt}$  of object B the  $Ht/\hbar=(H/\sqrt{(1-v^2/c^2)})t_0/Kt_0=KH^2=\phi^2$ . Define  $\phi=H\sqrt{K}$ . Note also ultrarelativistically that  $p$  is proportional to energy: for ultrarelativistic motion  $E^2=p^2c^2+m_0^2c^4$  with  $m_0$  small so  $E=Kp$ .

Suppressing the inertia component of the  $\kappa$  thus made us add a scalar field  $\phi$ . Thus

$\phi'=p(t)=e^{iHt/\hbar}|p_0\rangle=\cos(Ht/\hbar)=\exp(iH^2t_0/Kt_0)=\exp(i\phi^2)=\cos(\phi^2)=\phi'=1-\phi^4/2$ . Thus for a Klein Gordon boson we can write the Lagrangian as  $L=T-V=(d\phi/dx)(d\phi/dx)-\phi'^2=(d\phi/dx)(d\phi/dx)-\phi'^2=(d\phi/dx)(d\phi/dx)-i(1-\phi^4)^{1/2}$ . Thus we define this Klein Gordon scalar field  $\phi$  by itself from:

$$(D_\mu)^t(D_\mu\phi) - \frac{1}{4}\lambda(((\phi^t\phi)^2 - v^2))^2 \text{ Note in the covariant derivative}$$

$$D_\mu\phi = \left[ \partial_\mu + igW_\mu t + ig'\frac{1}{2}B_\mu \right] \phi$$

$W$  is from our new pde S matrix. Need the  $B_\mu$  of the form it has to make the neutrino charge zero. Need to put in a zero charge  $Z$ . The  $B$  component is generated from the  $r_H/r$  and the structure of the  $B$  and  $A=W+B=A_\mu = \cos\theta_W B_\mu + \sin\theta_W W_\mu^1$  is needed to both have a zero charge neutrino and nonzero mass electron. So Define

$$A_\mu = \cos\theta_W B_\mu + \sin\theta_W W_\mu^1$$

$$Z_\mu = -\sin\theta_W B_\mu + \cos\theta_W W_\mu^1$$

The left handed doublet was given by the fractal theory (section 4.4)

$$l_e = \begin{pmatrix} \nu_{EL} \\ e_L \end{pmatrix}$$

$W$  is needed in  $W+B$  to bring in the epsilon ambient metric mass.

Need to add the second term to the Dirac equation to give the electron mass.

$$\Lambda L_e = e_R i\gamma^\mu (\partial_\mu - ig'B_\mu) e_R - f_\mu (l_e \phi_e + e_R \phi l_e)$$

Recall section 4.9 ambient metric requires division by  $(1+\varepsilon+\Delta\varepsilon+r_H/r)$  to create the nontrivial ambient metric term  $1\pm\varepsilon$ .

$$\psi(t)=e^{iHt}\psi(t_0)=e^{i(1+\varepsilon+\Delta\varepsilon)^2} \psi(t_0). \text{ See partIII}$$

## 6.11 S States Are Point like Particles And P States Are Not Point Like Particles

### P States At $r=r_H$

Recall  $\Delta\varepsilon$  is ultrarelativistic so integrating the eq.7+eq.7+eq.7(PartII) Fitzgerald contraction in the 2P state ( $L=1$ ),  $r=r_H$  gives  $(\cos\theta\equiv v/c=\beta)$ ,  $\theta=90^\circ$

$$r_H \int \sqrt{(1-\cos^2\theta)} \cos\theta d\theta = r_H \int \sin\theta \cos\theta d\theta = r_H \sin^2\theta/2 = r_H/2 \equiv r_{HP} \quad (6.11.1)$$

so there is contraction by only a factor of 2 from the vantage point of the plane of rotation (From the axial perspective the radius is Fitzgerald contracted to near zero.). From part II. The  $\varepsilon$  P state big radius:  $r_{HP} \equiv 2ke^2/\text{electron} \approx 2ke^2/m_e c^2 = 2.817F = r_H$

### NS<sub>1/2</sub> States at $r=r_H$

$$\text{From equation 1.21} \quad r_L = r_H/(m_L c^2) \quad \text{Lepton } r_L \quad (6.11.2)$$

Thus the object B: S and P state metric quantization is the source of the tiny S state radius

$$\varepsilon \equiv r_e \equiv ke^2/(\text{tauon}+\mu\text{on}) \approx ke^2/(m_L c^2) \approx 10^{-18}m \quad (6.11.3)$$

*This explains why leptons (S states) appear to be point particles and baryons aren't!*



### Pure States From eqs.7+7+7 Equation 6.13.2 (Also see Part II of This Book)

Instead of the (hybrid) mixed metric quantization state  $1/\sqrt{(\Delta\epsilon+\epsilon)}$  of sect.6.13 we find the masses of the pure states  $1/\sqrt{\Delta\epsilon}$  and  $1/\sqrt{\epsilon}$  individually in the bound state eqs.7+7+7 (or 7+7) at  $r=r_H$  of part II so that  $1-r_H/r=0$  in 6.13.2 ( $r_H$  =Nth fractal scale, our subatomic scale).

Note these are not the free particle pure states  $\Delta\epsilon$  (electron) and  $\epsilon$  (muon) giving also the galactic halo constant stellar velocities.

$e^{i\Delta\epsilon} \rightarrow 1/[\sqrt{(1-\Delta\epsilon-r_H/r)}](1/(1\pm\epsilon))=(1/\sqrt{\Delta\epsilon})(1/(1\pm\epsilon))$  =mass of W,Z i.e., same as Paschen Back:  
 $E_Z=Bu_B(0+1+1+1)$  (fixes the value of the LS coupling coefficient)

$e^{i\epsilon} \rightarrow 1/[\sqrt{(1-\epsilon-r_H/r)}](1/(1\pm\epsilon))=(1/\sqrt{\epsilon})(1/(1\pm\epsilon))$  = mass of  $\pi^\pm, \pi^0$ . || Paschen Back

Fixes the value of the LS coupling coefficient

### 6.14 More Implications of The Two Metrics Of Equation 13 Of 14 and

#### Eq.11.2 Gaussian Pillbox Approach To General Relativity

From equation 11.2 the  $\kappa_{00}=1-r_H/r$  all the comoving observers are all at  $r=r_H$  so that only circumferencial motion is allowed with the new pde zitterbewung creating some radial motion  $dr'/ds$ . Also  $dr'^2=\kappa_{rr}dr^2=[1/(1-r_H/r)]dr^2$  so that the  $dr'$  space inside this volume is very large. See equation B8 in section B3. The effect of all this math is to flip over  $r_H/r$  in the Schwarzschild metric to  $r/r_H$  in the De Sitter metric (see discussion of eq.11.2) at  $r=r_H$ :

$$ds^2=-(1-r^2/\alpha^2)dt^2+(1-r^2/\alpha^2)^{-1}dr^2+d\Omega_{n-2}^2 \quad (6.14.1)$$

which also fulfills the fundamental small C requirement of eq.1.1.14 Dirac equation

zitterbewegung (for  $r<r_c$  and  $r\approx r_H$ ) and the eq.5 Minkowski metric requirement for  $\alpha=1$ . It also

keeps our square root  $\sqrt{\kappa_{00}} = \sqrt{1 - \frac{r_H}{r}} \rightarrow \sqrt{1 - \frac{r^2}{r_H^2}}$  real. Given the geometric structure of the

4D De Sitter submanifold surface we must live on a 4D submanifold hyperspace in this many point limit. So inside  $r_H$  for empty Gaussian Pillbox (since everything is at  $r_H$ )

Minkowski  $ds^2=-dx_0^2+\sum_{i=1}^n dx_i^2$

Submanifold is  $-x_0^2+\sum_{i=1}^n x_i^2=\alpha^2$

In static coordinates  $r,t$ : (the new pde harmonic coordinates for  $r<r_H$ )

$$x_0=\sqrt{(\alpha^2-r^2)}\sinh(t/\alpha): \quad (6.14.2)$$

$$x_1=\sqrt{(\alpha^2-r^2)}\cosh(t/\alpha):$$

$x_i=rz_i$   $2\leq i\leq n$   $z_i$  is the standard imbedding  $n-2$  sphere.  $R^{n-1}$ . which also imply the De Sitter metric 6.14.3. Recall from eq. 6.13.6

$$ds^2=-(1-r^2/\alpha^2)dt^2+(1-r^2/\alpha^2)^{-1}dr^2+d\Omega_{n-2}^2 \quad (6.14.3)$$

$\alpha\rightarrow i\alpha$ ,  $r\rightarrow ir$  Outside is the Schwarzschild metric to keep  $ds$  real for  $r>r_H$  since  $r_H$  is fuzzy because of objects B and C.

For torus  $(x^2+y^2+z^2+R^2-r^2)^2=4R^2(x^2+y^2)$ .  $R$ =torus radius from center of torus and  $r$ =radius of torus tube.

Let this be a spheroidal torus with inner edge at so  $r=R$ . If also  $x=r\sin\theta$ ,  $y=r\cos\theta$ ,  $\theta=\omega t$  from the new pde

Define time from  $2R=t$  you get the light cone for  $\alpha\rightarrow i\alpha$  in equation 6.14.2.

$x^2+y^2+z^2-t^2=0$  of 6.14.1 with also  $(x=r\sin\theta, y=r\cos\theta) \rightarrow$

$(x=\sqrt{(\alpha^2-r^2)}\sinh(t/\alpha), y=\sqrt{(\alpha^2-r^2)}\cosh(t/\alpha))$ ,  $\alpha\rightarrow i\alpha$ . So to incorporate the new pde into the Gaussian pillbox inside we end up with a spheroidal torus that has flat space geodesics.

Note on a toroid surface two parallel lines remain parallel if there was no expansion. So you have a flat space which is what is what is observed. The expansion causes them to converge for negative  $t$ . Note the lines go around the spheroidal toroid back to where they started, have the effect on matter motion of a gravimagnetic dipole field.

You are looking at yourself in the sky as you if you were a baby (370by ago that is). The sky is a baby picture of YOU!

The problem is that you are redshifted out to  $z=\text{infinity}$  so all you can see of your immediate vicinity (within 2byly that is) is the nearby galaxy super clusters such as the Shapely concentration and Perseus Pisces with lower red shifts.

So these superclusters should have a corresponding smudge in the CBR in exactly the opposite direction! I checked this out. The radial component  $r = r_{M+1}$  in 6.14.1 is still a function of that  $r_{bb}$  mercuron radius in  $\ln(r_{M+1}/r_{bb}) + 2 = [1/(e^\mu - 1) - \ln[e^\mu - 1]]^2$ .

Also the  $\kappa_{oo} = 1 - r^2/r_H^2$  in 6.14.1 (instead of the external observer  $\kappa_{oo} = 1 - r_H/r$ ) in  $E = 1/\sqrt{\kappa_{oo}}$  in looking outward (internal observer) at the cosmological oscillation from the inside ( $r < r_H$ ) implies that the longer the wavelength the higher the energy cosmological “photons”. So small wavelength cosmological oscillations (eg., object C  $\Delta \epsilon$  Period=2.5My) have much smaller effects than the larger wavelength oscillations (eg.,  $\epsilon$  Period=270My).

Note the sine wave has a period of 10trillion years and we are now at 370billion years, near  $\theta = -\pi/2$  in  $r = r_o \sin \theta$  where the upswing is occurring and so accelerating expansion is occurring. This is where we start out at in the sect.7.3 derivation. Since the metric is inside  $r < r_H$  it is also a source as we see in later section 5.4

## Observations Inside Of $r_H$

The metric quantization pulses ride the metric like sound waves moving in air, including going in straight lines in our toroidal universe. That means that when we look in the direction of object B using nearby metric quantization effects, like galaxies falling into a compression part of the vibration wave, which also organizes galaxy clusters as in the Shapely and Perseus-Pisces concentration, we are looking in straight lines at least for local superclusters ( $< 2\text{BLY}$ ) and so are actually looking in the direction of object B. But the CBR E&M radiation that is bent by strong gravity follows that toroidal path and so you really are looking at the (red shifted) light coming from yourself as you formed 370BY ago in this expanding frame of reference.

So the direction to the nearby galaxy clusters, even out to the Shapely concentration, is metric quantization dependent so we have straight line observation, but the CBR follows the curved space and so the galaxy superclusters we see in a given direction have CBR concentration counterparts in exactly the opposite direction. Note distant galaxy clusters are also not seen along straight lines, but lines on that spherical torus. So you only see hints of the actual directions of object B, of the object A electron dipole, etc. for relatively nearby superclusters.

The spherical torus Bg gravimagnetic dipole shape comes from the rotational motion implied by the new pde (from eq.7). Recall the new pde applies to dipole Bg field and spin motion; The electron has spin as you know. The new pde spherical torus is applied on top of a Minkowski space-time inside  $r_H$  because the Gaussian pillbox does not (usually) contain anything if its radius is smaller than  $r_H$ . So astronomers really are observing the inside of an electron (i.e., what comes out of the new pde) in this fractal model!

## 6.15 Relevance (Of These Two Metrics Of Section 1) to Shell Model of The Nuclear Force Just Outside $r_H$

Note my model is a flat de Sitter  $\alpha \rightarrow i\alpha$  inside  $r_H$  and perturbed Schwarzschild (i.e., Kerr) just outside, the two metrics of section 1.4 and Part II (on eqs. 7+7+7) above. The transition between the two is quite smooth. So at about  $r_H$  we have a force that gets stronger as  $r$  increases. But this is what the simple harmonic oscillator does in this region. So my model gives the simple harmonic oscillator (transition to Schwarzschild metric) and the flat part inside that the Shell model people have to arbitrarily have to adhoc put in (they call it the flattening of the bottom of the simple harmonic potential energy). Anyway, the above fractal theory explains all of this. Also the object B perturbation metric is a perturbative Kerr rotation.

## 7 Comoving Coordinate System: What We Observe Of The Ambient Metric

### 7.1 Comoving Coordinate System

Here we multiply eq. 11 result  $p\psi = -i\hbar \partial\psi/\partial x$  by  $\psi^*$  and integrate over volume to define the expectation value:

$$\int \psi^* p_x \psi dV \equiv \langle p_x \rangle = \langle p, t | p_x | p, t \rangle \text{ of } p_x. \quad (7.1.1)$$

In general for any QM operator  $A$  we write  $\langle A \rangle = \langle a, t | A | a, t \rangle$ . Let  $A$  be a constant in time (from Merzbacher, pp.597). Taking the time derivative then:

$$\begin{aligned} i\hbar \frac{d}{dt} \langle a, t | A | a, t \rangle &= i\hbar \frac{d}{dt} \langle \Psi(t), A \Psi(t) \rangle = \left( \Psi(t), A i\hbar \frac{\partial}{\partial t} \Psi(t) \right) - \left( i\hbar \frac{\partial}{\partial t} \Psi(t), A \Psi(t) \right) \\ &= (\Psi(t), A H \Psi(t)) - (\Psi(t), H A \Psi(t)) = i\hbar \frac{d}{dt} \langle A \rangle = \langle A H - H A \rangle \equiv [H, A] \end{aligned}$$

In the above equation let  $A = \alpha$ , from equation 9 Dirac equation Hamiltonian  $H$ ,  $[H, \alpha] = i\hbar d\alpha/dt$  (Merzbacher, pp.597).

The second and first integral solutions to the Heisenberg equations of motion (i.e., above  $[H, \alpha] = i\hbar d\alpha/dt$ ) is:

$$r = r(0) + c^2 p/H + (\hbar c/2iH) [e^{i2Ht/\hbar} - 1](\alpha(0) - cp/H). \quad (7.1.2)$$

$$v(t)/c = cp/H + e^{i2Ht/\hbar}(\alpha(0) - cp/H)$$

Note there is no Klein paradox at  $r < \text{Compton wavelength}$  in this theory and also Schrodinger's 1930 paper on the lack of a zitterbewegung does not apply to a region smaller than the Compton wavelength. So the above zitterbewegung analysis does apply in that region. The  $\sqrt{\kappa_{00}} = \sqrt{(1 - r_H/r)}$  modifies this a little in that from the source equations for  $\kappa_{\mu\nu}$  you also need a feed back since the field itself, in the most compact form, also is a eq.4.4.1.  $G_{00}$  energy density (source).

### 7.2 $r < r_H$ $e^{\omega t}$ -1 Coordinate transformation of $Z_{\mu\nu}$ : Gravity Derived

Summary:

#### Fractal Scale Content Generation From Generalized Heisenberg Equations of Motion

Specifically  $C$  in equation 1 applies to "observable" measurement error. But from the two "observable" fractal scales  $(N, N+1)$  we can infer the existence of a 3<sup>rd</sup> next smaller fractal  $N-1$  scale using the generalized Heisenberg equations of motion giving us

$$(\partial x_{0N})/(\partial x_{0N+1}) (\partial x_{0N})/(\partial x_{0N+1}) T_{00N} - T_{00N} = T_{00N-1} \quad (7.2.3)$$

which is equation 7.4.4 below. Thus we can derive the content of the rest of the fractal scales by this process.

On top of the fractal  $10^{40}X$  smaller coupling  $G$  (ref.5) baseline this  $T_{00N-1}$  gives a smaller time dependent coshu coefficient which is what we find here.

### 7.3 Derivation of The Terms in Equation 7.2.3

For free falling frame no coordinate transformation is needed of source  $T_{00}$ . For non free falling comoving frame with  $N+1$  fractal eq.1.1.24 motion we do need a coordinate transformation to obtain the perturbation  $\Delta T$  of  $T_{00}$  caused by this motion (in the new coordinate system we also get 5.1.2: the modified  $R_{ij}$ =source describing the evolution of the universe as seen from the outside fractal  $N+1$  scale observer that *he sees that we see*. We got

$\ln(r_{M+1}/r_{bb})+2=[1/(e^\mu-1)-\ln[e^\mu-1]]/2$  in our own coordinate frame). Recall in section 1 the  $N>0$  fractal scale this larger observer *actually sees himself*.



THE DISCOVERY INSTRUMENT

Spectroscopic Slit

Slipher's Spectroscopic Focal Plane Used To Discover The Expanding Universe.  
It is in the rotunda display at Lowell Observatory.

### 7.4 Dyadic Coordinate Transformation Of $T_{ij}$ In Eq. 7.2.3 eq., 14 Frame of Reference

Given  $N+1$  fractal cosmological scale (Who just sees the  $T_{00}$ ) frame of reference we then do a radial dyadic coordinate transformation to *our*  $N$ th fractal scale frame of reference so that  $T_{00} \rightarrow T_{00}' = T_{00} + dT_{00} \equiv T_{00} + G_{00}$  (Section 7.4 attachment).

The Dirac equation object has a radial center of mass of its zitterbewegung. That radius expands due to the **ambient metric expansion** of the next larger  $N+1$ th fractal scale (Discovered by Slipher. See his above instrumentation). We define a  $Z_{00}$  E&M energy-momentum tensor 00 component replacement for the  $G_{00}$  Einstein tensor 00 component. The energy is associated with the Coulomb force here, not the gravitational force. The dyadic radial coordinate transformation of  $Z_{ij}$  associated with the expansion creates a new  $z_{00}$ . Thus transform the dyadic  $Z_{00}$  to the coordinate system commoving with the radial coordinate expansion and get  $Z_{00} \rightarrow Z_{00} + z_{00}$  (section 3.1). The new  $z_{00}$  turns out to be the gravitational source with the  $G$  in it. The mass is that of the electron so we can then calculate the value of the gravitational constant  $G$ . From Ch.1

the object  $dr$  as seen in the observer primed nonmoving frame is:  $dr = \sqrt{\kappa_\pi} dr' =$

$\sqrt{(1/(1+2\varepsilon))} dr' = dr'/(1+\varepsilon)$ .  $1/\sqrt{(1+.06)} = 1.0654$ . Also using  $S_{1/2}$  state of equation 16

$\varepsilon = .06006 = m_\mu + m_e$

From equation 11.4 and  $e^{i\omega t}$  oscillation in equation 11.4.  $\omega = 2c/\lambda$  so that one half of  $\lambda$  equals the actual Compton wavelength in the exponent of section 4.11. Divide the Compton wavelength  $2\pi r_M$  by  $2\pi$  to get the radius  $r_M$  so that  $r_M = \lambda_M/(2(2\pi)) = h/(2m_e c 2\pi) = 6.626 \times 10^{-34}/(9.1094 \times 10^{-31} \times 2.9979 \times 10^8 \times 4\pi) = 1.9308 \times 10^{-13}$

From the previous chapter the Heisenberg equations of motion give  $e^{i\omega t}$  oscillation (zitterbewegung) both for velocity and position so we use the classical harmonic oscillator probability distribution of radial center of mass of the zitterbewegung cosine oscillation lobe. So the COM (radial) is:  $x_{cm} = (\sum x_m)/M = \iiint r^3 \cos r \sin \theta d\theta d\phi dr / (\iiint r^2 \cos r \sin \theta d\theta d\phi dr) = 1.036$ . As a fraction of half a wavelength (so  $\pi$  phase)  $r_m$  we have  $1.036/\pi = 1/3.0334$  (7.4.1)

Take  $H_t = 13.74 \times 10^9 \text{ years} = 1/2.306 \times 10^{-18} \text{ s}$ . Consistent with the old definition of the 0-0 component of the old gravity energy momentum tensor  $G_{00}$  we define our single  $S_{1/2}$  state particle (E&M) energy momentum tensor 0-0 component From eq.3.1  $Z_{00}$  we have:  $c^2 Z_{00}/8\pi \equiv \varepsilon = 0.06$ ,  $\varepsilon = 1/2 \sqrt{\alpha}$  = square root of charge.

$$Z_{00}/8\pi \equiv e^2/2(1+\varepsilon)m_p c^2 = 8.9875 \times 10^9 (1.6 \times 10^{-19})^2 / (2c^2(1+\varepsilon)1.6726 \times 10^{-27}) = 0.065048/c^2$$

Also from equation 16 the ambient metric expansion component  $\Delta r$  is:

$$\text{eq.1.12 } \Delta r = r_A(e^{\omega t} - 1) \quad (7.4.2)$$

To find the physical effects of the equation 11.4 expansion *we must* do a dyadic radial coordinate transformation (equation 7.4.3) on this single charge horizon (given numerical value of the Hubble constant  $H_t = 13.74 \text{ bLY}$  in determining its rate) in eq.4.2. In doing the time derivatives we take the  $\omega$  as a constant in the linear  $t$  limit:

$$\frac{\partial x^\alpha}{\partial x'^\mu} \frac{\partial x^\beta}{\partial x'^\nu} Z_{\alpha\beta} = Z'_{\mu\nu} \text{ with in particular } Z_{00} \rightarrow Z'_{00} \equiv Z_{00} + z_{00} \quad (7.4.3)$$

After doing this  $Z'_{00}$  calculation the resulting (small)  $z_{00}$  is set equal to the Einstein tensor gravity source ansatz  $G_{00} = 8\pi G m_e/c^2$  for this *single* charge source  $m_e$  allowing us to solve for the value of the Newtonian gravitational constant  $G$  here as well. We have then derived gravity for **all** mass since this single charged  $m_e$  electron vacuum source composes all mass on this deepest level as we noted in the section 4.2 discussion of the equivalence principle. Note Lorentz transformation

similarities in section 2.3 between  $r = r_0 + \Delta r$  and  $ct = ct_0 + c\Delta t$  using  $D\sqrt{1 - \frac{v^2}{c^2}} \approx D(1 - \Delta)$  for  $v \ll c$

with just a sign difference (in  $1 - \Delta$ , + for time) between the time interval and displacement  $D$  interval transformations. Also the  $t$  in equation 10.2 and therefore 12.3 is for a light cone coordinate system (we are traveling near the speed of light relative to  $t=0$  point of origin) so  $c^2 dt^2 = dr^2$  and so equation 11.4 does double duty as a  $r = ct$  time  $x_0'$  coordinate. Also note we are trying to find  $G_{00}$  (our ansatz) and we have a large  $Z_{00}$ . Also with  $Z_{rr} \ll Z_{00}$  we needn't incorporate  $Z_{rr}$ . Note from the derivative of  $e^{\omega t} - 1$  (from equation 11.4) we have slope  $= (e^{\omega t} - 1)/H_t = \omega e^{\omega t}$ . Also from equation 2AB we have  $\delta(r) = \delta(r_0(e^{\omega t} - 1)) = (1/(e^{\omega t} - 1))\delta(r_0)$ . Plugging values of equation 7.4.1 2 and 7.4.2 and the resulting equation 4.7.1 into equation 7.4.3 we have in  $S_{1/2}$  state in equation 4.3:

$$\frac{8\pi e^2}{2(1+\varepsilon)m_p c^2} \delta(r) = Z_{00} = R_{00} - \frac{1}{2} g_{00} R, \quad \frac{\partial x^0}{\partial x'^0} \frac{\partial x^0}{\partial x'^0} Z_{\alpha\beta} = Z'_{00} = Z_{00} + z_{00} \approx \quad (7.4.4)$$

$$\frac{\partial x^0}{\partial [x^0 - \Delta r]} \frac{\partial x^0}{\partial [x^0 - \Delta r]} Z_{00} = \frac{\frac{\partial x^0}{\partial [x^0 - \frac{r_m}{3.03(1+\varepsilon)}[e^{\omega t} - 1]]}}{\frac{\partial x^0}{\partial [x^0 - \frac{r_m}{3.03(1+\varepsilon)}[e^{\omega t} - 1]]}} Z_{00} = Z'_{00}$$

$$\left[ \frac{1}{1 - \frac{r_m \omega}{3.03c(1+\varepsilon)} e^{\omega t}} \right]^2 \frac{8\pi e^2}{2(1+\varepsilon)m_p c^2} \delta(r) = \left( \frac{8\pi e^2}{2(1+\varepsilon)m_p c^2} \delta(r) + 8\pi G \left( \frac{m_e}{c^2} \right) \delta(r) \right)$$

(Recall 3.03 value from eq.7.4.1.). So setting the perturbation  $z_{00}$  element equal to the ansatz and solving for  $G$ :

$$2 \left( \frac{e^2}{2(1+\varepsilon)m_p} \right) \left( \frac{r_M}{3.03m_e c(1+\varepsilon)} \right) \omega e^{\omega t} =$$

$$\begin{aligned} & \left( 2 \left( \frac{e^2}{2(1+\varepsilon)m_p} \right) \left( \frac{r_M}{3.03m_e c(1+\varepsilon)} \right) \left( \frac{e^{\omega t} - 1}{H_t} \right) \right) \delta(r) = \\ & = 2 \left( \frac{e^2}{2(1+\varepsilon)m_p} \right) \left( \frac{r_M}{cm_e 3.03(1+\varepsilon)} \right) \left( \frac{[e^{\omega t} - 1]\delta(r_0)}{[e^{\omega t} - 1]H_t} \right) = G\delta(r_0) \end{aligned}$$

Make the cancellations and get:

$$2(.065048)[(1.9308 \times 10^{-13} / (3 \times 10^8 \times 9.11 \times 10^{-31} \times 3.0334(1+.0654)))] (2.306 \times 10^{-18}) = \\ = 2(.065048)(2.2 \times 10^8)(2.306 \times 10^{-18}) = \mathbf{6.674 \times 10^{-11} \text{ Nm}^2/\text{kg}^2 \equiv G} \quad (7.4.5)$$

from plugging in all the quantities in equation 7.4.5. This new  $z_{oo}$  term is the classical  $8\pi G\rho/c^2 = G_{oo}$  source for the Einstein's equations and we have then **derived gravity** and incidentally also derived the value of the Newtonian gravitational constant since from our postulate the  $m_e$  mass (our "single" postulated source) is the *only* contribution to the  $Z_{oo}$  term. Note Dirac equation implies +E and -E solutions for -e and +e respectively and so in equation 7.4.5 we have  $e^2 = ee = q_1 X q_2$  in eq.7.4.5. So when G is put into the Force law  $Gm_1 m_2 / r^2$  there is an *additional*  $m_1 X m_2$  thus the resultant force is proportional to  $Gm_1 m_2 = (q_1 X q_2) m_1 m_2$  which is always positive since the paired negatives always are positive and so the gravitational force is always attractive.

Also recall in the free falling frame (So comoving with  $M = m_e$  so is constant) fractal scale for  $ke^2 / ((GM')M) = 10^{40}$  fractal jump,  $ke^2 / (m_e c^2) = ke^2 / (Mc^2)$  is also constant so if G is going up (in 7.4.4) then  $M'$  is going down. Note then  $r_H = ke^2 / (m_e c^2) \rightarrow 10^{40} X r_H = r_H(N+1) = GM'm_e / (m_e c^2) = GM' / c^2 =$  famous Schwarzschild radius.

To summarize we have then just done a coordinate transformation to the moving frame to find the contributing fields associated with the moving frame. Analogously one does a coordinate transformation to the charge comoving frame to show that current carrying wires have a magnetic field, also a 'new' force, around them. Also note that in the second derivative of eq.7.1.2  $d^2 \mathbf{r} / dt^2 = \mathbf{r}_o \omega^2 e^{\omega t} =$  **radial acceleration**. Thus in equations 7.1.4 and 7.1.5 (originating in section 4) **we have a simple account of the cosmological radial acceleration expansion** (discovered recently) **so we don't need any theoretical constructs such as 'dark energy' to account for it.**

If  $r_o$  is the radius of the universe then  $r_o \omega^2 e^{\omega t} \approx 10^{-10} \text{ m/sec}^2 = a_M$  is the acceleration of all objects around us relative to a inertial reference frame and comprises a accelerating frame of reference. If we make it an inertial frame by adding gravitational perturbation we still have this accelerating expansion and so on. Thus in gravitational perturbations  $na_M = a$  where n is an integer.

Note below equation 7.4.5 above that  $t = 13.8 \times 10^9$  years and use the standard method to translate this time into a Hubble constant. Thus in the standard method this time translates into light years which are  $13.8 \times 10^9 / 3.26 = 4.264 \times 10^9$  parsecs =  $4.264 \times 10^3$  megaparsecs assuming speed c the whole time. So  $3 \times 10^5 \text{ km/sec} / 4.264 \times 10^3 \text{ megaparsecs} = \mathbf{70.3 \text{ km/sec/megaparsec}}$  = Hubble's constant for this theory.

**Big Picture N=1 Fractal scale  $m_p / |m_p| =$  baryon number**

$$(7.4.4) \quad \left[ \frac{1}{\left[ 1 - \frac{r_m \omega}{3.03c(1+\varepsilon)} e^{\omega t} \right]} \right]^2 \frac{8\pi e^2}{2(1+\varepsilon)m_p c^2} \delta(r) = \left( \frac{8\pi e^2}{2(1+\varepsilon)m_p c^2} \delta(r) + 8\pi G \left( \frac{m_e}{c^2} \right) \delta(r) \right)$$



Recall from above that:

$$= 2 \left( \frac{e^2}{2(1+\varepsilon)m_p} \right) \left( \frac{r_M}{c3.03(1+\varepsilon)} \right) \left( \frac{[e^{\omega t}-1]\delta(r_0)}{[e^{\omega t}-1]H_t} \right) = Gm_e\delta(r_0) \quad (7.4.5)$$

Also  $r_M = \lambda_M / (2(2\pi)) = h / (2m_e c 2\pi)$ .

But for  $N=-1$  from sect.2.2 and appendix C  $CM/m = r_H = ke^2 10^{40N} / m = Gm_e^2$ .

So  $Gm_e$  is not a constant so  $\mu = m_\mu = \varepsilon$  (in 7.4.4) is not a constant in

$\ln(r_{M+1}/r_{bb}) + 2 = [1/(e^\mu - 1) - \ln[e^\mu - 1]]/2$  showing it is selfconsistent with eq.7.4.4.

Also in eq.7.4.5  $2m_p = \xi_1$  from  $CM/\gamma \equiv CM/\xi_1 = CM/(2m_p) =$  negative or positive small C limit depending on the frame of reference of the boost  $\gamma$  (sect.2.2). Add to this frame of reference the next larger fractal scale  $N=1$  motion. This  $m_p$  coefficient in 7.4.5 thereby implies mathematically a  $m_p/|m_p|$  sign that is equivalent to the effect of the sign on the above  $\partial x^0 / \partial x'^0$  expansion term (in eq. 7.4.5) which itself is relative to object B inertial frame dragging radial motion. Thus  $m_p/|m_p|$  is either  $m_p/|m_p| = -1$  or  $m_p/|m_p| = +1$  baryon number making  $G$  either negative or positive in eq. 7.4.5 for  $r > r_H$  cosmological relative to that exterior radially moving (boosted) frame of reference. Thus  $(+e + e - e)/|e| = m_p/|m_p| =$  baryon number  $+1$  determines the sign of  $G$  in the next higher fractal scale relative to an exterior Newpde object B radial relative motion. So a universe full of antiprotons might have a  $+G$  on the  $N$ th fractal scale for  $r > r_H$  in eq.7.4.5 (relative to an object B positive sign) or a negative  $m_p/|m_p|$  baryon number  $-G$  and repulsion relative to object B. Thus we recreate the idea of charge and the electric field on the next larger ( $N=1, \sim 10^{14}ly$ ) huge fractal scale with the net sign of  $m_p/|m_p|$  baryon number of the constituents of our own  $N=0$  fractal scale.

So the electric field on the next higher fractal scale is what we see as the gravity field on our much smaller fractal scale: thus the gravity and electric fields are one and the same field seen from different (fractal) frames of reference. Thus we have a unified field theory here.

## 7.5 Metric Quantized Hubble Constant

Metric quantization 4.2.3 means (change in speed)/distance is quantized. Given 6billion year object B vibrational metric quantization the radius curve

$\ln(r_{M+1}/r_{bb}) + 2 = [1/(e^\mu - 1) - \ln[e^\mu - 1]]/2$  is not smooth but comes in jumps.

I looked at the metric quantization for the 2.5My metric quantization jump interval using those 3 Hubble "constants" 67, 70, 73.3 km/sec/megaparsec.

Recall that for megaparsec is  $3.26 \text{Megalightyear} = (2.5/.821) \text{Megalightyear}$ .

**But 2.5 million years is the time between one of those metric quantization jumps.**

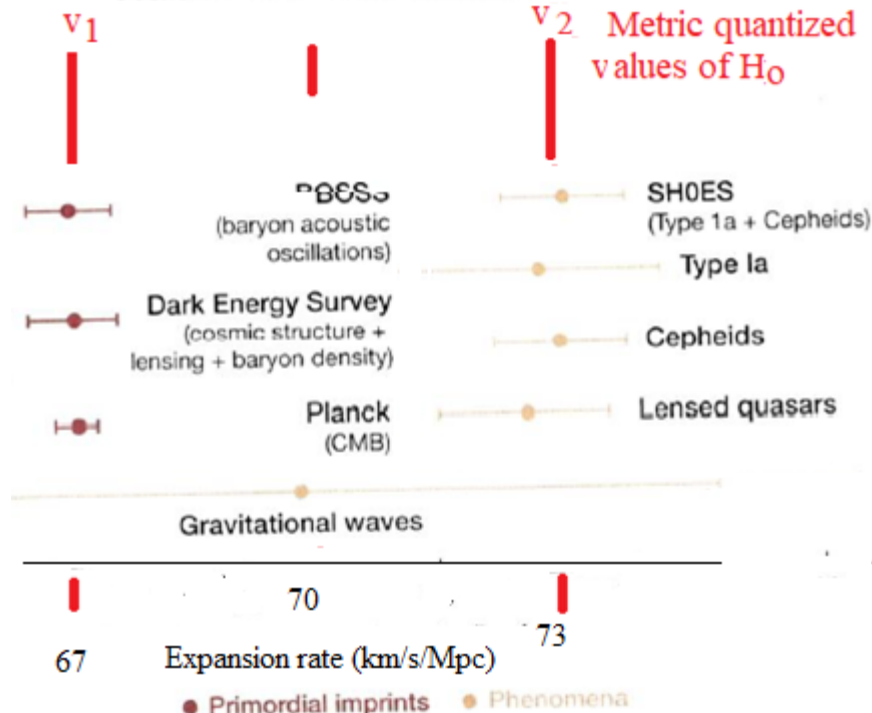
So instead of the 3 detected Hubble constants 67km/sec/megaparsec and 70km/sec/megaparsec and 73.3km/sec/megaparsec we have

81.6km/sec/2.5megaly, 85.26km/sec/2.5megaly, 89.3km/sec/2.5megaly. the difference between the contemporary one, the last and the two others then is

89.3km/sec/2.5megaly - 85.26km/sec/2.5megaly, = **4km/sec/2.5megaly**

and 89.3km/sec/2.5megaly - 89.3km/sec/2.5megaly = **8km/sec/2.5megaly**.

So the Hubble constant, with reference to the 2.5my metric quantization jump time, appears quantized in units of **4km/sec,8km/sec**, etc. Other larger denominator „averages“ are not



accurate. **Hubble Constant Measurements**

## 7.6 Cosmological Constant In This Formulation

In equation 4.6  $r_H/r$  term is small for  $r \gg r_H$  (far away from one of these particles) and so is nearly flat space since  $\epsilon$  and  $\Delta\epsilon$  are small and nearly constant. Thus equation 6.4.5 can be redone in the form of a Robertson Walker homogenous and isotropic space time. Given (from Sean Carroll) the approximation of a (homogenous and isotropic) Robertson Walker form of the metric we find that:

$$\frac{a''}{a} = -\frac{4\pi G}{3}(\rho + 3p) + \frac{\Lambda}{3}$$

$\Lambda$ =cosmological constant,  $p$ =pressure,  $\rho$ =density,  $a = 1/(1+z)$  where  $z$  is the red shift and 'a' the scale factor.  $G$  the Newtonian gravitational constant and  $a''$  the second time derivative here using cdt in the derivative numerator. We take pressure= $p=0$  since there is no thermodynamic pressure on the matter in this model; the matter is commoving with the expanding inertial frame to get the  $a''$  contribution. The usual 10 times one proton per meter cubed density contribution for  $\rho$  gives it a contribution to the cosmological constant of  $4.7 \times 10^{-36}/s^2$ .

Since from equation 7.6.1  $a = a_0(e^{\omega t} - 1)$  then  $a'' = (\omega^2/c^2) \sinh \omega t = a(\Lambda/3) = (\Lambda/3) \sinh \omega t$  and there results:

$$\Lambda = 3(\omega^2/c^2)$$

From section 7.4 above then  $\omega = 1.99 \times 10^{-18}$  with 1 year =  $3.15576 \times 10^7$  seconds, also  $c = 3 \times 10^8$  m/s. So:

$$\Lambda = 3(\omega^2/c^2) = 1.32 \times 10^{-52} /m^2, \text{ which is our calculated value of the cosmological constant.}$$

Alternatively we could use  $1/s^2$  units and so multiply this result by  $c^2$  to obtain:

$1.19 \times 10^{-35}/s^2$ . Add to that the above matter (i.e.,  $\rho$ ) contributions to get  $\Lambda = 1.658 \times 10^{-35}/s^2$  contribution.

## 7.7

Note that we have thereby derived the Newtonian gravitational constant  $G$  by using a radial coordinate transformation of the  $T_{00} = e^2 \delta(0)$  charge density component to the coordinate system commoving with the expansion of the  $N+1$  th fractal scale (cosmological).

Note that our new force we derived was charge and mass independent but the old force was charge dependent. Also note that the new force metric has universal geodesics that even curve space for photons. The old one had a  $q$  in the  $k_{ij}$  (chap.17). If  $q=0$  as with the photon there would be no effect on the trajectory of the photon whereas the same photon moving near a gravitational source would be deflected. Recall again this is all caused by the taking of the derivative in the above coordinate transformation.

So as a result of this coordinate transformation photons are deflected by the  $N+1$  fractal scale metric and area not deflected by the  $N$ th scale metric.

Also the GM does not change in the commoving coordinates for the same reason as the speed of light does not change as you enter a black hole, your watch slows down because of GR to compensate.

## References

Merzbacher, *Quantum Mechanics*, 2<sup>nd</sup> Ed, Wiley, pp.597

## 7.8 Comoving Interior Frame

Recall from solution 2 (section 1.2) that the new pde zitterbewegung  $E = 1/\sqrt{\kappa_{00}}$  energy smudged out  $r = \langle r_0 e^{i\omega t} \rangle$  with  $\omega \rightarrow i\omega$  inside  $r_H$ . so  $m = \sinh \omega t$ . Do a coordinate transformation (Laplace Beltrami) to the coordinate system of the  $r > r_H$  commoving observer (us) and that equation pops right out.

### The Origin of that Mercuron.

My new pde uses a source term  $\kappa_{00}$  in the external inertial reference frame. In contrast for the comoving term the field itself can be the origin of the field, especially near the time of the big bang so I must transform to the comoving coordinate system to derive the fields the comoving observer measures.

In that context in the commoving De Sitter metric reference frame inside  $r_H$  we are not in free space anymore with instead the source term as the multiple of the Laplacian of the metric tensor in harmonic local coordinates (recall the Dirac eq.) whose components satisfy Ricci tensor  $= R_{ij} = -(1/2)\Delta(g_{ij})$  where  $\Delta$  is the Laplace-Beltrami second derivative operator is not zero.

Geometrically, the Ricci curvature is the mathematical object that controls the growth rate of the volume of metric balls in a manifold. Note also the second derivative (Laplacian) of  $\sin \omega t$  is  $-\omega^2 \sin \omega t$ . Also recall that inside  $r_H$  so that  $r < r_H$ , then  $\sin \omega t \rightarrow \sinh \omega t$ , which is rewritten as  $\sinh \mu$  to match with  $R_{22} = e^{-\nu} [1 + \frac{1}{2} r(\mu' - \nu')]$  with  $\mu = \nu$  (spherical symmetry). So the de Sitter metric submanifold is itself the source of this  $R_{22}$  which is a nontrivial effect in the very early, extremely high density, universe.

I solved this  $R_{22}$  equation and got  $\ln(r_{M+1}/r_{bb}) + 2 = [1/(e^\mu - 1) - \ln[e^\mu - 1]]/2$

That Mandelbrot set Lepton analysis (appendix C) implies that  $u$  is the muon contribution (as a fraction of the tauon mass). Set  $r_{M+1} = 10^{11} \text{ LY}$  and get  $r_{bb}$  (radius of Big Bang) of about 30 million miles, approximately the size of Mercury's orbit (hence the "Mercuron"), a large enough volume to just pack together those  $10^{82}$  electrons (With 3 each a proton) at  $r = r_H$  separation.

Note the above equation shows the muon mass  $\mu$  is getting smaller with time. It started out at  $\mu=1$  and is now at  $\mu=.06$ . CODATA=1.883531627X10<sup>-28</sup> [42] or a uncertainty of 5 parts in 10<sup>9</sup>. Muon mass is changing with 1 part in 10<sup>11</sup> per year in the above formula but per decade it is 1 part in 10<sup>10</sup>

close to what is measurable. Since  $ge/2m$  =gyromagnetic ratio so mass  $m$  is in the denominator the gyromagnetic ratio would also change with time so perhaps the mass change with time can be found by measuring that gyromagnetic ratio changes with time.

Given these protons we *do not require protogenesis* and we also have an *equal number of particles and antiparticles*(proton  $2e^+, e^-$ ; extra  $e^-$ ). The rotation gives us *CP violation* since  $t$  invariance is broken in the Kerr metric. This formula predicts an age of 370by *explaining these early supermassive black holes* (they had plenty of time to accrete) and the thermodynamic equilibrium required to create the *black body CBR*: all these modern cosmological conundrums are solved here

Recall we start out in the new pde external frame of reference that observes the Schwarzschild metric with perturbative rotation. Furthermore at  $r=r_H$  the Schwarzschild metric appears to the comoving observer as a De Sitter universe. But in the commoving De Sitter metric reference frame inside  $r_H$  we are not in free space anymore so the multiple of the Laplacian of the metric tensor in harmonic local coordinates whose components satisfy  $R_{ij} = -(1/2)\Delta(g_{ij})$  where  $\Delta$  is the Laplace-Beltrami second derivative operator is not zero. Geometrically, the Ricci curvature is the mathematical object that controls the growth rate of the volume of metric balls in a manifold. Note the second derivative (Laplacian) of  $\sin\omega t$  is  $-\omega^2 \sin\omega t$ . Also recall that inside  $r_H$  so that  $r < r_H$ , then  $\sin\omega t \rightarrow \sinh\omega t$ , which is rewritten as  $\sinh\mu$  to match with  $R_{22} = e^{-\lambda} [1 + \frac{1}{2} r(\mu' - v')]$  with  $\mu = v$  (spherical symmetry) and  $\mu' = -v'$ . So the de Sitter metric submanifold is itself the source of this  $R_{22}$  which is a nontrivial effect in the very early, extremely high density, universe. (Note that the contemporary G calculation in Ch.12 just uses the de Sitter  $\sinh\mu$  (just as in Ch.12 coordinate transformation because this feedback effect no longer is dominant in this era). So the usual spherically symmetric:

$R_{22} = e^{-\lambda} [1 + \frac{1}{2} r(\mu' - v')]$  -1=0  $\rightarrow$  de Sitter metric  $\cosh\mu=1$ , itself is the source, comoving coordinate  $R_{22} = e^{-\lambda} [1 + \frac{1}{2} r(\mu' - v')]$  -1=-sinh $\mu$  (A)

Use metric a ansatz:  $ds^2 = -e^v (dr)^2 - r^2 d\theta^2 - r^2 \sin^2\theta d\phi^2 + e^\mu dt^2$  so that  $g_{00} = e^\mu$ ,  $g_{rr} = e^v$ . From  $R_{ij} = 0$  for spherical symmetry in free space

$$R_{11} = \frac{1}{2}\mu'' - \frac{1}{4}v'\mu' + \frac{1}{4}(\mu')^2 - v'/r = 0 \quad (6.4.7)$$

$$R_{22} = e^{-v} [1 + \frac{1}{2} r(\mu' - v')] - 1 = 0 \quad (6.4.8)$$

$$R_{33} = \sin^2\theta \{ e^{-v} [1 + \frac{1}{2} r(\mu' - v')] - 1 \} = 0 \quad (6.4.9)$$

$$R_{00} = e^{\mu-\lambda} [-\frac{1}{2}\mu'' + \frac{1}{4}v'\mu' - \frac{1}{4}(\mu')^2 - \mu'/r] = 0 \quad (6.4.10)$$

$$R_{ij} = 0 \text{ if } i \neq j$$

(eq. 6.4.7 -6.4.10 from pp.303 Sokolnikof): Equation 6.4.9 is a mere repetition of equation 6.4.8.

We thus have only three equations on  $v$  and  $\mu$  to consider. From equations 6.4.7; 6.4.10 we deduce that  $v' = -\mu'$ . Here we consider the possibility of a large ambient metric  $C$   $\mu = v + C$  and **fractal selfsimilar comoving frame with Laplace-Beltrami -sinhu rotation (Kerr perturbation)  $R_{22}$  source** as observed internally to  $r_H$ .

$R_{22} = e^{-v} [1 + \frac{1}{2} r(\mu' - v')] - 1 = -\sinh v = -(e^v - e^{-v})/2$ ,  $v' = -\mu'$  so

$e^{-\mu} [-r(\mu')] = -\sinh\mu - e^{-\mu} + 1 = -(-e^{-\mu} + e^\mu)/2 - e^{-\mu} + 1 = -(e^{-\mu} + e^\mu)/2 + 1 = -\cosh\mu + 1$ . So given  $v' = -\mu'$

$e^{-\nu}[-r(\mu')] = 1 - \cosh \mu$ . Thus

$e^{-\mu} r(d\mu/dr) = 1 - \cosh \mu$

This can be rewritten as:

$$e^{\mu} d\mu / (1 - \cosh \mu) = dr/r \quad (B)$$

The integration is from  $\xi_1 = \mu = \varepsilon = 1$  to the present day mass of the muon = .06 (X tauon mass).

Integrating equation B from  $\varepsilon = 1$  to the present  $\varepsilon$  value we then get:

$$\ln(r_{M+1}/r_{bb}) + 2 = [1/(e^{\mu} - 1) - \ln[e^{\mu} - 1]]^2 \quad (7.8.1)$$

the equation that gives the comoving observer time evolution of the universe. The equation works near the min of the sinusoidal oscillation where we are slightly inside  $r_H$ .

### Summary

The rebound time is 350by = very large  $\gg 14$ by solving the horizon problem since temperatures could (nearly) come to equilibrium during that time (From recent Hubble survey: "The galaxies look remarkably mature, which is not predicted by galaxy formation models to be the case that early on in the history of the universe." "lots of dust already in the early universe", "CBR is the result of thermodynamic equilibrium" requiring slow expansion then, etc.).

### Also Spherical Bessel Function Oscillation Nodes Inside Mercuron

Given  $\mu$  is the muon mass 7.4.4 in equation 7.8.1 the smallest radius of this oscillation period is about the radius of that Mercuron). Because of object B rotational energy 51 radial oscillation (270My into 14BY) nodes also exist in the Mercuron creating  $(4\pi/3)(51)^3 = 5.5 \times 10^5$  (gravitational wave spherical Bessel function nodes with Mercuron surface boundary conditions creating the) voids we see today. Note these voids thereby have reduced G in them and are local higher rates of metric  $g_{ij}$  expansion regions. GM is invariant. The Sachs Wolfe effect then creates the resulting CBR inhomogeneities.

### Fortran Program for Eq.7.8.1

```

program FeedBack
  DOUBLE PRECISION e,ex,expp,rM1,rd,rb,rbb,uu,u11,den,eu1,u
  DOUBLE PRECISION NN,enddd,bb,ee,rmorbb,Ne,rr
  INTEGER N,endd
  open(unit=10,file='FeedBack_m',status='unknown')
  !FeedbackEquation
  !e^udu/(1-coshu)=dr/r
  !ln(rM+1/rbb)+2=[1/(e^u-1)-ln[e^u-1]]^2
  e=2.718281828
  u11=.06
  endd=100
  enddd=endd*1.0
  uu=.06/enddd
  Ne=1000.0
  Do 1000 N=100,1000
  Ne=Ne-1.0
  rr=n/100.0
  rbb=30.0*(10.0**6)*1600.0
  rbb=1.0
  ! rd=2.65*(10**13)
  u=Ne*uu
  eu1=(e**u)-1.0
  ex=(2.0/eu1)-(2.0*LOG(eu1))-2.0
  expp=(ex)
  rM1=(e**expp)*rbb !ln logarithitnm
  rM1=e**ex
  !rMorbb
  !bb=log(ee)
  if (ex.GT.36.0)THEN
  goto 2001
  endif
  write(10,2000) rr,rM1
1000 CONTINUE

```

```

2000 format(f7.2,1x,1x,1x,f60.6)
2001 end

```

$\text{Sin}(1-u)=r$  gives the same functionality as the above program does for  $\mu \approx 1$  the  $\sin(1-\mu)$  And the sine:  $\sin(1-\mu) \approx \sinh(1-\mu)$ . For larger  $1-\mu$  we must use  $1-\mu \rightarrow i(1-\mu)$  given sect 5.2 harmonic coordinates from the new pde in the sine wave bottom.

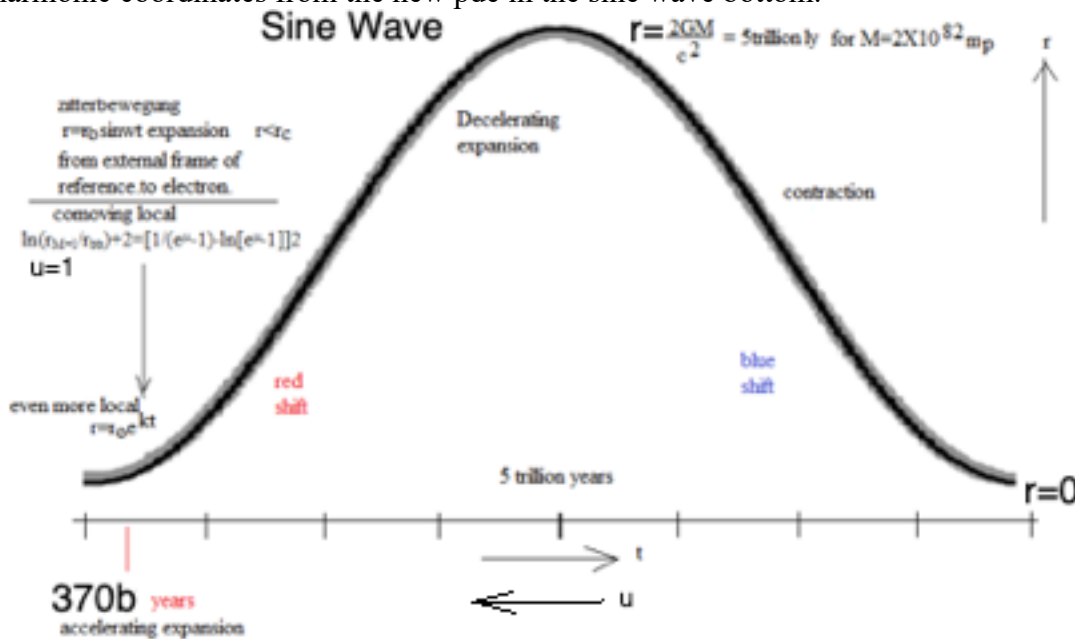


fig.10

## Sine Wave

The 10 trillion years represents the period of object A we are inside.

### Average Acceleration

If we assumed a *linear expansion* at constant acceleration 'a' up to 2X our (linear) time  $\approx 2X10^{11}y=2t=2X10^{11}X365.25X24X3600=2(3X10^{18})\text{sec}$  we can then use  $v=at$ . (but our actual  $a=e^{ikt}$  is not linear). From above graph we are also about halfway to the straightline slope c (We cannot use  $v=c$  anyway here because  $v=at$  is a nonrelativistic relation.). So since we assumed a linear expansion we can use  $a=v/t=(3X10^8/2)/(2X10^{11}/2)=3X10^8/3X10^{18}=10^{-10}\text{m/s}^2=1\text{A/s}^2=\text{MOND}$  which is approximately what is seen today . $d=(1/2)at^2$  gives the universe sized d.

### 7.10 Construct The Standard Model Lagrangian

Note we have derived from first principles (i.e., from postulate 1) the new pde equation for the electron (eq.7 eq.16, pde for the neutrino (eq.8) Maxwell's equations for the photon, the Proca equation for the Z and the W (Ch.3) and the found the mass for the Z and the W (4.2.1). We even found the Fermi 4 point from the object C perturbations. The distance to object B determines mass and we found that it is equivalent to a scalar field (Higgs) source of mass in sect.4.1.5. We have no gluons or quarks or color in this model but we can at least derive the phenomenology these concepts predict with oureq  $16+16+16$  at  $r=r_H$  strong force model (ie.,  $16+16+16$   $r=r_H$ , Ch.9,10)

So from the postulate of 1 we can now construct the standard model Lagrangian, or at least predict the associated phenomenology, from all these results for the Nth fractal scale. Here it is:



|          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |
|----------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>1</b> | $-\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4} g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e + \frac{1}{2} i g_s^2 (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- -$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | $W_\mu^- \phi^+) - \frac{1}{2} i g^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2} g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) + \frac{1}{2} i g^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w^2}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- -$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |
| <b>2</b> | $M^2 W_\mu^+ W_\mu^- - \frac{1}{2} \partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2} \partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2} \partial_\mu H \partial_\mu H - \frac{1}{2} m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2} \partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2} M \phi^0 \phi^0 - \beta_h [\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2} (H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-)] + \frac{2M^4}{g^4} \alpha_h - i g c_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - i g s_w [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - \frac{1}{2} g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2} g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\mu^0 W_\nu^+ W_\nu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - 2 A_\mu Z_\mu^0 W_\nu^+ W_\nu^-] - g \alpha [H^3 + H \phi^0 \phi^0 + 2 H \phi^+ \phi^-] - \frac{1}{8} g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4 H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2] - g M W_\mu^+ W_\mu^- H - \frac{1}{2} g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \frac{1}{2} i g [W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)] + \frac{1}{2} g [W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)] + \frac{1}{2} g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - i g \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + i g s_w M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - i g \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + i g s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4} g^2 W_\mu^+ W_\mu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 \frac{1}{c_w} Z_\mu^0 Z_\mu^0 [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2} g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- +$ | $W_\mu^- \phi^+) - \frac{1}{2} i g^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2} g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) + \frac{1}{2} i g^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w^2}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - g^1 s_w^2 A_\mu A_\mu \phi^+ \phi^- - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda \gamma \partial \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + m_u^\lambda) u_j^\lambda - d_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + i g s_w A_\mu [-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3} (\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3} (\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)] + \frac{i g}{4c_w} Z_\mu^0 [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - 1 - \gamma^5) u_j^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 - \gamma^5) d_j^\lambda)] + \frac{i g}{2\sqrt{2}} W_\mu^+ [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)] + \frac{i g}{2\sqrt{2}} W_\mu^- [(\bar{e}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\lambda\kappa}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda)] + \frac{i g}{2\sqrt{2}} \frac{m_\lambda^2}{M} [-\phi^+ (\bar{\nu}^\lambda (1 - \gamma^5) e^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) \nu^\lambda)] -$ |
| <b>3</b> | $M^2 W_\mu^+ W_\mu^- - \frac{1}{2} \partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2} \partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2} \partial_\mu H \partial_\mu H - \frac{1}{2} m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2} \partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2} M \phi^0 \phi^0 - \beta_h [\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2} (H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-)] + \frac{2M^4}{g^4} \alpha_h - i g c_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - i g s_w [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - \frac{1}{2} g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2} g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\mu^0 W_\nu^+ W_\nu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - 2 A_\mu Z_\mu^0 W_\nu^+ W_\nu^-] - g \alpha [H^3 + H \phi^0 \phi^0 + 2 H \phi^+ \phi^-] - \frac{1}{8} g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4 H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2] - g M W_\mu^+ W_\mu^- H - \frac{1}{2} g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \frac{1}{2} i g [W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)] + \frac{1}{2} g [W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)] + \frac{1}{2} g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - i g \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + i g s_w M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - i g \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + i g s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4} g^2 W_\mu^+ W_\mu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 \frac{1}{c_w} Z_\mu^0 Z_\mu^0 [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2} g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- +$ | $W_\mu^- \phi^+) - \frac{1}{2} i g^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2} g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) + \frac{1}{2} i g^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w^2}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - g^1 s_w^2 A_\mu A_\mu \phi^+ \phi^- - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda \gamma \partial \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + m_u^\lambda) u_j^\lambda - d_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + i g s_w A_\mu [-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3} (\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3} (\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)] + \frac{i g}{4c_w} Z_\mu^0 [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - 1 - \gamma^5) u_j^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 - \gamma^5) d_j^\lambda)] + \frac{i g}{2\sqrt{2}} W_\mu^+ [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)] + \frac{i g}{2\sqrt{2}} W_\mu^- [(\bar{e}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\lambda\kappa}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda)] + \frac{i g}{2\sqrt{2}} \frac{m_\lambda^2}{M} [-\phi^+ (\bar{\nu}^\lambda (1 - \gamma^5) e^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) \nu^\lambda)] -$ |
| <b>4</b> | $M^2 W_\mu^+ W_\mu^- - \frac{1}{2} \partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2} \partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2} \partial_\mu H \partial_\mu H - \frac{1}{2} m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2} \partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2} M \phi^0 \phi^0 - \beta_h [\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2} (H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-)] + \frac{2M^4}{g^4} \alpha_h - i g c_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - i g s_w [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - \frac{1}{2} g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2} g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\mu^0 W_\nu^+ W_\nu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - 2 A_\mu Z_\mu^0 W_\nu^+ W_\nu^-] - g \alpha [H^3 + H \phi^0 \phi^0 + 2 H \phi^+ \phi^-] - \frac{1}{8} g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4 H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2] - g M W_\mu^+ W_\mu^- H - \frac{1}{2} g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \frac{1}{2} i g [W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)] + \frac{1}{2} g [W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)] + \frac{1}{2} g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - i g \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + i g s_w M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - i g \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + i g s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4} g^2 W_\mu^+ W_\mu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 \frac{1}{c_w} Z_\mu^0 Z_\mu^0 [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2} g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- +$ | $\frac{g}{2} \frac{m_\lambda^2}{M} [H (\bar{e}^\lambda e^\lambda) + i \phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda)] + \frac{i g}{2M\sqrt{2}} \phi^+ [-m_\lambda^2 (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + m_\lambda^2 (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa) + \frac{i g}{2M\sqrt{2}} \phi^- [m_\lambda^2 (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_\lambda^2 (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\kappa) - \frac{g}{2} \frac{m_\lambda^2}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_\lambda^2}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{i g}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{i g}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + X^+ (\partial^2 - M^2) X^+ + X^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 -$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |
| <b>5</b> | $M^2 W_\mu^+ W_\mu^- - \frac{1}{2} \partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2} \partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2} \partial_\mu H \partial_\mu H - \frac{1}{2} m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2} \partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2} M \phi^0 \phi^0 - \beta_h [\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2} (H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-)] + \frac{2M^4}{g^4} \alpha_h - i g c_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - i g s_w [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - \frac{1}{2} g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2} g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\mu^0 W_\nu^+ W_\nu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - 2 A_\mu Z_\mu^0 W_\nu^+ W_\nu^-] - g \alpha [H^3 + H \phi^0 \phi^0 + 2 H \phi^+ \phi^-] - \frac{1}{8} g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4 H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2] - g M W_\mu^+ W_\mu^- H - \frac{1}{2} g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \frac{1}{2} i g [W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)] + \frac{1}{2} g [W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)] + \frac{1}{2} g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - i g \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + i g s_w M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - i g \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + i g s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4} g^2 W_\mu^+ W_\mu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 \frac{1}{c_w} Z_\mu^0 Z_\mu^0 [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2} g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- +$ | $\frac{M^2}{2c_w} X^0 + \bar{Y} \partial^2 Y + i g c_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + i g s_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ Y) + i g c_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^0 X^+) + i g s_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + i g c_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^- - \partial_\mu \bar{X}^- X^+) + i g s_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) - \frac{1}{2} g M [\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w} \bar{X}^0 X^0 H] + \frac{1-2c_w^2}{2c_w} i g M [\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-] + \frac{1}{2c_w} i g M [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + i g M s_w [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \frac{1}{2} i g M [\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0]$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |

Fig. 10

The next fractal scale N+1 coming out of our eq.1 gives the cosmology and GR gravity, which is not included in the standard model. In fact the whole model repeats on the N+1 fractal scale. Object B provides ambient metric quantization states that have been observed implying new physics. So there is the promise of breakthrough physics from our new (postulate 1) model.

<sup>i</sup> Weinberg, Steve, *General Relativity and Cosmology*, P.257