

# A Generally Covariant Generalization of the Dirac equation that does not require gauges(Newpde)

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Abstract: In that regard Dirac in 1928 made his equation(1) flat space(2). But space is not in general flat, there are forces.

So over the past 100 years people have had to try to make up for that mistake by adding adhoc convoluted gauge force after gauge force until theoretical physics became a mass of confusion, a train wreck, a junk pile. So all they can do for ever and ever is to rearrange that junk pile with zero actual progress in fundamental theoretical physics being made,.. forever.

By the way note that Newpde(3)  $\gamma^\mu \sqrt{\kappa_{\mu\mu}} \partial\psi/\partial x_\mu = (\omega/c)\psi$  is NOT flat space (4) so it cures this problem(5).

## References

(1)  $\gamma^\mu \partial\psi/\partial x_\mu = (\omega/c)\psi$

(2) Spherical symmetry:  $(\gamma^x \sqrt{\kappa_{xx}} dx + \gamma^y \sqrt{\kappa_{yy}} dy + \gamma^z \sqrt{\kappa_{zz}} dz + \gamma^t \sqrt{\kappa_{tt}} dt)^2 = \kappa_{xx} dx^2 + \kappa_{yy} dy^2 + \kappa_{zz} dz^2 - \kappa_{tt} dt^2 = ds^2$   
 $\kappa_{xx} = \kappa_{yy} = \kappa_{zz} = \kappa_{tt} = 1$  is flat space, Minkowski, as in his Dirac equation(1).

(3) Newpde:  $\gamma^\mu \sqrt{\kappa_{\mu\mu}} \partial\psi/\partial x_\mu = (\omega/c)\psi$  for  $e, \nu$ . So we didn't just drop the  $\kappa_{\mu\nu}$

(4) Here  $\kappa_{oo} = 1 - r_H/r = 1/\kappa_{rr}$ ,  $r_H = (2e^2)(10^{40}N)/(mc^2)$ . The  $N = \dots -1, 0, 1, \dots$  applies to the Nth Fiegenbaum point self-similar fractal scale. Newpde from Occam's razor **optimized postulate 1**:  $z = zz$  is the algebraic definition of **1** and adding (small) constant C is trivial in  $z + C = zz$ ,  $\delta C = 0$  (1)

**A** Substitute  $z = 1 + \delta z$  into **equation 1** and get 2D Dirac equations for  $e, \nu$  (sect.1.1).

**B** Substitute left side z into right side zz repeatedly in **equation 1** and get the 2D Mandelbrot set **A, B** together gives 4D Newpde. So **Postulate 1**  $\rightarrow$  **Newpde**

(5) For  $N=0$  the third order Taylor expansion term of  $\sqrt{\kappa_{\nu\nu}}$  gives the Lamb shift and anomalous gyromagnetic ratio (without the renormalization and infinities(6))

For  $N=-1$  (i.e.,  $e^2 \times 10^{-40}$ )  $\kappa_{\mu\nu}$  is then the Schwarzschild metric  $g_{\mu\nu}$ ; so we just derived General Relativity and the gravity coupling *from* Quantum Mechanics(QM) in one line. So  $\kappa_{\mu\nu}$  even provides the general covariance of the Newpde. Eq 2a (ref.7) *even* provides us space-time  $r, t$

For  $N=1$  (so  $r < r_C$ ) Newpde zitterbewegung expansion stage explains the universe expansion.

For  $N=1$  zitterbewegung harmonic coordinates *and* Minkowski metric submanifold (after long time expansion) gets De Sitter ambient metric we observe astronomically(B1).

For  $N=0$   $r = r_H$  composite  $3e$  is the baryons and composite  $e, \nu$  is the Standard electroweak Model Bosons(append.A). We derived Quantum Mechanics (QM, Newpde) for *all* N fractal scales!(B3)

For  $N=1$  for example the QM large wavelength psi's provide the explanation for the **large stellar speeds**  $v$  in the halos (eg., Witten's 'fuzzy' theory). Just set  $\kappa_{oo} = g_{oo}$  in the halo, solve for constant  $v$

For  $N=1$  there is a ambient fractal self similar ( $S=1/2$ ) cosmological Kerr metric *Newpde* rotation so with off diagonal  $dt d\phi$  cross term T violation that **then causes** the (given CPT) **CP violation** and (the selfsimilar  $S=1/2$  spin axis) also puts a weak dipole on the cbr sky (thus the 'axis of evil')

For  $N=0$  (Eqs.2-5, ref.7)  $2D R_{oo} - (1/2)g_{oo}R = G_{oo} = +H_e + H_\nu$  giving  $\sigma * p = H_\nu$  a negative sign and so **left handed chirality** to  $\nu$  for maximally symmetric space (MS) time since then for 2D  $G_{oo} = 0$ . If not MS, as in a nonzero gravity gradient,  $H_\nu$  (**neutrino**) thereby **gains**  $G_{oo}$ , i.e., **mass**.

**References (continued)**

6) Need infinities if flat space Dirac equation. For flat space  $\partial g_{ik}/\partial x^j = \mathbf{0}$  as a limit. Then must take  $g^{km} = 1/0 = \infty$  to get finite Christoffel symbol  $\Gamma^m_{ij} \equiv (g^{km}/2)(\partial g_{ik}/\partial x^j + \partial g_{jk}/\partial x^i - \partial g_{ij}/\partial x^k)$   
 $= (1/0)(\mathbf{0}) = \text{undefined}$  but still implying *nonzero* acceleration on the left side of the geodesic

equation:  $\frac{d^2 x^\mu}{ds^2} = -\Gamma^\mu_{\nu\lambda} \frac{dx^\nu}{ds} \frac{dx^\lambda}{ds}$  So we need infinite fields for flat space. Thus QED requires (many such) infinities. But we have in general curved space  $g_{ij} = \kappa_{ij}$  in the New pde so do not require that anything be infinite and yet we still obtain for the third order Taylor expansion term of  $\sqrt{\kappa_{\mu\nu}}$  the Lamb shift and anomalous gyromagnetic ratio correction (sect.1.2).

7) Derivation of Newpde: **Physics of self similar fractal scales**

We can do this using the Occam's razor *optimized postulate 1*. For example  $z = zz$  is the algebraic definition of **1** and adding constant C is trivial in

$$z + C = zz, \delta C = 0 \tag{1}$$

**A Substitute**  $z = 1 + \delta z$  into **equation 1**, get  $\delta z + \delta z \delta z - C = 0$  (or  $\delta(\delta z + \delta z \delta z) = 0$ ) (2)

We assume C has a constant density. Solve eq.2 and in-general get  $\delta z = \frac{-1 \pm \sqrt{1+4C}}{2}$ ,

$C \ll -1/4$ , so **BIG-C** so big  $\delta z$  for (for random time t) complex solution  $\delta z = dr + idt$  (3)

Big  $\delta z$  so  $\delta z \ll \delta z \delta z$  (and  $\delta \delta z \approx 0$ ) in eq.2. So  $\delta(\delta z + \delta z \delta z) \approx \delta(\delta z \delta z) = (dr^2 - dt^2 + i(dr dt + dt dr)) = 0$  (4)

and take **real** Minkowski and **imaginary** component Clifford algebra which for negative and positive dr, dt imply *noninfinite* extremum  $dr dt + dt dr = 0 = \gamma^i dr \gamma^j dt + \gamma^j dt \gamma^i dr = (\gamma^i \gamma^j + \gamma^j \gamma^i) dr dt = 0$  (5)

Given that Clifford algebra we get, after factoring  $dr^2 - dt^2 = ds^2$ , 2D Dirac equations for e, v. ( $\delta z = \psi$ )

**B Substitute left side z into right side zz** repeatedly in **equation 1** and thereby get the **Mandelbrot set** iteration (with its well known  $10^{40N}$  X fractal selfsimilar  $N = \dots, -1, 0, 1, \dots$  scale jumps at Feigenbaum point  $C_M$  2D nonflat extremum  $\delta z'$ ). C is not uniform density here.

Notes: **Big -C case** allows random t and so Hamiltonians H (i.e., *physics*)

**Real eigenvalues of H** require the (**Mandelbrot set** subset) Cauchy sequence, sect.2.3.

Big  $\gamma$  (in  $(1/\gamma)\delta z$ ) boost means small  $C \approx \delta z \gg \delta z \delta z$  (so  $\delta(\delta z') = 0$ ) and so no more quadratic equation but we still keep our complex  $\delta z$  and so dt. Small C is  $z = zz$  **postulate 1**.

**A, B together** (and the  $\gamma$  boost) gives: **Newpde**  $\gamma^\mu \sqrt{\kappa_{\mu\nu}} \partial \psi / \partial x_\mu = (\omega/c) \psi$  for e, v

with  $\kappa_{00} = 1 - r_H/r = 1/\kappa_{rr}$ ,  $r_H = (2e^2)(10^{40N}) / (mc^2)$

Summary: **Postulate 1**  $\rightarrow$  **Newpde**

8) **ring of truth: Equation 1** bears a striking resemblance to the **Mandelbrot set** iteration formula and yet puts out as **imaginary & real** components the **Dirac** eqs. for e, v. They are connected! (also via Newpde). So we thereafter just do that big  $\gamma$  boost that gets small  $\delta z \approx C$  and so  $zz = z$  so **postulate 1** ( $\gamma$  boost also gets the numerical outputs of the Newpde such as that  $mc^2$ )

Note this is the first Occam's razor *optimized* (i.e., **postulate 1**) method of deriving theoretical physics (We figured it out! Appen.A8), not that  $\sim 100$  postulates, assumptions,  $> 23$  free parameters mess (So where do those many postulates come from?). Furthermore, this New pde Nth fractal scale approach is clearly the path to breakthrough physics and generates correct physical constants as we saw in reference 5.

## I Summary: Algebra Details of the two substitutions (A,B):

1.1 (Simply **postulate 1**. But  $z=zz$  is the algebraic definition of **1** and adding constant C (or K) is trivial in:  $zz=z+C, \delta C=0$  (1)

**A Substitute**  $z=1+\delta z$  into **eq.1**, get  $\delta z+\delta z\delta z=C$  (2) (or  $\delta(\delta z+\delta z\delta z)=0$ ) with in general (for  $\delta z=\frac{-1\pm\sqrt{1+4C}}{2}$ ,  $C\ll-1/4$ , so **Big-C** and so big  $\delta z$  for random time t complex solution  $\delta z=dr+idt$  (2a) Big  $\delta z$  so,  $\delta z\ll\delta z\delta z$ ,  $\delta\delta z=0$  So from eq.2,2a  $\delta((\delta z+\delta z\delta z)\approx\delta(\delta z\delta z)=(dr^2-dr^2+i(dr dt+dt dr))=0$  (2b) and take **real** Minkowski and **imaginary** component Clifford algebra which for negative and positive dr,dt the *noninfinite* extremum  $dr dt+dt dr=0=\gamma^i dr \gamma^j dt+\gamma^j dt \gamma^i dr=(\gamma^i \gamma^j+\gamma^j \gamma^i) dr dt=0$  (3) Factor  $dr^2-dt^2=ds^2$  eg.,  $\delta[(dr+dt)(dr-dt)]=0=[\delta(dr+dt)](dr-dt)+[(dr+dt)[\delta(dr-dt)]]$  and solve to get: (ds  $\equiv$  proper time invariant.)

$$(\rightarrow \pm e) \quad dr+dt=ds, \quad dr-dt=ds \equiv ds_1 \quad \text{for } +ds \rightarrow \text{ I, IV quadrants} \quad (4)$$

$$(\rightarrow \text{light cone } \nu) \quad dr+dt=ds, \quad dr=-dt, \quad \text{for } +ds \rightarrow \text{ II quadrant} \quad (5)$$

$$\text{“ “} \quad dr-dt=ds, \quad dr=dt, \quad \text{“ “} \quad \text{III quadrant} \quad (6)$$

$$(\rightarrow \text{vacuum}) \quad dr=dt, \quad dr=-dt \quad \text{so } dt=0=dr \quad (7)$$

We square eq.4  $ds_1^2=(dr+dt)(dr+dt)=[dr^2+dt^2]+(dr dt+dt dr)\equiv ds^2+ds_3=ds_1^2$ . Since  $ds_3$  (is max or min) and  $ds^2$  (from eq.4) are invariant then so is **Circle**  $ds^2=dr^2+dt^2=ds_1^2-ds_3$ . Note this separate  $ds$  is a minimum at  $45^\circ$  and so **Circle** $\equiv\delta z=dse^{i\theta}=dse^{i(\Delta\theta+\theta_0)}=dse^{i((\cos\theta dr+\sin\theta dt)/(ds)+\theta_0)}$ ,  $\theta_0=45^\circ$ . We define  $k\equiv dr/ds$ ,  $\omega\equiv dt/ds$ ,  $\sin\theta\equiv r$ ,  $\cos\theta\equiv t$ .  $dse^{i45^\circ}\equiv ds'$ . So take the global ordinary dr derivative

$$\text{(since flat space) of 'Circle' } \frac{\partial \left( dse^{i\left(\frac{r dr}{ds} + \frac{t dt}{ds}\right)} \right)}{\partial r} = i \frac{dr}{ds} \delta z \text{ so } \frac{\partial (dse^{i(rk+wt)})}{\partial r} = ik\delta z, \quad k\delta z = -i \frac{\partial \delta z}{\partial r} \quad (8)$$

Cancel that  $e^{i45^\circ}$  coefficient then multiply both sides of eq.8 by  $\hbar$  and define  $\delta z\equiv\psi$ ,  $p\equiv\hbar k$ . Eq.8 then implies (Hermitian) operator  $\hbar k$  **observables** formalism(QM). See next paragraph for real k part, (also appendix B3). Eqs 4,5,6,8 and eq.3 Clifford algebra imply 2D Dirac equations for e,v.

**Needed Big -C to have random t and Hamiltonians (observability)**

**B Substitute** left side z into right side zz repeatedly of **eq.1** to get a Mandelbrot set **iteration** (for small C limit **eq.1** cases  $z\approx 1,0$ ). The right side extremum Cauchy seq. iteration defines **real** k (dr/ds eigenvalues) in eq.8. It's left side small dr dt (eq.3,  $\delta(dr dt)=0$ ) extremum is the fractal Feigenbaum pt. $=C_M$  Mandelbulb  $\delta z'$ . Note certain Cs have a higher density here so *perturbations*

**A&B Big  $\gamma$**   $(1/\gamma)\delta z$  boost means small  $C\approx\delta z\gg\delta z\delta z$  and so no more quadratic equation but still keeps our complex  $\delta z$  and so dt. So we must Fitzgerald contract (boost= $\gamma$ )  $\delta z$  to get small C and so  $z=zz$  and the **postulate** of **1**. So then boost  $C_M$  as in  $\delta z'=C=C_M/\gamma=C_M/\xi=r_H$  so  $\xi_1$  (defining mass) *must be big*. For  $z=1$  in  $z=1+\delta z$ ,  $\delta z$  is small and so in  $C_M=\xi\delta z$ ,  $\xi_1$  **is big** and so we got  $z=zz$  and the **postulate** of **1**. But for  $z=0$ ,  $\delta z$  is big so  $\xi_0$  is small and in  $\delta C_M=\delta\xi\delta z+\xi\delta\delta z=0$  then since  $\delta\delta z=0$  then  $\delta\xi$  small so  $\xi_0$  is both stable and small ( $\equiv$ electron). On small scales  $\delta z\gg\delta z\delta z$  so in eq.2  $|\delta z|\approx C=\text{constant}$  so can only perturb eq.4 at  $45^\circ$  using  $(dr-\delta z')+(dt+\delta z')\equiv dr'+dt'=ds$  (9) since  $ds=|\delta z|=C$ . Define  $\kappa_{rr}\equiv(dr/dr')^2=(dr/(dr-(C_M/\xi_1)))^2=1/(1-r_H/r)^2=A_1/(1-r_H/r)+A_2/(1-r_H/r)^2$   $r\equiv dr$ . The  $A_1$  term can be split off from RN (as in classic GR) and so  $\kappa_{rr}\approx 1/[1-((C_M/\xi_1)r)]$ . So we have:  $ds^2=\kappa_{rr}dr'^2+\kappa_{oo}dt'^2+..$ (10). Note from eq.3  $dr'dt'=\sqrt{\kappa_{rr}}dr\sqrt{\kappa_{oo}}dt=drdt$  so  $\kappa_{rr}=1/\kappa_{oo}$  so given that 2D perturbation we get curved space 4D. For 4D our eq.3 Clifford algebra then implies  $(\gamma^x \sqrt{\kappa_{xx}}dx+\gamma^y \sqrt{\kappa_{yy}}dy+\gamma^z \sqrt{\kappa_{zz}}dz+\gamma^t \sqrt{\kappa_{tt}}idt)^2=\kappa_{xx}dx^2+\kappa_{yy}dy^2+\kappa_{zz}dz^2-\kappa_{tt}dt^2=ds^2$ . Multiplying the bracketed term by  $1/ds$  &  $\delta z$  then eq 8 implies 4D **Newpde**  $\gamma^\mu(\sqrt{\kappa_{\mu\mu}})\partial\psi/\partial x_\mu=(\omega/c)\psi$  for e,v (11) (covariant derivative still ordinary since  $\psi$  (complex) scalar). Therefore **postulate1** $\rightarrow$ **Newpde**

Small C boost gets  $z=zz$  (so postulate 1) but also gets the **numerical value of Large  $\xi_1$**

For that stable  $z=0$  the only way to get stable large  $\xi$  (required by that small C boost) is with the Newpde **composite 3e**  $2P_{3/2}$  at  $r=r_H$  state (partII davidmaker.com). So *stability* ( $dt'^2=(1-r_H/r)dt^2$ ) clocks stop at  $r=r_H$ . The *two positron motion* and  $h/2e$  quantization of flux BA then gives us the exact proton mass  $m_p$  as a reduced mass for the associated Hund rule  $\tau \equiv 2S_{1/2}, 1S_{1/2} \equiv \mu$  states (so  $\tau + \mu = \xi_1, m_p = \xi_1/2$ ). We rewrite this in the Kerr metric formalism with the 3<sup>rd</sup> mass also reversing the pair annihilation (Thus virtual pair creation inside the  $r_H$  volume given  $\sigma = \pi r_H^2 \approx (1/20)$  barns) and reducing the inertial frame dragging due to the spin $^{1/2}$   $\xi_1$  thereby adding a Kerr metric  $-(a/r)^2$  angular momentum operator in  $\kappa_{oo} = 1 - (a/r)^2 - r_H/r = \xi_1 + \xi_o - C_M/(\xi_o r) = \tau + \mu + m_e - 2e^2/(\xi_o r) = 1 + \varepsilon + \Delta\varepsilon + 2e^2/(\xi_o r) = \kappa_{oo}$  (Fiegenbaum pt.  $C_M$  defines charge  $e^2$ ). Divide by  $\xi_1 = 1 + \varepsilon$  to normalize for only free electron  $\Delta\varepsilon$  energy (Needed for the following two electron applications in eqs.15,16) asymptotic local flat space and thereby finally getting back to that initial requirement for that free particle  $z=1$ , *large*  $\xi_1$  case:  $\kappa_{oo} = 1 - \xi_o/(1 + \varepsilon) - C_M/(\xi_1 r) = 1 + \Delta\varepsilon/(1 + \varepsilon) - 2e^2/(2m_p r)$  (12) also giving us the *numerical value* of that **large  $\xi_1$**  ( $=2m_p$ ). With  $\tau$  normalized to  $\tau=1$  with the Newpde ground state  $e$  mass then  $\Delta\varepsilon = m_e = .0005799$  with  $\varepsilon = \mu = .06$ . (12a)